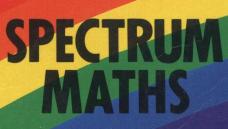
# go further with NUMBER SKILLS

### For National Curriculum levels 3-6

1995 CURRICULUNI



A 372.7 KIR



## go further with NUMBER SKILLS

### For National Curriculum levels 3-6

### **SPECTRUM MATHS**

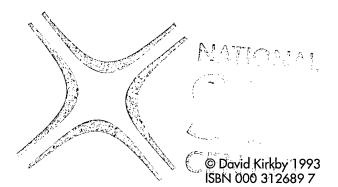
### Dave Kirkby



้เ<mark>al</mark> *blishers* 

An i

•



Published by 1993 by Collins Educational An imprint of HarperCollins Publishers 77-85 Fulham Palace Road, Hammersmith, London W6 8JB

Reprinted 1994, 1996

The purchase of this copyright material confers the right on the purchasing institution to photocopy the pupils' pages and special paper pages without any specific authorisation by the publisher. No other part of this publication may be reproduced, stored in a retrieval system, or transmitted in any form or by any means, electronic, mechanical, photocopying, recording or otherwise, without the prior permission of the publisher.

*Illustrated by* Teri Gower

*Designed by* Shireen Nathoo Design

Cover photographs of children by Olly Hatch

Acknowledgement We should like to thank NES Arnold Ltd, Nottingham, for kindly lending us the pictures of educational equipment for the cover.

Printed in Great Britain by Martin's The Printers Ltd Berwick upon Tweed

Bound in Great Britain by Hunter & Foulis, Edinburgh

### THE SPECTRUM MATHS SERIES

Starting	More	Go Further With
Investigations	Investigations	Investigations
Games	Games	Games
Data Handling	Data Handling	Data Handling
Algebra/Shape and Space	Algebra/Shape and Space	Algebra/Shape and Space
Number Skills	Number Skills	Number Skills

### CONTENTS

فأر

- **1** The Big Wheel
- 2 Magic Squares
- **3** Grid Journeys
- 4 Tenths
- **5** Powers
- 6 Countdown
- 7 Mixed Equations
- 8 Nearly 20
- 9 5-Card Sums
- **10** Double See-Saw
- **11** Lowest Common Multiples
- **12** Factor Show
- **13** Three Stones
- **14** Number Puzzles
- 15 A Special Date
- **16** Multiplying Grids
- 17 Minus a Digit
- **18** Factor Grids
- **19** Remainder Charts
- 20 Multiple Percentages

- 21 Division Grids
- 22 Place Nine
- 23 Multiples of 10
- 24 Division Wheels
- 25 Highest Common Factors
- 26 Hexanimals
- 27 Subtraction Guessing
- 28 Goal Percentages
- 29 Consecutive Flowers
- **30** Fraction Wheels
- **31** Fractions and Decimals
- 32 One Hundred
- **33** Tridiscs
- **34** Multiplication Triangles
- 35 Mixed totals
- **36** Percentage Wheels
- **37** Five Ways
- 38 Take Your Pick
- **39** Decimal Pyramids
- 40 Tower Blocks

### INTRODUCTION

Most schools use a mathematics scheme and teachers using these require a range of support material to supplement the scheme. Such material is provided by **Spectrum Maths**.

#### SPECTRUM MATHS: NUMBER SKILLS

This is a series of three books of number activities primarily for Key Stages 1 and 2, though much of it is also appropriate for Key Stage 3.

The books are defined in terms of three levels. Broadly, these levels are :

**Starting** Number Skills (Years 1, 2 and 3) **More** Number Skills (Years 3, 4 and 5) **Go Further With** Number Skills (Years 5, 6 and 7).

Each book contains:

40 pupil activities in the form of photocopymasters. There are also detailed teacher's notes accompanying each activity and Special Papers in the form of photocopymasters

to help children record their work.

#### THE ACTIVITIES

A principal aim of mathematics teaching is to equip children to handle numbers with confidence. These activities provide an opportunity for children to practise number skills, with a strong emphasis on operational skills.

Each activity contains empty **number boxes** which children are required to complete, or sometimes colour. In most cases this is followed by an appropriate extension activity.

#### **USING THE ACTIVITIES**

The activities do not, in general, attempt to teach children the number skills they need. They provide practice and reinforcement for children who, having been introduced to the skills, need experiences to develop them.

Activities can be selected by the teacher to suit particular needs and situations. They can be used in a variety of ways:

- to integrate into the school mathematics programme
- to consolidate other work in the school mathematics scheme
- to provide enrichment material at appropriate times
- to form support material for responding to wide ranges of ability
- to complement other activities within the Spectrum Maths series.

In particular, many activities in the **Spectrum Games** and **Spectrum Investigations** series can be used in conjunction with this series to provide rich and varied opportunities for children to develop their skills.

#### THE TEACHER'S NOTES

The teacher's notes contain, for each activity:

- clear indications of the content area
- details of any necessary apparatus
- notes outlining suggestions for introducing the activities
- ideas for extending the activities
- answers to the activities
- clearly identifiable National Curriculum references on a grid
- reference to related activities within the book and other books in the Spectrum Maths series.

### **USING THE TEACHER'S NOTES**

	LEVEL	UA	N	SSM	HD	A
	1					
	2					
	3					
	4					
	5					
	6					
KE	EY UA N	Numbe	er			
		_	-	e and M	easure	es
	HD	Handli	ng Da	ata		

- HD Handling I
- A Algebra

#### SKILLS

This section summarises the main content area of the activity.

#### APPARATUS

Details of necessary apparatus or special paper photocopymasters which are included at the back of the book

#### NOTE

This section contains suggestions for introducing the activity.

#### EXTENSION

This contains ideas for extending the activity.

This section contains answers to the activity. These appear as a reduced copy of the pupil activity sheet.

The table on the left refers to the Programmes of Study and Levels 1–6 of the National Curriculum. An algebra column has been included for teachers using this book at Key Stage 3. An attempt has been made to locate, by means of dots in the table, the approximate content level for each activity, but it must be appreciated that many activities can be performed at a variety of levels.

	Data Handling	Games	Investigations	Algebra / S&S	Number Skills
Starting					
More	Th		ted activities available the gives the number and tit		eries.
Go Further With					



### The Big Wheel

LEVEL	UA	N	SSM	HD	A
1					
2		•			
3		•			
4					
5					
6					

• Learning and using addition and subtraction facts.

#### SKILLS

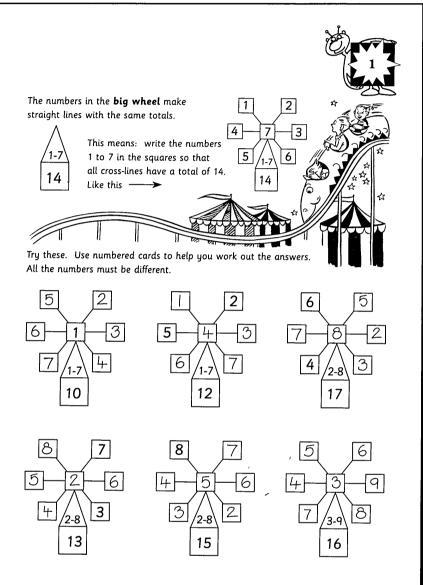
- Adding three single-digit numbers
- Searching for sets of numbers which have a given total

#### APPARATUS

Numbered cards, 1-9

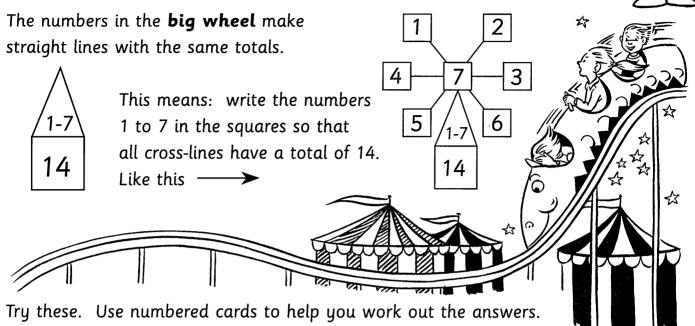
#### NOTE

Suggest to the children that they draw a large wheel on paper, then use numbered cards placed on the wheel to help them find solutions.

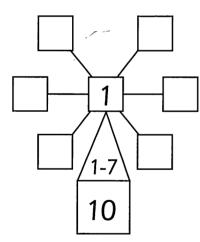


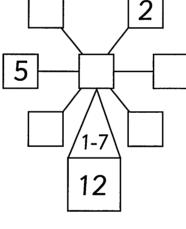
	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting			23 Dice Sort		
More		26 Fifteens	2 Lucky 13 11 Triplets		<ul> <li>25 Addition Grids</li> <li>34 Magic Windmills</li> <li>35 Magic Triangles</li> <li>38 Side Totals</li> </ul>

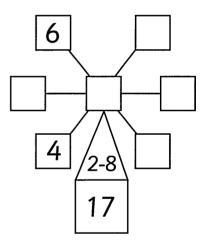
### The Big Wheel

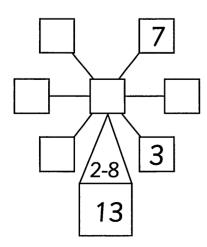


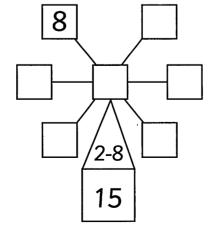
All the numbers must be different.

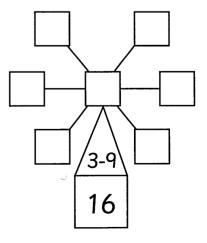














### **Magic Squares**

LEVEL	.UA	Ν	SSM	HD	A
1					
2	Ċ,	٠			
3	1	٠			
4					
5					
6					

• Learning and using addition and subtraction facts to 20.

• Adding three single-digit numbers.

#### SKILLS

- Adding three single-digit numbers
- Searching for arrangements of numbers within a 3 x 3 grid for given row and column totals

#### APPARATUS

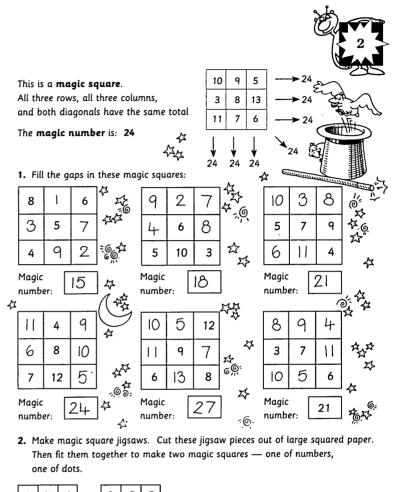
Squared paper, scissors

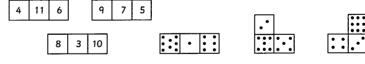
#### NOTE

The solutions can be deduced by systematically working round the square.

#### EXTENSION

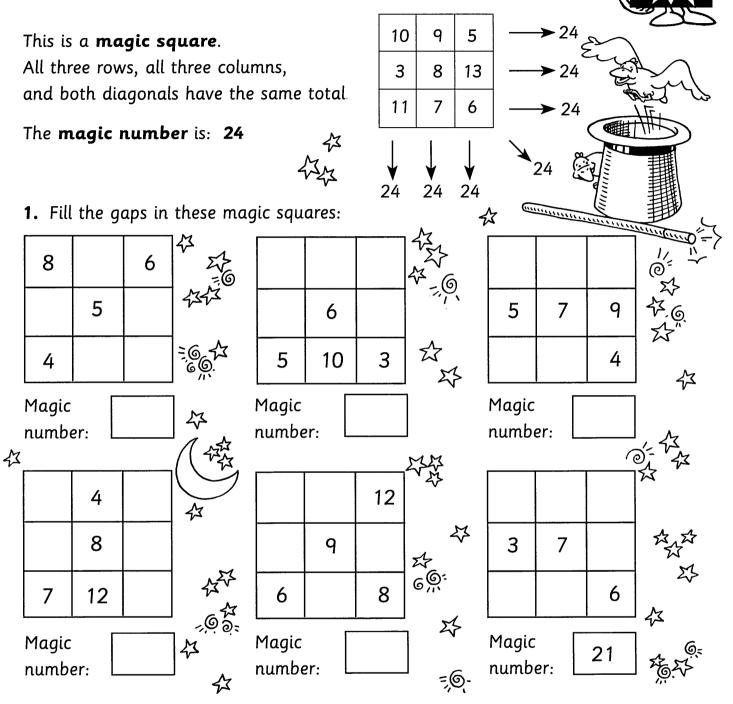
Create 4 x 4 magic squares using, for example, the numbers 1-16.



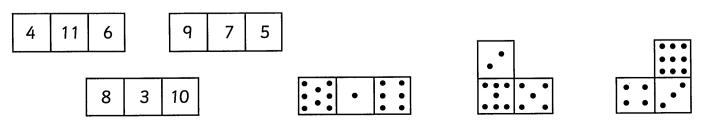


	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More		26 Fifteens			<ul> <li>18 2 x 2 Addition Squares</li> <li>25 Addition Grids</li> <li>26 Cloud Numbers</li> </ul>
Go Further With					22 Place Nine

### **Magic Squares**



 Make magic square jigsaws. Cut these jigsaw pieces out of large squared paper. Then fit them together to make two magic squares — one of numbers, one of dots.





### **Grid Journeys**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•				
4	٠	•			
5					
6					

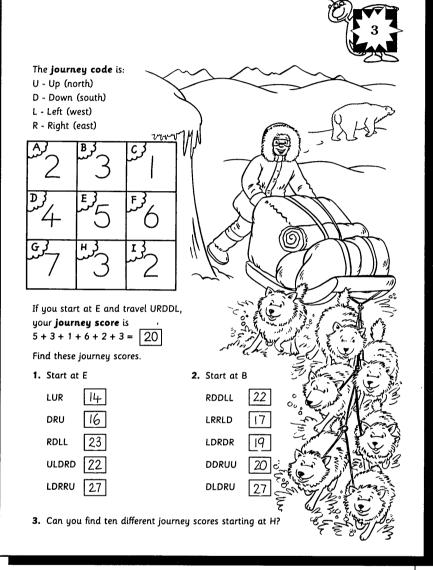
- Addition of several single-digit numbers.
- Giving and understanding instructions for movement along a route.

#### SKILLS

Finding a running total when adding several single-digit numbers Following a path on a grid based on left, right, up, down movements

#### **EXTENSION**

Ask children to draw up a larger (say, 4 x 4) grid and work out routes for friends to follow.



