

This Latin square design is used to test
 three varieties of rhubarb.
Adapt the experiment so that each variety is also tested for three different fertilisers: $A, B$ and $C$.

These are called Graeco-Latin squares.

The problem is much more difficult with 4 crop varieties and 4 fertilisers.
There are 4 really different possible Latin square designs - and for some of them, there is no Graeco-Latin solution.

For each design: either find a solution or prove that it is impossible.

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Amazing fact: For order 11, there are 5363937773277371298119673540771840 different Graeco-Latin squares! Proved in 2005 by McKay and Wanless