#### Question 3: Some different journey scores starting at H are:

Three stages:

Two stages: LU - 3 + 7 + 4

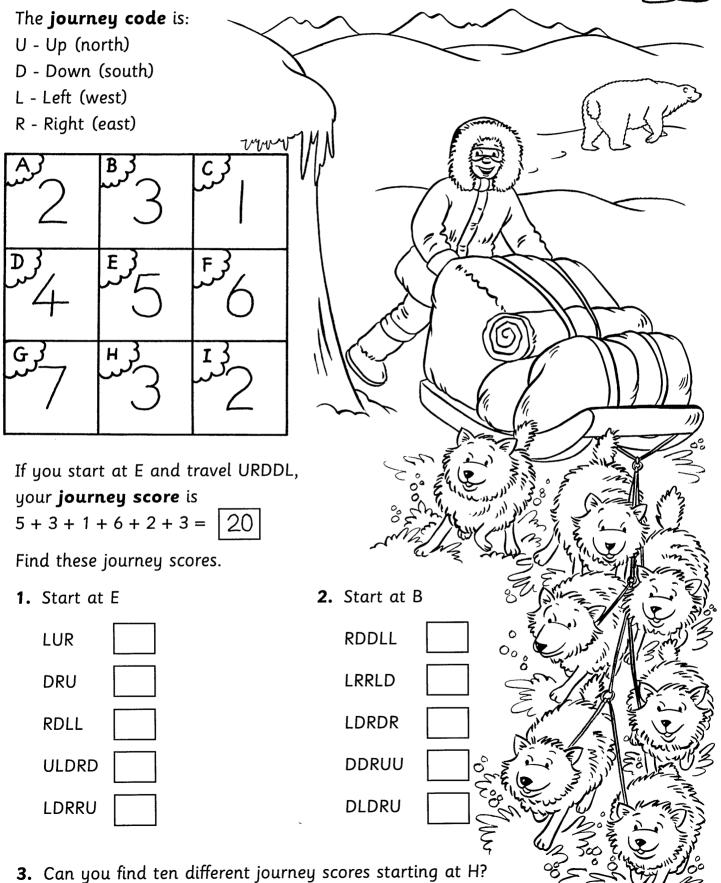
	5
LU - 3 + 7 + 4 = 14	UUR - 3 + 5 + 3 + 1 = 12
UL - 3 + 5 + 4 = 12	UUL - 3 + 5 + 3 + 2 = 13
RU - 3 + 2 + 6 = 11	URU - 3 + 5 + 6 + 1 = 15
UR - 3 + 5 + 6 = 14	ULU - 3 + 5 + 4 + 2 = 14
UU - 3 + 5 +3 = 11	URD - 3 + 5 + 6 + 2 = 16

SPECTRUM L	INKS.
------------	-------

Data Handling	Games	Investigations	Algebra/S&S	Number Skills
				32 Number Journey
	Data Handling	Data Handling Games	Data Handling Games Investigations	Data Handling Games Investigations Algebra/S&S

### **Grid Journeys**







### **Tenths**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•				
4	•	•			
5					
6					

- Using, with understanding, decimal notation, in the context of measurement.
- Approximating.

#### SKILLS

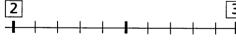
- Locating position on a number line using tenths
- Rounding decimals to the nearest whole number

#### **APPARATUS**

Squared paper

#### **EXTENSION**

Children can be given further practice with the use of a 10-point number line on the wall. Vary the number cards at the ends of the line, for example:





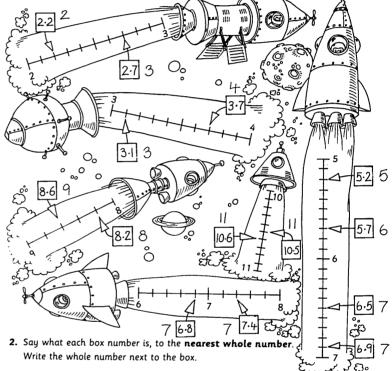
Discussion will arise regarding the nearest whole number to 10.5, for example.

#### **SPECTRUM LINKS**

#### 6.5 7 7.4 7 6.8 7 $\frac{1}{2}$ 2. Say what each box number is, to the nearest whole number Write the whole number next to the box. 3. Draw your own number lines using squared paper. Then draw boxes to show the position of some numbers. Ask a friend to fill in the boxes. 3 6 ..... . ...

These number lines are marked in tenths or fifths.

1. Complete the boxes to show where the arrow points on each number line. Show it in **decimals**. The first one has been done for you.



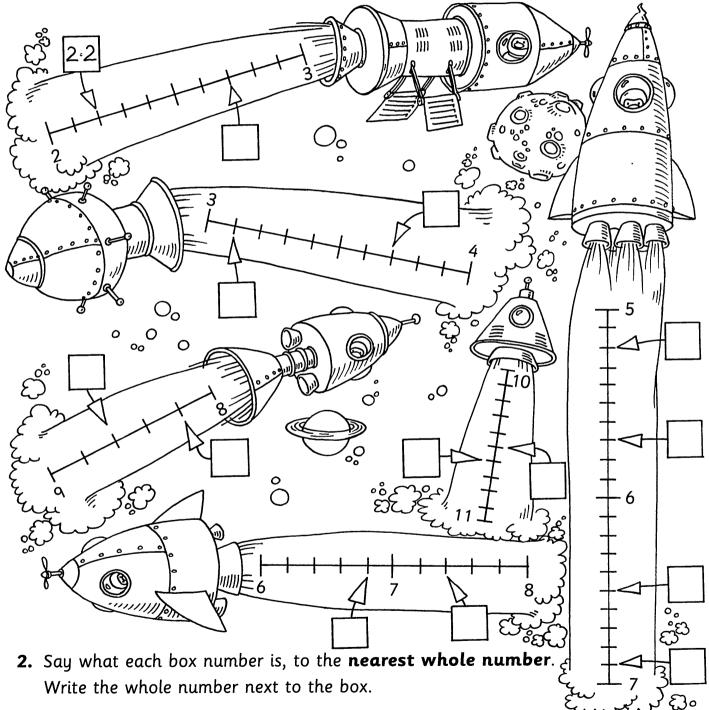
	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More					11 Temperature Scales 27 Nearest 100 29 Nearest 10
Go Further With	<ul><li>9 Inches and Centimetres</li><li>18 Miles and Kilometres</li></ul>	<ul><li>12 Decimate</li><li>14 Two Places</li><li>37 Four Rounds</li></ul>	20 Nearest Wholes		<ul><li>31 Fractions and Decimals</li><li>39 Decimal Pyramids</li></ul>

### Tenths



These number lines are marked in **tenths** or **fifths**.

 Complete the boxes to show where the arrow points on each number line. Show it in **decimals**. The first one has been done for you.



3. Draw your own number lines using squared paper.Then draw boxes to show the position of some numbers.Ask a friend to fill in the boxes.



### Powers

LEVEL	UA	N	SSM	HD	A
1					
2					
3	•	•			
4	•	•			
5	•				
6					

- $10 \times 10$  and using them in multiplication and division problems.
- Explaining number patterns and predicting subsequent numbers.
  Generalising, mainly in words, patterns which arise, eg 'square'.

#### SKILLS

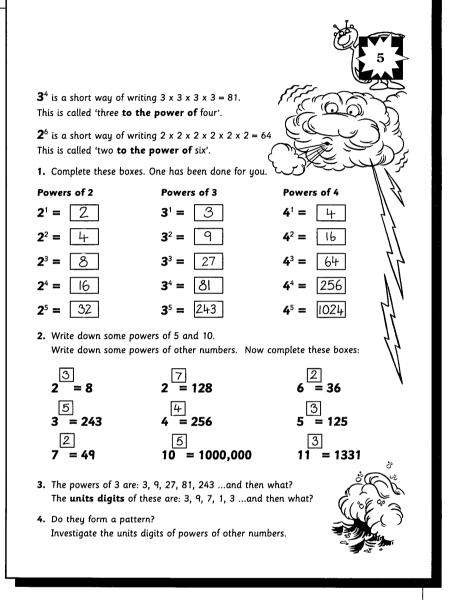
 Expressing numbers using power notation

#### APPARATUS

Calculators

#### NOTES

Children may need help with the idea of 'to the power of one'. They may also need the term 'units digit' explained.



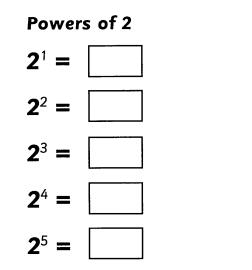
Question 3: 729; 9 Question 4: The patterns in the units digits of powers are: Powers of 2: 2, 4, 8, 6, ..... Powers of 3: 3, 9, 7, 1, ..... Powers of 4: 4, 6, 4, 6, ..... Powers of 5: 5, 5, 5, 5, ..... Powers of 6: 6, 6, 6, 6, ..... Powers of 7: 7, 9, 3, 1, ..... Powers of 8: 8, 4, 2, 6, ..... Powers of 9: 9, 1, 9, 1, .....

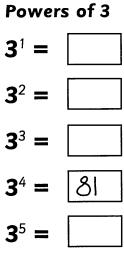
### Powers

 $\mathbf{3}^4$  is a short way of writing  $3 \times 3 \times 3 \times 3 = 81$ . This is called 'three **to the power of** four'.

**2**<sup>6</sup> is a short way of writing  $2 \times 2 \times 2 \times 2 \times 2 \times 2 = 64$ This is called 'two **to the power of** six'.

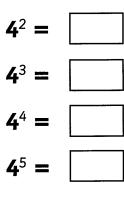
1. Complete these boxes. One has been done for you.



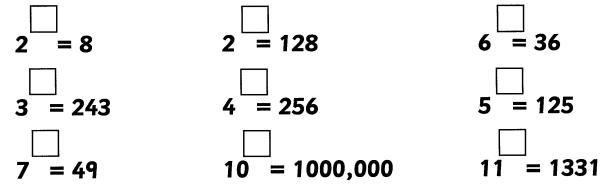


Powers of 4

 $4^{1} =$ 

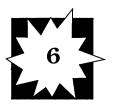


Write down some powers of 5 and 10.
 Write down some powers of other numbers. Now complete these boxes:



- **3.** The powers of 3 are: 3, 9, 27, 81, 243 ...and then what? The **units digits** of these are: 3, 9, 7, 1, 3 ...and then what?
- **4.** Do they form a pattern? Investigate the units digits of powers of other numbers.





### Countdown

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•	•			
4		•			
5	•				
6					

- Addition, subtraction, and multiplication.
- Approximating.

#### SKILLS

 Writing expressions for numbers using combinations of a given set of digits and operations

#### NOTE

If children cannot find a solution, then they must aim to be as close as possible.

#### EXTENSION

Ask the children to work with the first set of useful numbers, and suggest they try to make as many target numbers as possible, within a particular range (100-200, for example). These **target numbers** can be made from the **useful numbers**. **1.** Try these. Use each **useful number** once only in a line.

¥2

☆

You can use multiplication, addition and subtraction. How many of these ten targets can you reach? Write your answers in the **results** column. (The first one has been done for you.)

Target numbers	Useful numbers	Result
336	100 8 4 3 1 7	(3×100)+(4×7)+8
132	100 <sup>3</sup> 5 <sup>4 6</sup> 2	100 + (5 X 6) + 2
256	100 1 7 8 9 2	(2 X 100) + (7 X 8)
410	100 <sup>3</sup> 5 <sup>8</sup> 4 1	(4 x 100) + 8 + 5 - 3
314	100 <sup>5</sup> 6 <sup>3</sup> 2 <sup>1</sup>	(3×100)+5+2+6+1
680	100 <sup>7</sup> 8 <sup>9 4</sup> 2	(7 x 100)-4-(2 x 8)
823	200 4 7 2 3 5	(4×200)+(3×7)+2
856	200 8 3 2 4 6	(4 x 2 <i>0</i> 0) + (6 x 4 x 2)+8
525	100 2 7 1 4 5	(5 x 100) + (4 x 7) - 2 - 1
186	100 2 <sup>6</sup> 7 <sup>5</sup> 4	(2x100)-5-6-7+4

2. Invent a set of your own target numbers and useful numbers. See how many targets you can reach.

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting		<ul><li>13 Big Match</li><li>18 Summary</li><li>27 Choosy</li></ul>	10 Trios 12 Keep Your Balance 14 Card Tricks	<ul><li>6 Shape Search</li><li>10 Stroking Cats</li><li>15 Hunt the Numbers</li></ul>	
More		3 Boxer 8 Dice Superstars	29 Asking Questions	<b>10</b> Mystery People	<ol> <li>Dice Lines</li> <li>Equation Solving</li> <li>Arch Numbers</li> <li>Target Practice</li> </ol>
Go Further With		<ul><li>8 A Mouthful</li><li>33 Challenge</li><li>38 Switch</li></ul>	16 Number Nine 21 Equations 33 Signs	<ul><li>7 Number Tricks</li><li>10 Think of a Number</li><li>14 Whodunnit?</li></ul>	<ul><li>7 Mixed Equations</li><li>13 Three Stones</li><li>15 A Special Date</li></ul>

### Countdown



1727

47

These **target numbers** can be made from the **useful numbers**.

 Try these. Use each useful number once only in a line. You can use multiplication, addition and subtraction. How many of these ten targets can you reach? Write your answers in the results column. (The first one has been done for you.)

Target numbers	Useful numbers	Result
336	100 8 4 3 1 7	(3×100)+(4×7)+8
132	100 <sup>3</sup> 5 <sup>4 6</sup> 2	
256	100 1 7 8 9 2	
410	100 <sup>3</sup> 5 <sup>8</sup> 4 1	
314	100 <sup>5</sup> 6 <sup>3</sup> 2 <sup>1</sup>	
680	100 7 8 9 4 2	
823	200 4 7 2 3 5	
856	200 8 3 2 4 6	
525	100 2 7 1 4 5	
186	100 2 <sup>6</sup> 7 <sup>5</sup> 4	

Invent a set of your own target numbers and useful numbers.
 See how many targets you can reach.



### **Mixed Equations**

LEVEL	UA	N	SSM	HD	A
1					
2					
3	٠	٠			
4	•	•			
5	•	•			
6					

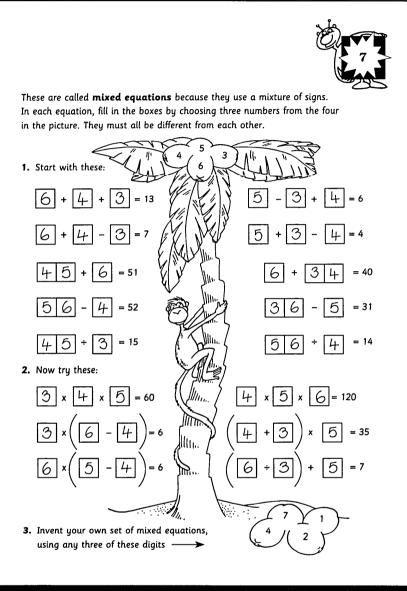
- Addition, subtraction, multiplication and division.
- Simple equations.

#### SKILLS

- Finding solutions to a variety of different equations with three missing digits to be selected from four
- Adding, subtracting, multiplying, dividing, and combinations of these

#### NOTE

Discuss the need for brackets and encourage children to use these when they are creating their own equations.

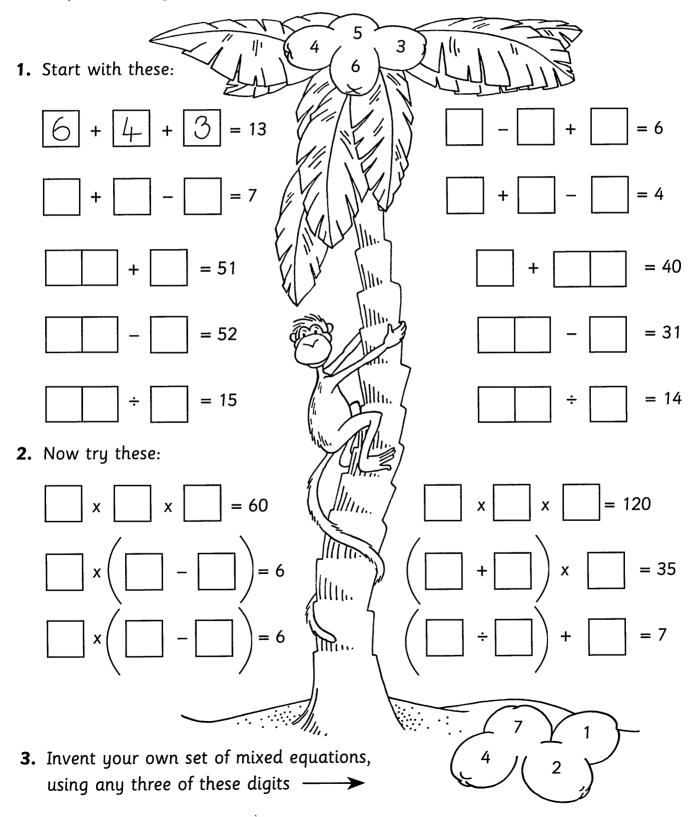


	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting		<ul><li>13 Big Match</li><li>18 Summary</li><li>27 Choosy</li></ul>	<ol> <li>10 Trios</li> <li>12 Keep Your Balance</li> <li>14 Card Tricks</li> </ol>	<ul><li>6 Shape Search</li><li>10 Stroking Cats</li><li>15 Hunt the Numbers</li></ul>	
More		3 Boxer 8 Dice Superstars	29 Asking Questions	10 Mystery People	<ol> <li>Dice Lines</li> <li>Equation Solving</li> <li>Arch Numbers</li> <li>Target Practice</li> </ol>
Go Further With		<ul><li>8 A Mouthful</li><li>33 Challenge</li><li>38 Switch</li></ul>	16 Number Nine 21 Equations 33 Signs	<ul><li>7 Number Tricks</li><li>10 Think of a Number</li><li>14 Whodunnit?</li></ul>	<ul><li>6 Countdown</li><li>13 Three Stones</li><li>15 A Special Date</li></ul>

### **Mixed Equations**



These are called **mixed equations** because they use a mixture of signs. In each equation, fill in the boxes by choosing three numbers from the four in the picture. They must all be different from each other.





### Nearly 20

LEVEL	UA	N	SSM	HD	A
1					
2					
3	•				
4	•	•			
5	•				
6					

- Adding and subtracting two two-digit numbers.
- Estimating and approximating to check the validity of addition and subtraction calculations.

#### SKILLS

- Subtracting two-digit numbers
- Creating subtractions by selecting from a choice of digits to give a particular answer

#### **APPARATUS**

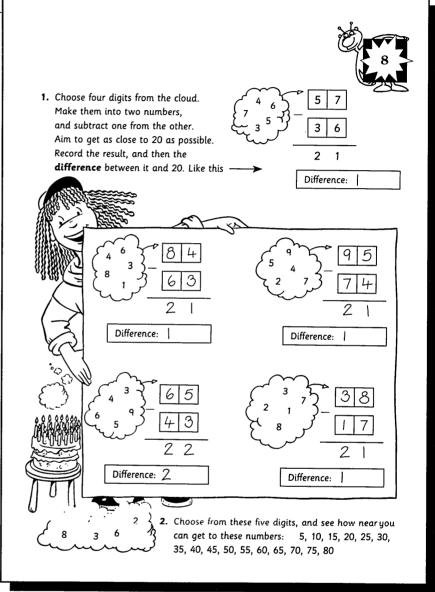
Numbered cards, 1-9

#### NOTE

This activity can be started by drawing a large outline of the subtraction on a piece of paper, selecting the appropriate numbered cards, and then trying different arrangements to produce the best solution.

#### EXTENSION

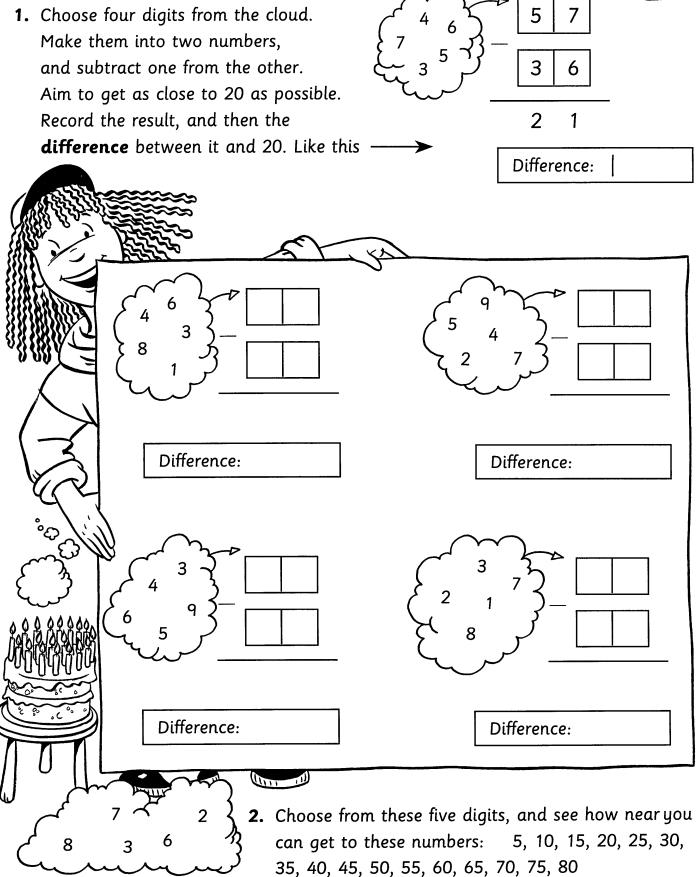
 Ask children to explore how many different answers can be created for any one set of numbers.



	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting			17 Totals		
More			25 4-Card Fun		7 What's Missing? 22 Nearly 60 36 Differences
Go Further With					<ul> <li>9 5-Card Sums</li> <li>17 Minus a Digit</li> <li>27 Subtraction Guessing</li> <li>35 Mixed Totals</li> </ul>

### Nearly 20







### **5-Card Sums**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•				
4	•	•			
5	•				
6					

Adding two two-digit numbers.
 Estimating and approximating to check the validity of addition and subtraction calculations.

#### SKILLS ·

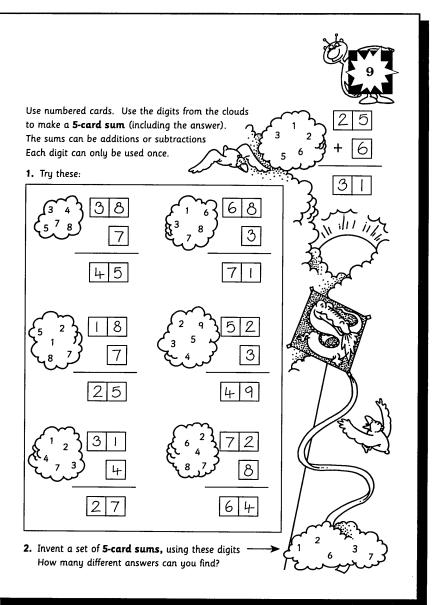
- Adding a single-digit number to a twodigit number
- Arranging five digits to create both the addition and the result

#### **APPARATUS**

Numbered cards, 1-9

#### NOTES

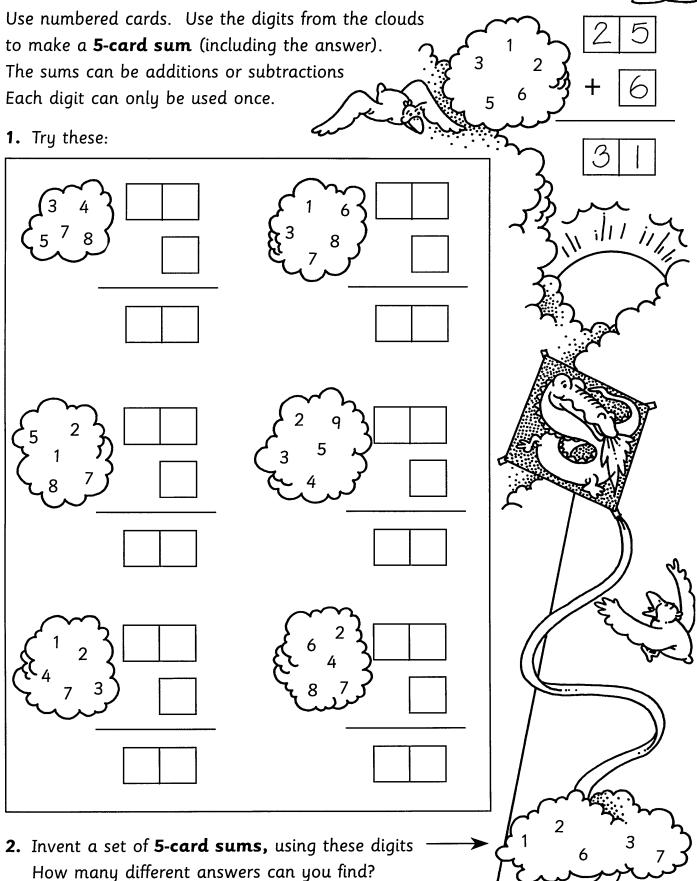
Start by asking children to draw a large outline of the addition on a piece of paper. Then select the appropriate numbered cards for each addition and arrange them in search of a solution.



	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting			17 Totals		
More			<b>25</b> 4-Card Fun		7 What's Missing? 22 Nearly 60 36 Differences
Go Further With					<ul> <li>8 Nearly 20</li> <li>17 Minus a Digit</li> <li>27 Subtraction Guessing</li> <li>35 Mixed Totals</li> </ul>

### **5-Card Sums**







### **Double See-Saws**

LEVEL	UA	Ν	SSM	HD	A
1					
2		•			
3	•	٠			
4	٠				
5	0				
6		1	1		

• Learning and using addition and subtraction facts.

#### SKILLS

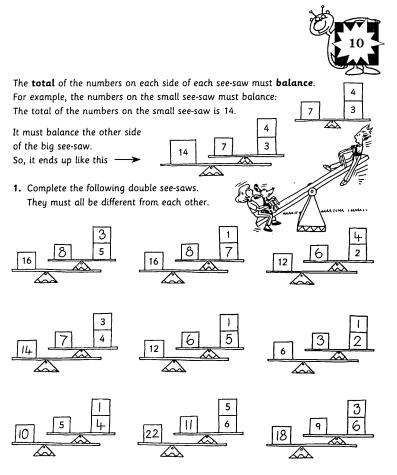
 Matching one number to the total of several others

#### **APPARATUS**

Numbered cards, 1-20

#### NOTES

Suggest to children that they draw a picture of a large double see-saw and use numbered cards on this to help them find answers. Note that the left-hand number must be even, for whole number solutions.



- 2. Can you find four different solutions to the last see-saw in question one?
- **3.** Can you find four different ways of balancing numbers, none of which are more than 10?
- 4. Can you find some ways of balancing numbers which are all even?

Question 2: possible solutions include 1 and 8, 2 and 7, 3 and 6, 4 and 5 on the right-hand arm of the small see-saw.

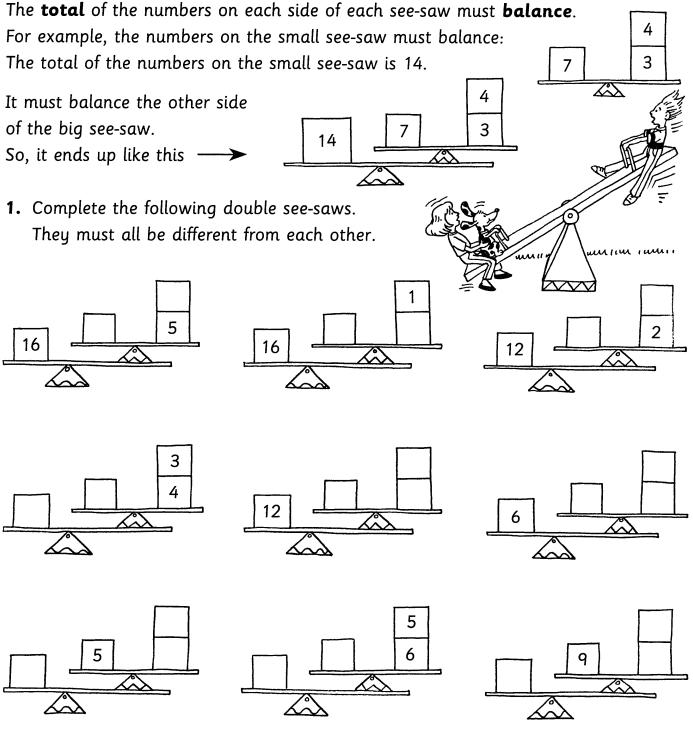
Question 3: balance 10 with 5 and 2 + 3 and with 5 and 1 + 4. Balance 8 with 4 and 3 + 1. Balance 6 with 3 and 1 + 2.

Question 4: possible solutions include: balancing 20 with 10 and 4 + 6; and balancing 16 with 8 and 6 + 2.

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting			12 Keep Your Balance		30 3-Number See-Saws 37 4-Number See-Saws
More					2 Pairs See-Saw

### **Double See-Saws**

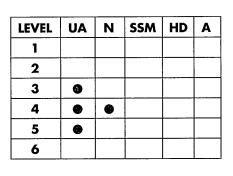




- 2. Can you find four different solutions to the last see-saw in question one?
- **3.** Can you find four different ways of balancing numbers, none of which are more than 10?
- 4. Can you find some ways of balancing numbers which are all even?



### **Lowest Common Multiples**



Multiplication facts up to 10 × 10.
Patterns in multiples.

#### SKILLS

 Finding the lowest common multiple of two numbers

#### NOTES

Ask the children to discuss any pattern they find in the table. Which numbers most often appear in the table as lowest common multiples?

#### EXTENSION

The activity could be extended to multiples of numbers greater than 10. To find the **lowest common multiples** of 3 and 4: look in the x 3 row, **and** in the x 4 row.

List all the numbers you see in both (12, 24, 36, etc.) and then choose the lowest one. It is **12**.

Now list the numbers which appear in both the x 6 row and the x 10 row. Find the lowest common multiple of 6 and 10. It is 30.

These lowest common multiples are written in the table below.

							_	18	1	1
									5	Ą
x2	2	4	6	8	10	12	14	16	18	20
х3	3	6	9	12	15	18	21	24	27	30
x4	4	8	12	16	20	24	28	32	36	40
x5	5	10	15	20	25	30	35	40	45	50
x6	6	12	18	24	30	36	42	48	54	60
x7	7	14	21	28	35	42	49	56	63	70
x8	8	16	24	32	40	48	56	64	72	80
x٩	9	18	27	36	45	54	63	72	81	90
x10	10	20	30	40	50	60	70	80	90	100

- Now find some lowest common multiples for yourself.
   First, choose one of the numbers on the left of the table below.
   Then choose a number from along the bottom.
   Using the table above, find the lowest common multiple of these two numbers.
   When you have found it, write it on the table, in the right square.
- Find the rest of the lowest common multiples to complete the table.



10	10	30	20	10	30	70	40	90	10
9	18	9	36	45	18	63	72	9	90
8	8	24	16	40	24	56	8	72	40
7	14	21	28	35	42	7	56	63	70
6	6	6	12	30	6	42	24	18	30
5	10	15	20	5	30	35	40	45	10
4	4	12	4	20	12	28	16	36	20
3	6	3	12	15	6	21	24	9	30
2	2	6	4	10	6	14	8	18	10
	2	3	4	5	6	7	8	9	10

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More			6 Table Patterns 8 Table Ends	<ol> <li>6 Multiple Gaps</li> <li>12 Sift the Multiples</li> <li>18 Patterns With 9</li> </ol>	<ol> <li>Factor Pairs</li> <li>Cloud Numbers</li> <li>The Right Boxes</li> </ol>
Go Further With	<ul><li>26 Sevens</li><li>36 Multiplication</li><li>Tables</li></ul>	<ul><li>17 Fives and Threes</li><li>24 Multiple Choice</li></ul>	13 Tables 37 Multiples	17 Factor Graph	20 Multiple Percentages

### Lowest Common Multiples

#### To find the lowest common multiples

of 3 and 4: look in the x 3 row, **and** in the x 4 row. List all the numbers you see in both (12, 24, 36, etc.) and then choose the lowest one. It is **12**.

Now list the numbers which appear in both the x 6 row and the x 10 row. Find the lowest common multiple of 6 and 10. It is 30. These lowest common multiples are

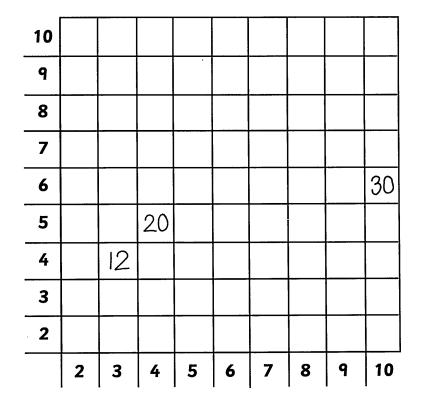
written in the table below.

x2	2	4	6	8	10	12	14	16	18	20
х3	3	6	q	12	15	18	21	24	27	30
x4	4	8	12	16	20	24	28	32	36	40
x5	5	10	15	20	25	30	35	40	45	50
x6	6	12	18	24	30	36	42	48	54	60
x7	7	14	21	28	35	42	49	56	63	70
<b>x8</b>	8	16	24	32	40	48	56	64	72	80
<b>x9</b>	9	18	27	36	45	54	63	72	81	90
x10	10	20	30	40	50	60	70	80	90	100

Now find some lowest common multiples for yourself.
 First, choose one of the numbers on the left of the table below.
 Then choose a number from along the bottom.
 Using the table above, find the lowest common multiple of these two numbers.
 When you have found it, write it on the table, in the right square.

**2.** Find the rest of the lowest common multiples to complete the table.







### **Factor Show**

LEVEL	UA	Ν	SSM	HD	Α
1					
2					
3	•				
4	•	۲			
5	•				
6					

• Factors.

#### SKILLS

 Searching for and recording factors of different numbers

#### APPARATUS

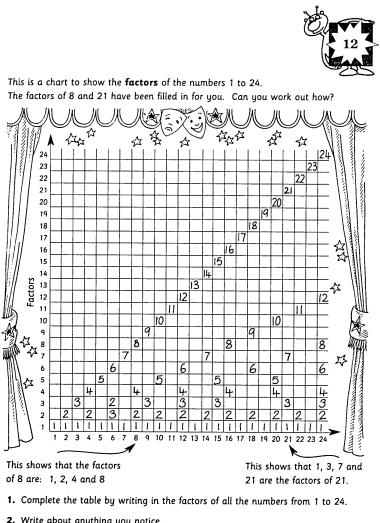
Squared paper (for the extension)

#### NOTES

Using a multiplication square can help in the search for factors, particularly with numbers beyond 24. The resulting charts can provide a useful display to help with the exploration of factors and primes.

#### **EXTENSIONS**

- Point out to children that most numbers have two or four factors. Ask, Which do not?
- Ask children to make an extended table on squared paper, to show factors of numbers greater than 24.



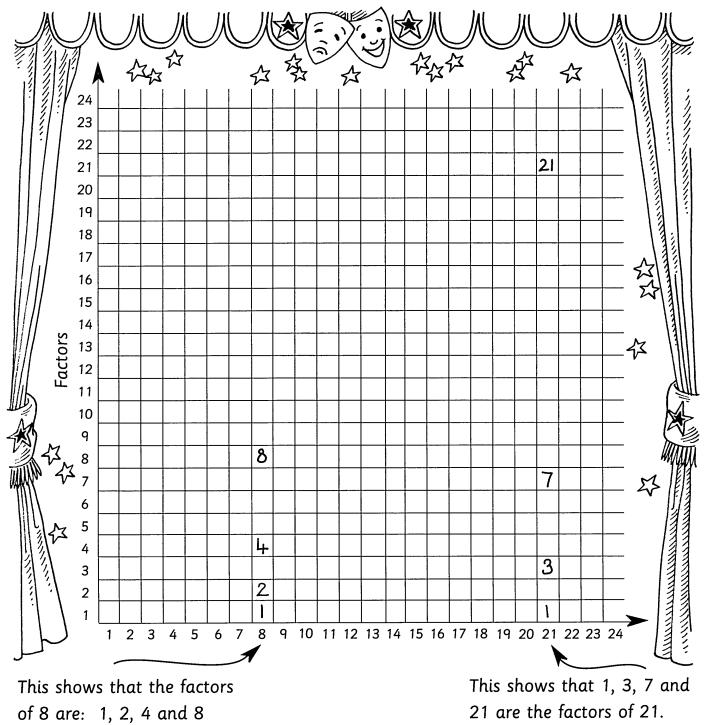
Write about anything you notice.
 Which numbers have the most factors? Which the least?

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More		37 Snake Bite 38 Divido	<ol> <li>6 Table Patterns</li> <li>7 Pick Your Cards</li> <li>8 Table Ends</li> </ol>	<ul> <li>8 Completing Rectangles</li> <li>12 Sift the Multiples</li> <li>13 Table Patterns</li> </ul>	16 Factor Pairs 26 Cloud Numbers
Go Further With		<ol> <li>Race Track</li> <li>Factor</li> <li>Multiple Choice</li> </ol>	9 Factors 13 Tables	<ul><li>4 Prime Numbers</li><li>17 Factor Graph</li><li>18 Multiplication Machines</li></ul>	<ol> <li>Lowest Common Multiples</li> <li>Factor Grids</li> <li>Highest Common Factors</li> </ol>

### **Factor Show**



This is a chart to show the **factors** of the numbers 1 to 24. The factors of 8 and 21 have been filled in for you. Can you work out how?



- 1. Complete the table by writing in the factors of all the numbers from 1 to 24.
- 2. Write about anything you notice.Which numbers have the most factors? Which the least?



### **Three Stones**

LEVEL	UA	N	SSM	HD	A
1					
2					
3	•	٠			
4	•	•			
5	•	٠			•
6					

- Addition, subtraction, multiplication and division.
- Simple equations.

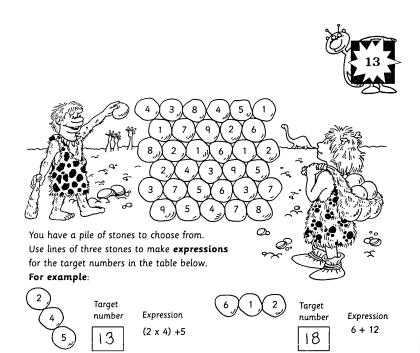
#### SKILLS

 Creating expressions for numbers using combined operations of addition, subtraction, multiplication and division

#### EXTENSION

Ask the children to explore as many different solutions as can be found from a given number. For example:

18 6 12 = 6 + 12 7 92 = 7 + 9 + 2 6 9 = 6 + 9 + 3



1. Write in as many expressions for the target numbers in the table as you can.

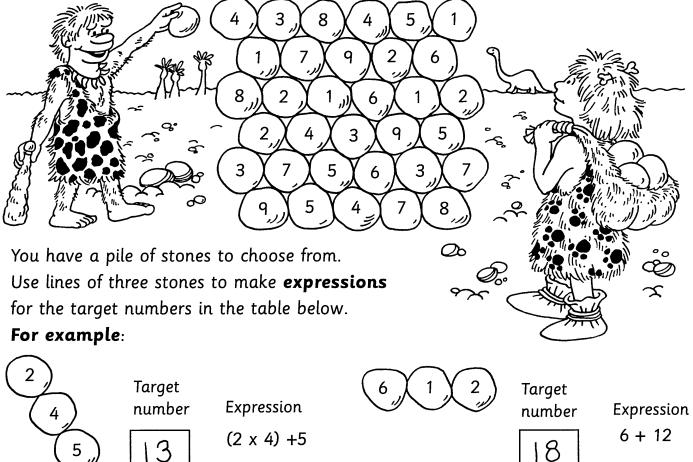
Target number	Expression	Target number	Expression
13	‰ (2 x 4) +5	18	000 6+12
8	000 4+5-1	24	000 (9X2)+6
14	200 2+7+5	19	Que 13+6
6	@ (4+2) XI	23	@@ (8X2)+7
25	030 (6 X 3) + 7	44	600 45-1
10	000 9+5-4	28	300 (3X8)+4
72	090 (7+5)×6	51	©@3 (6×9)-3

2. Make a new table. Write in some different target numbers and try again.

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting		<ul><li>13 Big Match</li><li>18 Summary</li><li>27 Choosy</li></ul>	<ul><li>10 Trios</li><li>12 Keep Your Balance</li><li>14 Card Tricks</li></ul>	<ul><li>6 Shape Search</li><li>10 Stroking Cats</li><li>15 Hunt the Numbers</li></ul>	
More		3 Boxer 8 Dice Superstars	29 Asking Questions	<b>10</b> Mystery People	<ul> <li>15 Dice Lines</li> <li>20 Equation Solving</li> <li>28 Arch Numbers</li> <li>31 Target Practice</li> </ul>
Go Further With		8 A Mouthful 33 Challenge 38 Switch	<ul><li>16 Number Nine</li><li>21 Equations</li><li>33 Signs</li></ul>	<ul><li>7 Number Tricks</li><li>10 Think of a Number</li><li>14 Whodunnit?</li></ul>	<ul><li>6 Countdown</li><li>7 Mixed Equations</li><li>15 A Special Date</li></ul>

### **Three Stones**





1. Write in as many expressions for the target numbers in the table as you can.

Target number	Expression	Target number	Expression
13	®uss (2 x 4) +5	18	@02 6+12
8		24	
14		19	
6		23	
25		44	
10		28	
72		51	

2. Make a new table. Write in some different target numbers and try again.



### Number Puzzles

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•	٠			
4	•	•			
5	•	•			
6			Ì		

• Learning and using addition and subtraction facts.

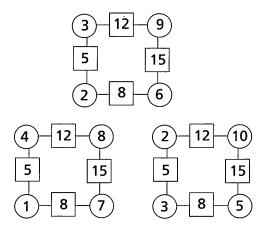
• Using 'trial and improvement' methods.

#### SKILLS

Adding and subtracting

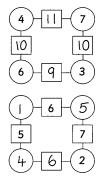
#### NOTES

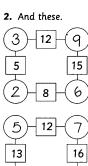
The first three are straightforward. The next three can be solved by working round the puzzle from one corner. The second group can be approached by trial and error. In some of these cases, more than one solution is possible. For example, the first one in this group:



If you add two numbers in **circles**, you get the number between them, in a **square**.

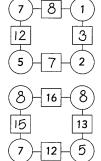
1. Complete the gaps in these.

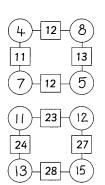


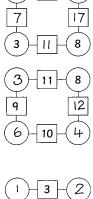


17

8







13

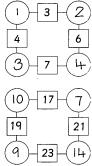
4 3

(5)-7-(2)

5

1

6



3. Look at any one of the second set of puzzles. Can you find a different solution to the same puzzle?

9

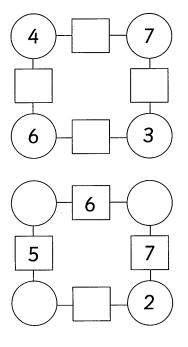
	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More					24 Triangle Sums
Go Further With					34 Multiplication Triangles

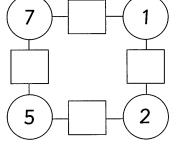
### **Number Puzzles**

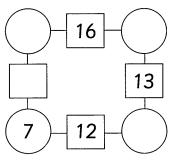


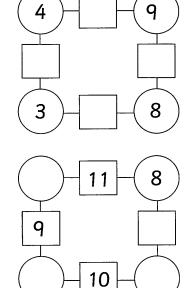
If you add two numbers in **circles**, you get the number between them, in a **square**.  $\begin{array}{c}
1 - 4 - 3 \\
6 5 \\
5 - 7 - 2
\end{array}$ 

1. Complete the gaps in these.

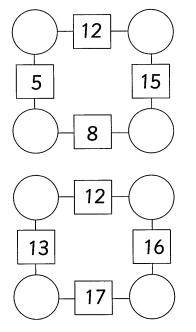


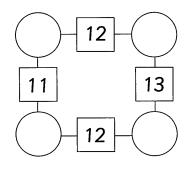


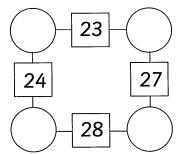




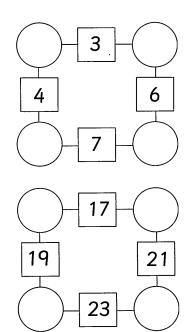
#### 2. And these.







**3.** Look at any one of the second set of puzzles. Can you find a different solution to the same puzzle?





# **A Special Date**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•				
4	•				
5	•	•			
6				-	

- Addition, subtraction, multiplication and division.
- Simple equations.

### SKILLS

 Creating expressions for different numbers using a set of digits and a choice of operation signs

#### APPARATUS

Special Paper 1 for the extension

#### EXTENSION

 Continue the activity using Special Paper 1.



1. Choose a date when something special happened, (not your birthdate). Suppose you choose: 23. 3. 93

Keeping the date digits in order and using signs, see how many different numbers you can make.

For example: 2 + 3 + 3 + 9 + 3 = 20 2 + 3 + 3 + 9 - 3 = 14 23 - 3 - 9 - 3 = 8 23 + 3 - 9 + 3 = 20

 Colour each number on this hundred square that you can make from your date. Write down how you made it. See how many of the numbers you can colour.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

3. Try again using your birthdate.

\*

G U S T 3 4 5 6 7 10 11 12 13 14 17 18 19 20 21 24 25 26 27 28



	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting		<ul><li>13 Big Match</li><li>18 Summary</li><li>27 Choosy</li></ul>	<ol> <li>10 Trios</li> <li>12 Keep Your Balance</li> <li>14 Card Tricks</li> </ol>	<ul><li>6 Shape Search</li><li>10 Stroking Cats</li><li>15 Hunt the Numbers</li></ul>	
More		3 Boxer 8 Dice Superstars	29 Asking Questions	10 Mystery People	<ol> <li>Dice Lines</li> <li>Equation Solving</li> <li>Arch Numbers</li> <li>Target Practice</li> </ol>
Go Further With		<ul><li>8 A Mouthful</li><li>33 Challenge</li><li>38 Switch</li></ul>	<ul><li>16 Number Nine</li><li>21 Equations</li><li>33 Signs</li></ul>	<ul><li>7 Number Tricks</li><li>10 Think of a Number</li><li>14 Whodunnit?</li></ul>	<ul><li>6 Countdown</li><li>7 Mixed Equations</li><li>13 Three Stones</li></ul>

# **A Special Date**



 Choose a date when something special happened, (not your birthdate). Suppose you choose: 23. 3. 93

Keeping the date digits in order and using signs, see how many different numbers you can make.

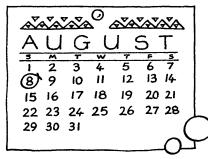
For example: 2 + 3 + 3 + 9 + 3 = 202 + 3 + 3 + 9 - 3 = 1423 - 3 - 9 - 3 = 823 + 3 - 9 + 3 = 20

2. Colour each number on this hundred square that you can make from your date. Write down how you made it. See how many of the numbers you can colour.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



3. Try again using your birthdate.





# **Multiplying Grids**

LEVEL	UA	N	SSM	HD	A
1					
2					
3					
4	•				
5	•				
6					

 Learning multiplication facts up to 10 × 10 and using them in multiplication and division problems.

### SKILLS

- Multiplying by single-digit numbers
- Dividing by single-digit numbers

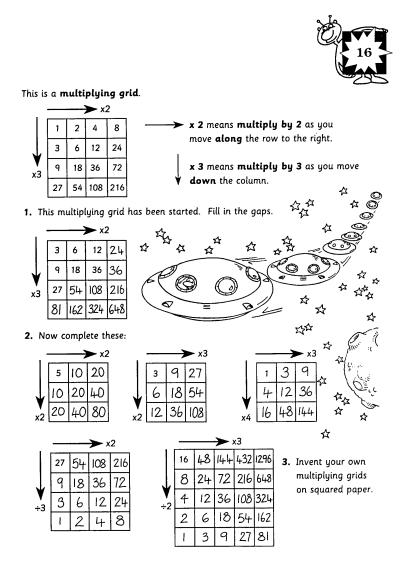
### APPARATUS

Squared paper

### NOTES

Children creating their own multiplying grids, using multiplication in both directions, will find the numbers in the grids soon become large. It is easiest to start with very small numbers.

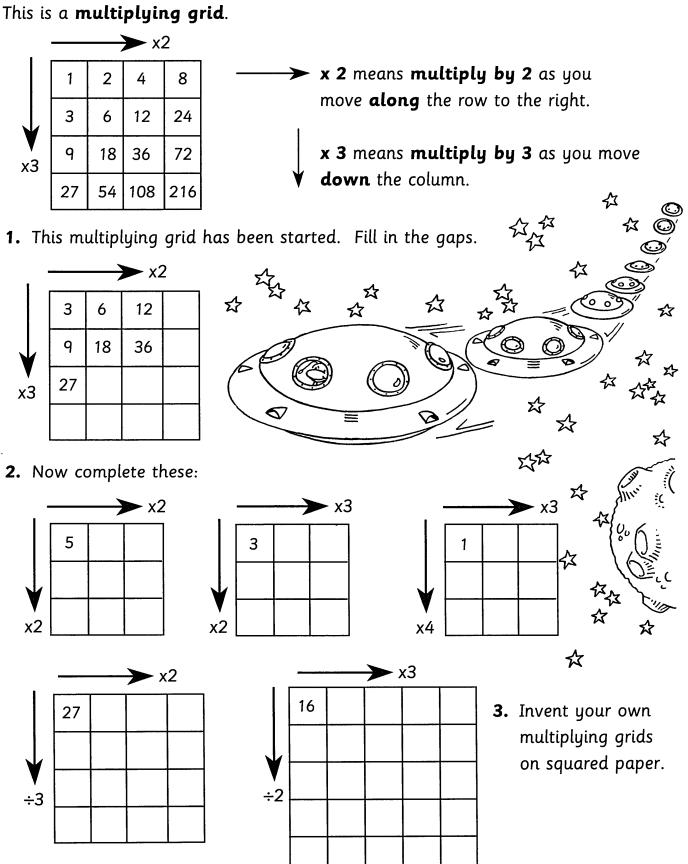
When using division, the top corner number has to be carefully selected so that it can be divided repeatedly by the same number.



	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting					21 Grids
More					13 Arrow Grids

# **Multiplying Grids**







# Minus A Digit

LEVEL	UA	Ν	SSM	HD	A
1					
2		٠			
3	•				
4	•	•			
5	•				
6					

Subtracting two-digit numbers.
 Collecting data to produce a frequency table.

#### SKILLS

Subtracting two-digit numbers

### NOTE

Children can find out which digit is most often missing by making a frequency table like this:

Digit | 1 2 3 4 5 6 7 8 9

Frequency

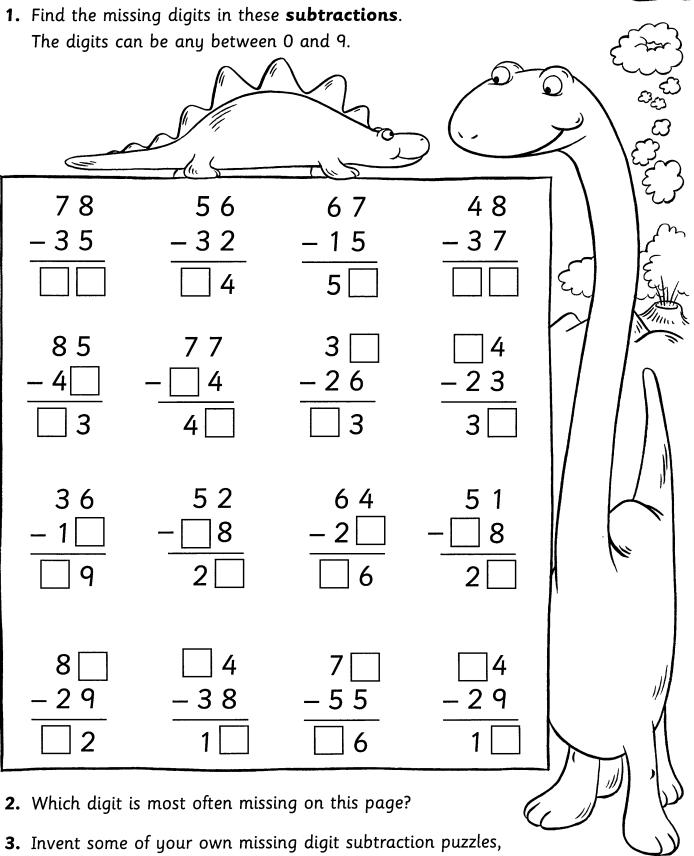
	ing digits in these n be any between			
78 -35 43	5 6 - 3 2 2 4	67 -15 52	48 -37	
85 -42 43	77 - <u>34</u> 43	3 9 - 2 6 1 3	54 -23 31	
36 -17 19	52 -28 24	64 -28 36	51 -28 23	
8] -29 52	5 4 - 3 8 1 6	7 [] - 5 5 [] 6	ー29 15	
<b>3.</b> Invent some o	s most often missi of your own missi and to do them.		Ý	

Question 2: 1 is most often missing.

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting			17 Totals		
More			25 4-Card Fun		7 What's Missing? 22 Nearly 60 36 Differences
Go Further With					<ul> <li>8 Nearly 20</li> <li>9 5-Card Sums</li> <li>27 Subtraction Guessing</li> <li>35 Mixed Totals</li> </ul>

# Minus A Digit





and get a friend to do them.



### **Factor Grids**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•				
4		•			
5	•				
6					

- Learning multiplication facts up to  $10 \times 10$  and using them in multiplication and division problems.
- Generalising, mainly in words, patterns, eg, 'factor'.

### SKILLS

- Finding factors
- Multiplying by single-digit numbers

### NOTES

Children will need to understand what is meant by a 'prime number'.

The activity can lead to exploration of numbers which have many factors. i.e. the numbers which appear in the bottom right-hand corner. So, for example, the factors of 36 are: 1, 2, 3, 4, 6, 9, 12, 18, 36 (36 has nine factors altogether.)

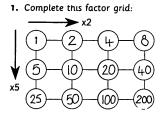
The size of the grid determines the number of factors for the number in the bottom right-hand corner.

This is a factor grid. You can use it to find, for example, the factors of 18: 1, 2, 3, 6, 9, 18.



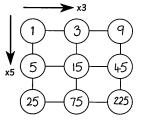
or the factors of 12: 1, 2, 3, 4, 6, 12.

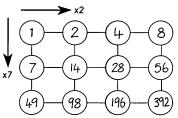




2. Now write the: factors of 20 1,2,4,5,10,20 factors of 50 1.2.5.10, 25, 50 / factors of 40 1,2,4,8,5,10,20,40 factors of 100 1.2, 4, 5, 10, 20, 25, 50, 100

3. Complete these and write some lists of factors.

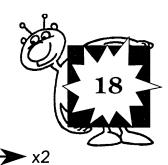




4. Make some more factor grids. You can make them by multiplying numbers in the grid by any pair of prime numbers (2, 3, 5, 7, 11, 13 and so on).

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More		37 Snake Bite 38 Divido	<ul><li>6 Table Patterns</li><li>7 Pick Your Cards</li><li>8 Table Ends</li></ul>	<ul> <li>8 Completing Rectangles</li> <li>12 Sift the Multiples</li> <li>13 Table Patterns</li> </ul>	16 Factor Pairs 26 Cloud Numbers
Go Further With		<ol> <li>Race Track</li> <li>Factor</li> <li>Multiple Choice</li> </ol>	9 Factors 13 Tables	<ol> <li>Prime Numbers</li> <li>Factor Graph</li> <li>Multiplication Machines</li> </ol>	<ol> <li>Lowest Common Multiples</li> <li>Factor Show</li> <li>Highest Common Factors</li> </ol>

### **Factor Grids**



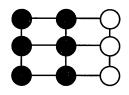
4

12

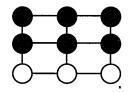
36

This is a **factor grid**.

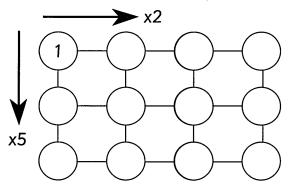
You can use it to find, for example, the factors of 18: 1, 2, 3, 6, 9, 18.



or the factors of **12**: 1, 2, 3, 4, 6, 12.



1. Complete this factor grid:



2.	Now write the:	
	factors of <b>20</b>	
	factors of <b>50</b>	
	factors of <b>40</b>	
	factors of <b>100</b>	

2

6

18

1

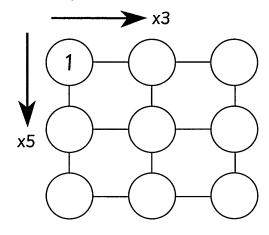
3

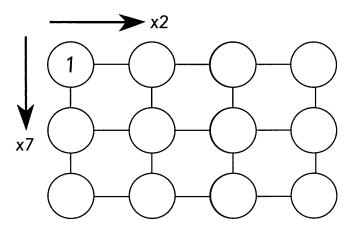
9

.1

xЗ

3. Complete these and write some lists of factors.





4. Make some more factor grids. You can make them by multiplying numbers in the grid by any pair of **prime numbers** (2, 3, 5, 7, 11, 13 and so on).



# **Remainder Charts**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	0	•			
4	•	٠			
5	•				
6					

- Understanding remainders.
- Dividing two-digit numbers by single-digit numbers.

#### SKILLS

- Dividing by single-digit numbers
- Finding remainders
- Multiplying by single-digit numbers

#### NOTE

Discuss what it means when '0' appears in a chart.

### EXTENSION

If the 16 remainder chart is extended, for example, from 2 to 16, then all possible remainders can be analysed. This can lead to discussion about which numbers could not appear in this chart and why.

									• ]	۵	
									Ċ	) N	
											19 >
Here is the i	remai	nder c	hart	for 28.	$\sqrt{2}$					2	35
				/		<u>•</u> /					
Divide ł	by [	2	3	4	5	6	7	8	٩	10	
Remain	der	0	l	0	3	4	0	4	I	8	
When 28 a remain	der of	3. Wi	rite it	here	Ĵ	a ren	nainde	divided r of 4.	Write		1
<ol> <li>Divide 28 Write ab</li> </ol>	-				•				τ.		
2. Now con	nplete	these r	emain	der cha	arts:						
				$\square$	24						
Divide by	2	3	4	5	6	7	8	9	10	· ]	
Remainder	0	0	Ō	4	0	3	Ó	6	4		
				$\square$	16						
Divide by	2	3	4	5	6	7	8	9	10	2	
Remainder	0		0		4	. 2	0	7	6		
					35 -						
Divide by	2	3	4	5	6	7	8	9	10	2	
Remainder	1	2	3	0	5	С	3	8	5		
<ol> <li>Make the numbers</li> </ol>		-		how re	mainde	rs if yc	u are c	lividing	by		

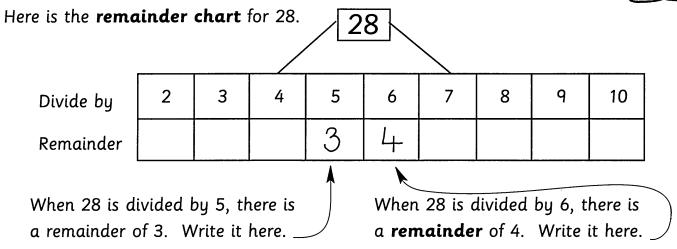
4. Invent some remainder charts of your own.

Question 1: Children should notice that, when a number is divided by one of its factors, the remainder is 0.

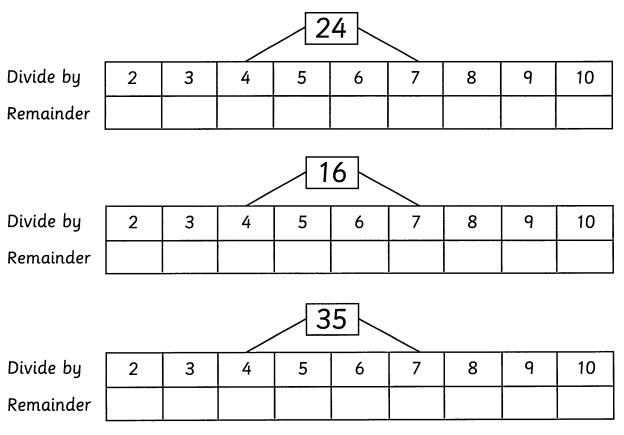
	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Go Further With		<ol> <li>Remainders</li> <li>Sixes</li> <li>Sevens</li> <li>Divide It</li> <li>Left Overs</li> </ol>	<ul><li>9 Factors</li><li>25 Divisions</li><li>40 Remainders</li></ul>	19 Remainder Tables	

# **Remainder Charts**





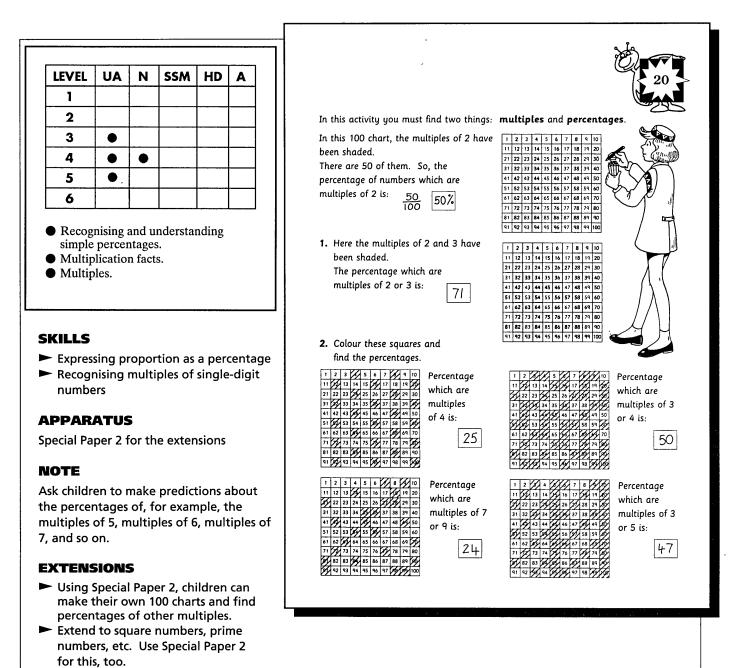
- Divide 28 by other numbers, and complete the remainder chart. Write about anything you notice. (Hint: think about factors.)
- 2. Now complete these remainder charts:



- **3.** Make the charts longer to show remainders if you are dividing by numbers greater than 10.
- 4. Invent some remainder charts of your own.



### **Multiple Percentages**



	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More			6 Table Patterns 8 Table Ends	<ol> <li>6 Multiple Gaps</li> <li>12 Sift the Multiples</li> <li>18 Patterns With 9</li> </ol>	<ul><li>16 Factor Pairs</li><li>26 Cloud Numbers</li><li>33 The Right Boxes</li></ul>
Go Further With	<ul><li>26 Sevens</li><li>36 Multiplication Tables</li></ul>	<ul><li>17 Fives and Threes</li><li>24 Multiple Choice</li></ul>	13 Tables 37 Multiples	17 Factor Graph	20 Goal Percentage 33 Tridiscs 36 Percentage Wheels

# **Multiple Percentages**

In this activity you must find two things: **multiples** and **percentages**.

In this 100 chart, the multiples of 2 have been shaded.

There are 50 of them. So, the percentage of numbers which are

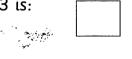
multiples of 2 is:

50%

1. Here the multiples of 2 and 3 have been shaded.

The percentage which are

multiples of 2 or 3 is:



### 2. Colour these squares and find the percentages.

_									
1	2	3	4	5	6	7	8	٩	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Percentage which are multiples of 4 is:



Percentage which are multiples of 7 or 9 is:



				÷-					
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

which are multiples of 3 or 4 is:

Percentage



Percentage which are multiples of 3 or 5 is:



	10	9	8	7	6	5	4	3	2	1
	20	19	18	17	16	15	14	13	12	11
4	30	29	28	27	26	25	24	23	22	21
	40	39	38	37	36	35	34	33	32	31
6	50	49	48	47	46	45	44	43	42	41
	60	59	58	57	56	55	54	53	52	51
	70	69	68	67	66	65	64	63	62	61
	80	79	.78	77	76	75	74	73	72	71
	90	89	88	87	86	85	84	83	82	81
	100	99	98	97	96	95	94	93	92	91
3	1	T	T	1	T	1	1	1	1	

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100





# **Division Grids**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•	•			
4	•				
5	•				
6					

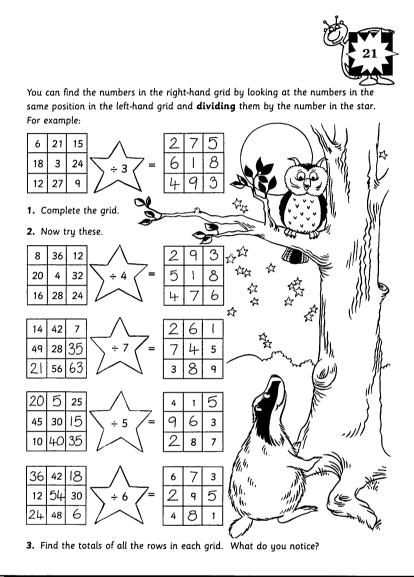
- Dividing two-digit numbers by single-digit numbers.
  Recognising that multiplication and
- Recognising that multiplication and division are inverse operations.

#### SKILLS

- Dividing two-digit numbers by singledigit numbers
- Multiplying as the inverse of dividing
- Adding two-digit numbers

### NOTE

In order to complete question 2, children may need some help in understanding that multiplication and division are inverse operations.



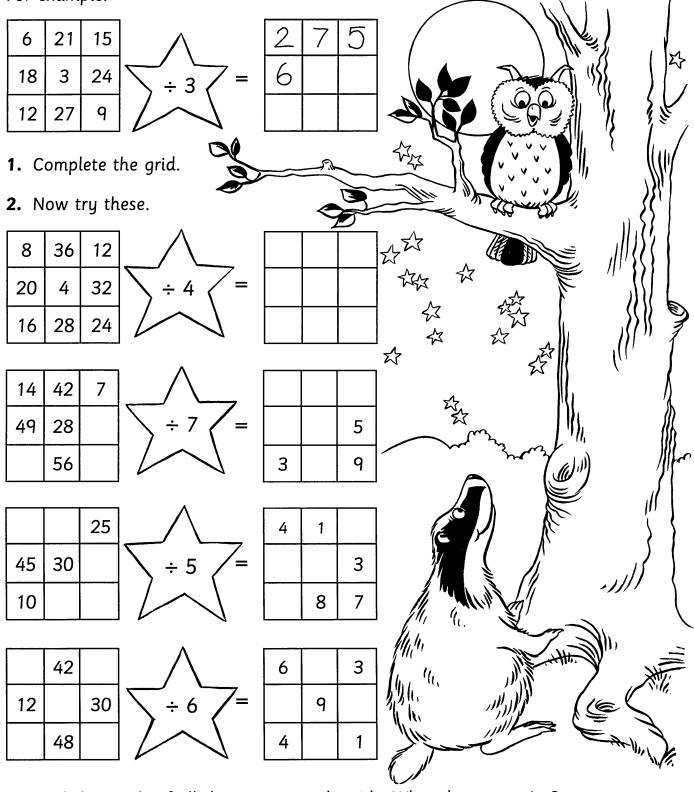
3. The row totals of the left-hand grids, when divided, give the row totals of the right-hand grids.

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting					<b>11</b> Addition Wheels
More		38 Divido			21 Multiplication Wheels
Go Further With		10 Sixes 27 Sevens 28 Divide It	<ul><li>9 Factors</li><li>25 Divisions</li><li>40 Remainders</li></ul>	19 Remainder Tables	24 Division Wheels

# **Division Grids**



You can find the numbers in the right-hand grid by looking at the numbers in the same position in the left-hand grid and **dividing** them by the number in the star. For example:



3. Find the totals of all the rows in each grid. What do you notice?



### **Place Nine**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•	•			
4	•	٠			
5			İ		
6			1		

subtraction facts.
Adding several single-digit numbers.

### SKILLS

- Adding and subtracting
- Seeking arrangements of numbers in a two-way table to match given totals

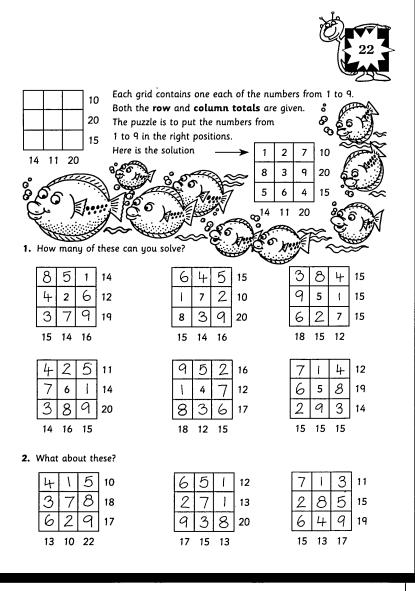
### APPARATUS

Numbered cards, 1-9

### NOTES

Ask children to draw a large 3 x 3 grid on paper, and use a set of numbered cards to place in the grid.

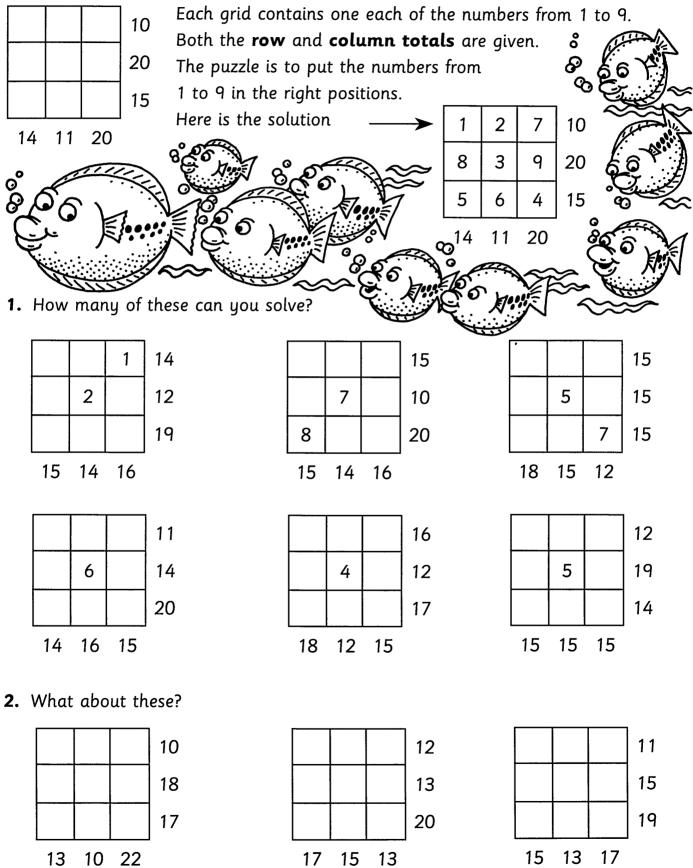
They can also make labels to represent the row and column totals, and place these in position for each puzzle. The task can be made easier by giving children an extra clue (number in a square).



	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More		26 Fifteens			<ul> <li>18 2 x 2 Addition Squares</li> <li>25 Addition Grids</li> <li>26 Cloud Numbers</li> </ul>
Go Further With					2 Magic Squares

# **Place Nine**







# **Multiples of 10**

LEVEL	UA	Ν	SSM	HD	A
1					
2		•			
3	•	•			
4	•	•			
5	•				
6			1		

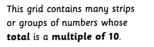
- Addition patterns.
- Number patterns.
- Addition of two-digit numbers.

#### SKILLS

 Adding sets of numbers to find totals which are multiples of 10

#### NOTES

Ask the children to look for the sums of units digits which produce multiples of 10. For example, 1 and 9, 2 and 8, 3 and 7, 5 and 5.



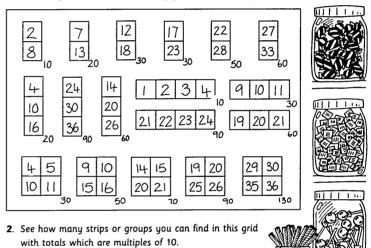
For example, this strip has a total of 30, which is a multiple of 10.





1. These are the outlines of strips or groups which have numbers whose total is a multiple of 10. See how many you can find. They are all different.

30



1	2	3	4	5	6	7	8	٩	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30



	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting			35 In the Window		4 Giraffe 12 Difference Dog 31 Elephant Tricks
More				<b>19</b> Unit Digit Patterns	19 Twenties
Go Further With					26 Hexanimals

# **Multiples of 10**

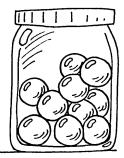


This grid contains many strips or groups of numbers whose **total** is a **multiple of 10**.

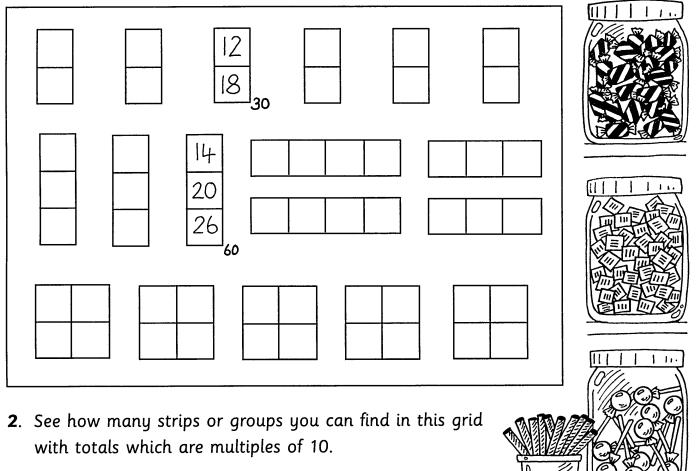
For example, this strip has a total of 30, which is a multiple of 10.

	12	
	18	
1		30

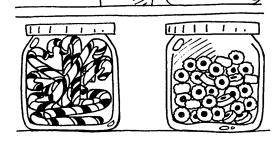
1	2	3	4	5	6
7	8	9	10	11	12
13	14	15	16	17	18
19	20	21	22	23	24
25	26	27	28	29	30
31	32	33	34	35	36



1. These are the outlines of strips or groups which have numbers whose total is a multiple of 10. See how many you can find. They are all different.



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30





# **Division Wheels**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•				
4	٠	•			
5	•				
6					

- Dividing two-digit numbers by a single-digit number.
- Recognising that multiplication and division are inverse operations and using this to check calculations.

### SKILLS

- Dividing two-digit numbers by singledigit numbers
- Using multiplication as the inverse of division

#### **APPARATUS**

Special Paper 3 for the extension activity

#### NOTE

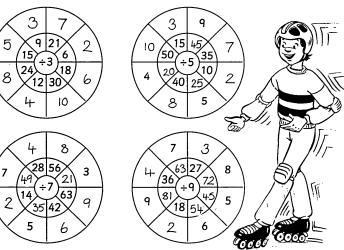
The table is given as a check. In the first instance, children should be encouraged to try completing the wheels without reference to it.

#### **EXTENSIONS**

- Children can build their own division wheels, using Special Paper 3.
- They could take the activity further to include division by numbers greater than 10.

#### **SPECTRUM LINKS**

									Ø	<u>لو</u>	
This part of the table shows these <b>division facts</b>	x	1	2	3	4	5	6	7	8	9	10
$24 \div 6 = 4$	F	1	2	3	4	5	6	7	8	9	10
24 ÷ 4 = 6	2	2	4	6	8	10	12	14	16	18	20
1. Write down some more	3	3	6	∕q∕	12	15	18	21	24	27	30
division facts for dividing by	4	4	8	12	16	20	24	28	32	36	40
8, and then for dividing by 6.	5	5	10	15	20	25	30	35	40	45	50
	6	6	12	18	24	30	36	42	48	54	60
<ol> <li>Complete these division wheels.</li> <li>The first one has been started for you,</li> </ol>	7	7	14	21	28	35	42	49	56	63	70
to show you how it works.	8	8	16	24	32	40	48	56	64	72	80
Use the table to check your answers.	9	9	18	27	36	45	54	63	72	81	90
	10	10	20	30	40	50	60	70	80	90	100



3. Build your own division wheels using these divisions:  $\div$  2,  $\div$  4,  $\div$  6,  $\div$  10

	Data Handling		Games Investigations		Number Skills		
Starting					<b>11</b> Addition Wheels		
More		38 Divido			21 Multiplication Wheels		
Go Further With		10 Sixes 27 Sevens 28 Divide It	9 Factors 25 Divisions 40 Remainders	19 Remainder Tables	21 Division Grids		

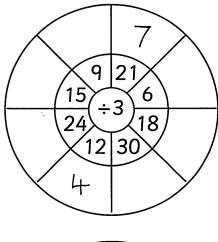
# **Division Wheels**

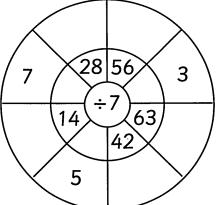


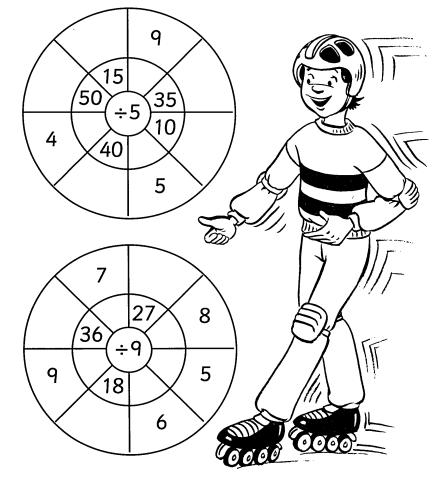
This part of the table shows these **division facts**:  $24 \div 6 = 4$  $24 \div 4 = 6$ 

- Write down some more division facts for dividing by 8, and then for dividing by 6.
- Complete these division wheels.
   The first one has been started for you, to show you how it works.
   Use the table to check your answers.

x	1	2	3	4	5	6	7	8	9	10
$\neq$	1	2	3	4	5	6	7	8	9	10
2	2	4	6	8	10	12	14	16	18	20
3	3	6	لم	12	15	18	21	24	27	30
4	4	8	12	16	20	<b>°</b> 24	28	32	36	40
5	5	10	15	20	25	30	35	40	45	50
6	6	12	18	24	30	36	42	48	54	60
7	7	14	21	28	35	42	49	56	63	70
8	8	16	24	32	40	48	56	64	72	80
9	9	18	27	36	45	54	63	72	81	90
10	10	20	30	40	50	60	70	80	90	100



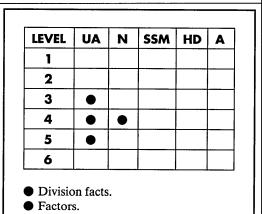




**3.** Build your own division wheels using these divisions:  $\div 2, \div 4, \div 6, \div 10$ 



# **Highest Common Factors**



### SKILLS

- Listing the factors of a number
- Finding the highest common factor of two numbers

#### NOTE

The sheet is best preceded by an activity which involves searching for factors. For example: 18: 'Factor Grids' or 12: 'Factor Show' On this grid you can show the highest common factors of pairs of numbers. For example: factors of 12 are: 1, 2, 3, 4, 6, 12 factors of 20 are: 1, 2, 4, 5, 10, 20

**Common** factors of 12 and 20 are: 1, 2, 4 (that means they are factors of both numbers).

The **highest common factor** of 12 and 20 is: 4

 Complete the grid by finding the highest common factors of the other pairs of numbers.

2. Now complete these grids.

	24	16	10
12	12	4-	2
15	3	1	5
8	ව	8	2

			-))
	30	٩	32
40	10	1	8
6	6	3	2
18	6	9	2

	30	20	16	36
48	6	4	16	12
10	10	10	2	2
50	10	10	2	2

	32	8	28	14
12	4	4	4	2
18	2	2	2	2
42	2	2	14	7

12

6

4

4

6

20

16

15

3

5

ł

8

2

4

8

3. Draw your own grids, and invent your own numbers for finding the highest common factors.

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More		37 Snake Bite 38 Divido	<ol> <li>6 Table Patterns</li> <li>7 Pick Your Cards</li> <li>8 Table Ends</li> </ol>	<ul> <li>8 Completing Rectangles</li> <li>12 Sift the Multiples</li> <li>13 Table Patterns</li> </ul>	16 Factor Pairs 26 Cloud Numbers
Go Further With		<ol> <li>Race Track</li> <li>Factor</li> <li>Multiple Choice</li> </ol>	9 Factors 13 Tables	<ol> <li>Prime Numbers</li> <li>Factor Graph</li> <li>Multiplication Machines</li> </ol>	<ol> <li>Lowest Common Multiples</li> <li>Factor Show</li> <li>Factor Grids</li> </ol>

# **Highest Common Factors**

On this grid you can show the highest common factors of pairs of numbers. For example: factors of 12 are: 1, 2, 3, 4, 6, 12 factors of 20 are: 1, 2, 4, 5, 10, 20

**Common** factors of 12 and 20 are: 1, 2, 4 (that means they are factors of both numbers).

The highest common factor of 12 and 20 is: 4

- 1. Complete the grid by finding the highest common factors of the other pairs of numbers.
- **2.** Now complete these grids.

	24	16	10
12			
15			
8			

	30	20	16	36
48				
10				
50				

	32	8	28	14
12				

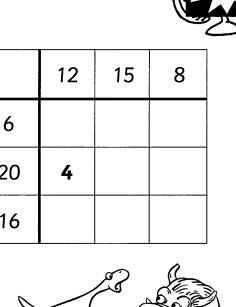


18

3. Draw your own grids, and invent your own numbers for finding the highest common factors.

	12	15	8
6			
20	4		
16			

			-))
	30	9	32
40			
6			
18			





### Hexanimals

LEVEL	UA	N	SSM	HD	A
1					
2					
3	۲	•			
4	•	•			
5	•				
6					

- Learning and using addition and subtraction facts to 20.
- Adding mentally several single-digit numbers.

### SKILLS

 Finding sets of several numbers which have a given total

### APPARATUS

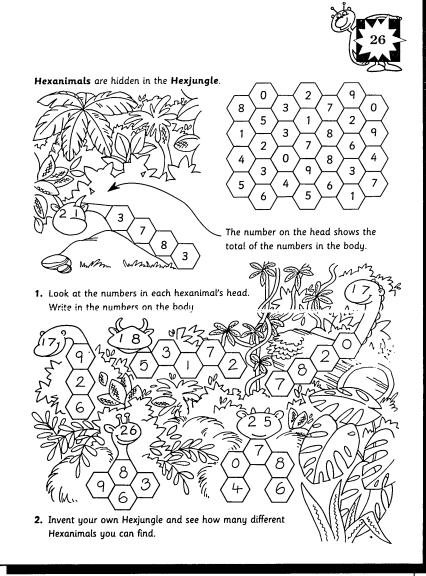
Special Paper 4, for the initial work and the extension

### NOTE

Children can use Special Paper 4 to create their own jungle and to record Hexanimals.

#### EXTENSION

Explore different Hexanimals on this grid. For example, start with a total of 10, then 11, then 12, and so on, each time inviting children to find a Hexanimal.

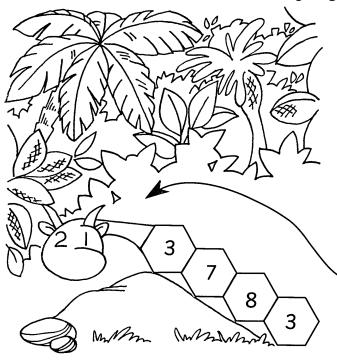


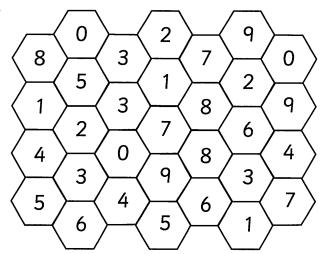
	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting			35 In the Window		4 Giraffe 12 Difference Dog 31 Elephant Tricks
More				<b>19</b> Unit Digit Patterns	19 Twenties
Go Further With					23 Multiples of Ten

# Hexanimals



### Hexanimals are hidden in the Hexjungle.





The number on the head shows the total of the numbers in the body.

Look at the numbers in each hexanimal's head.
 Write in the numbers on the body.

8

Invent your own Hexjungle and see how many different Hexanimals you can find.

61

00

0h

13

5

2



## **Subtraction Guessing**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•	•			
4	•	•			
5	•				
6					

- Approximating to the nearest 10.
- Subtracting two two-digit numbers.
- Estimating and approximating to check the validity of subtraction calculations.

### SKILLS

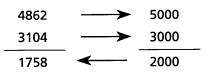
- Approximating results of subtracting
- Rounding numbers to the nearest 10
- Using a calculator as a check

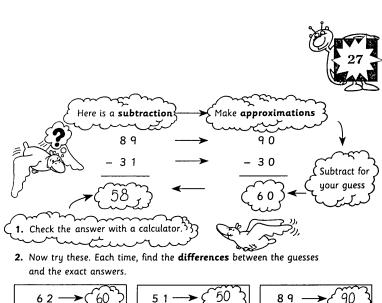
### APPARATUS

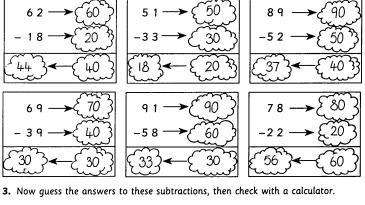
Calculator

### EXTENSION

This activity can be extended to much larger numbers which, for example, are rounded off to the nearest 100, e.g.

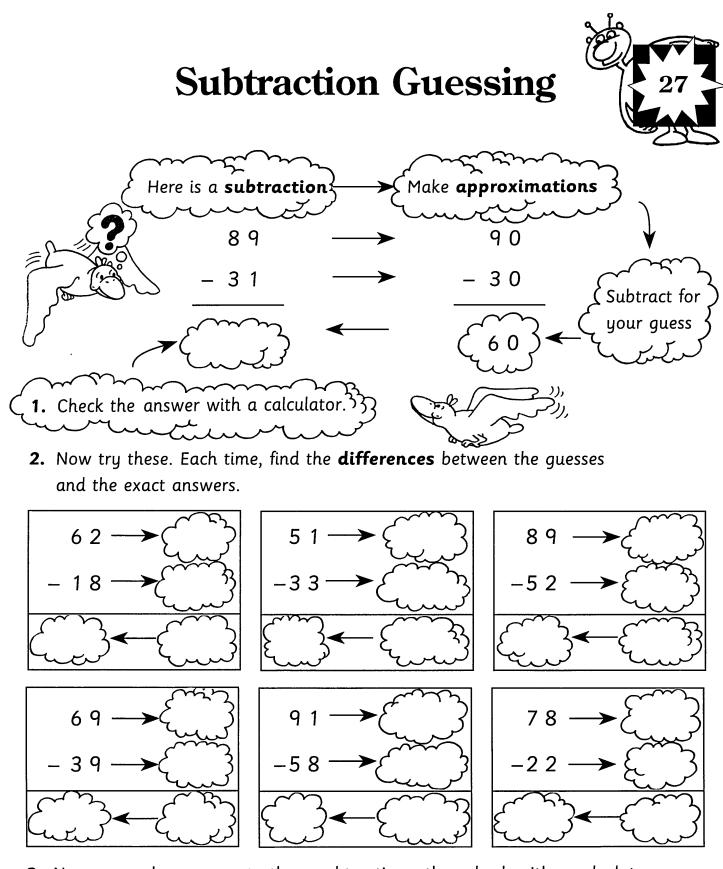






87	128	131	109	204	211
- 7 1	- 62	- 79		- 119	- 87

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More					22 Nearly 60 36 Differences 40 Which Truck?
Go Further With					17 Minus a digit



**3.** Now guess the answers to these subtractions, then check with a calculator.

87	128	131	109	204	211
_ 7 1	- 62	- 79	- 43	- 119	- 87



### **Goal Percentages**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•	•			
4	•				
5	•	•			
6					

- Recognising and understanding simple percentages.
- Calculating percentages.
- Extracting information from tables and lists.

### SKILLS

- Expressing proportions of 100, 50 and 25 as a percentage
- Finding percentages of a quantity
- Processing discrete data

#### **EXTENSIONS**

- ► Find percentages when the sets of scores do not total 100, 50 or 25.
- Sunday newspapers provide a range of data, and the percentages can be found using a calculator.

Here	is a list	of sco	res for S	50 foot	ball ma	tches.					25
НА	на	на	на	на	НА	на	на	Н А 0-2	НА	на	на
0 - 1	0 - 1	1 - 0	1 - 1	4 - 3	5 - 1	2 - 0	1 - 2	0 - 2	0 - 2	1 - 0	0 - 3
1 - 2	0-0	3 - 1	6 - 1 1 - 0 1 - 2	0 - 1	0 - 1	4 - 3	1 - 0	1 - 0	3 - 4	1 - 1	2-0
2 - 0	1 - 2	0 - 0	1-0	0 - 3	1 - 0	3 - 0	0 - 3	2 - 0	1-0	0 - 1	0 - 1
1 - 2	2 - 2	1 - 2	1 - 2	1 - 0	1 - 1	5 - 0	1 - 1	1 - 1	0 - 2	1 - 0	1-0
1 - 3	1 - 0							l			
			three sc		2	-1- :-	20/				
50 th	e perce	ntage c	of team:	s scortr	ig 4 go	ais is:	5%				
<b>1.</b> Fi	nd thes	e perce	ntages:								
Team	s scorin	ig 0 go	als 33	5%	Tea	ims sco	ring 2	or more	e goals	307	
Team	s scorin	ig 1 go	al 3	7%	Ma	tches e	nding i	n a dra	w	16%	]
Team	s scorin	ig 2 go	als 15	%	Ma	tches e	nding i	n a hor	ne win		
Team	s scorin	ig 3 go	als 9	%	Ma	tches e	nding i	n an av	vay wi	n [40%	,
Here	is a list	of the	scores	in 25 h	ockey r	natche	5:				
ΗA	ĮН	AII	H A	НА	ιн	ALH	A	H A	і н	A	
1 - 0	3	1	2 - 0	1 1	0 -	0 1	- 4	50	2 -	1	
2 - 0	3 -	3	1 1	4 - 1	2 -	3   1	1	2 - 1	1 -	2	
0 - 1	3	1	H A 2 - 0 1 1 1 - 0	1 - 1	2 -	1   1	- 6	4 - 4			
4 - 2	2 -	4									
<b>2.</b> Fi	nd thes	e perce	ntages:								
Te	ams sc	oring O	goals	16%		Team	s scorir	ng 2 or	more g	joals	44%
Te	ams sc	oring 1	goal	40%		Match	nes end	ling in d	a draw		28%
Te	ams sc	oring 2	goals	18%		Match	nes end	ling in d	1 home	win	48%
Te	ams sc	oring 3	goals	10%		Match	ies end	ling in d	in awa	y win	24%

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More	18 Arsenal v Liverpool				
Go Further With					20 Multiple Percentages 33 Tridiscs 36 Percentage Wheels

### **Goal Percentages**



Here is a list of scores for 50 football matches.

					НА						
0 - 1	0 - 1	1 - 0	1 - 1	4 - 3	5 - 1 0 - 1	2 - 0	1 - 2	0 - 2	0 - 2	1 - 0	0 - 3
1 - 2	0 - 0	3 - 1	6 - 1	0 - 1	0 - 1	4 - 3	1 - 0	1 - 0	3 - 4	1 - 1	2 - 0
2 - 0	1 - 2	0 - 0	1 - 0	0 - 3	1 - 0	3 - 0	0 - 3	2 - 0	1 - 0	0 - 1	0 - 1
1 - 2	2 - 2	1 - 2	1 - 2	1 - 0	1 - 0 1 - 1	5 - 0	1 - 1	1 - 1	0 - 2	1 - 0	1 - 0
1 - 3	1 - 0										
	•					•	•		•	•	•

Out of 100 teams, three scored 4 goals. So the percentage of teams scoring 4 goals is: 3%

1. Find these percentages:

Teams scoring 1 goal

Teams scoring 0 goals

- . . .

Teams scoring 2 goals

Teams scoring 3 goals

Teams scoring 2 or more goals Matches ending in a draw Matches ending in a home win Matches ending in an away win

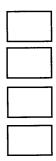
Here is a list of the scores in 25 hockey matches:

ΗA	ΗА	ΗA	НА	ΗA	ΗA	ΗA	ΗA
1 - 0	3 - 1	2 - 0	1 - 1	0 - 0	1 - 4	5 - 0	2 - 1
2 - 0	3 - 3 3 - 1	1 - 1	4 - 1	2 - 3	1 - 1	2 - 1	1 - 2
0 - 1	3 - 1	1 - 0	1 - 1	2 - 1	1 - 6	4 - 4	
4 - 2	2 - 4						

### 2. Find these percentages:



Teams scoring 2 or more goals Matches ending in a draw Matches ending in a home win Matches ending in an away win





### **Consecutive Flowers**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•	•			
4	٠	•			
5	•				
6			1		

• Addition of several numbers.

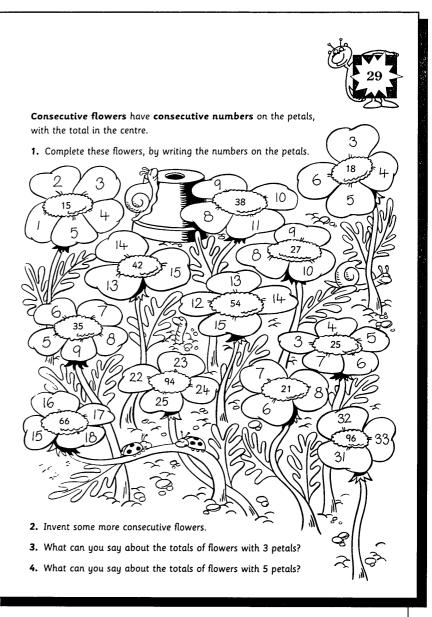
- Number patterns.
- Generalising patterns in numbers.

#### SKILLS

- Finding a set of consecutive whole numbers which have a given total
- Approximating by division

#### NOTE

A useful starting technique is to locate approximate size of the numbers by dividing the centre number by the number of petals.



Question 3: flowers with 3 petals have centre numbers which are multiples of 3.

Question 4: flowers with 5 petals have centre numbers which are multiples of 5.

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting					2 Lucky Number Sweets
More			21 Three in a Row		6 Consecutive Train

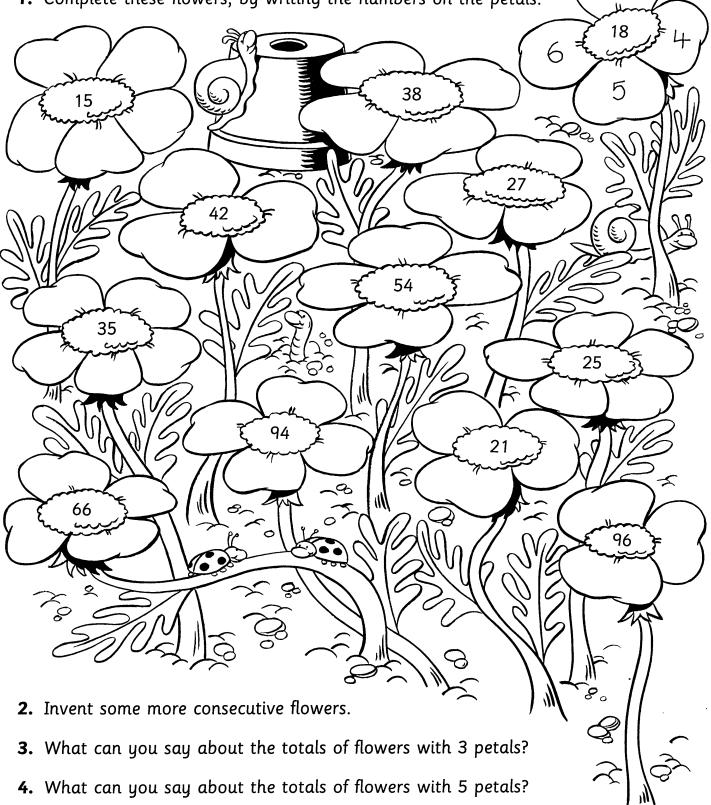
# **Consecutive Flowers**



3

**Consecutive flowers** have **consecutive numbers** on the petals, with the total in the centre.

1. Complete these flowers, by writing the numbers on the petals.





# **Fraction Wheels**

LEVEL	UA	N	SSM	HD	A
1					
2					
3	•	•			
4	•	•			
5	•	٠			
6					

- Recognising and understanding simple fractions.
- Calculating fractions of quantities.

### SKILLS

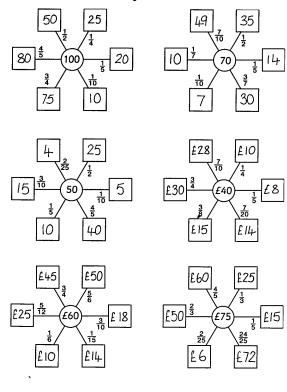
Writing fractions of a quantity

### EXTENSION

A reverse form of this activity is to provide children with all the numbers in the boxes, and invite them to write the appropriate fraction on each arm. 30

The number or amount in the centre of each **fraction wheel** can be divided into fractions. The fractions are written on the spokes of the wheel.

1. Write the **fractions** of the centre numbers in the boxes. Two have been done for you.



2. Invent your own fraction wheels.

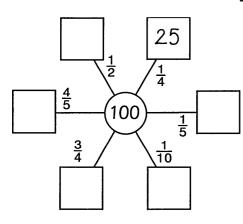
	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting					<b>38</b> Colouring Fractions
More		28 Wheels		14 Equivalent Fractions	8 Fraction Shades
Go Further With					<ul><li>31 Fractions and Decimals</li><li>33 Tridiscs</li></ul>

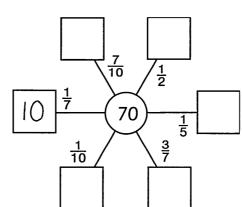
# **Fraction Wheels**

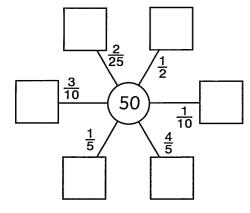


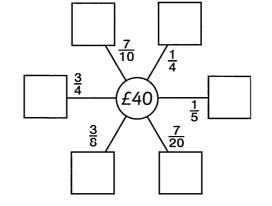
The number or amount in the centre of each **fraction wheel** can be divided into fractions. The fractions are written on the spokes of the wheel.

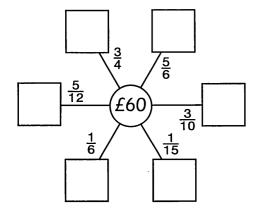
 Write the **fractions** of the centre numbers in the boxes. Two have been done for you.

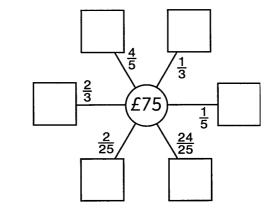








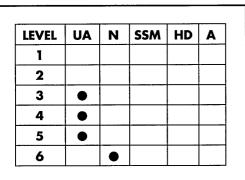




2. Invent your own fraction wheels.



# **Fractions and Decimals**



• Converting fractions to decimals.

#### SKILLS

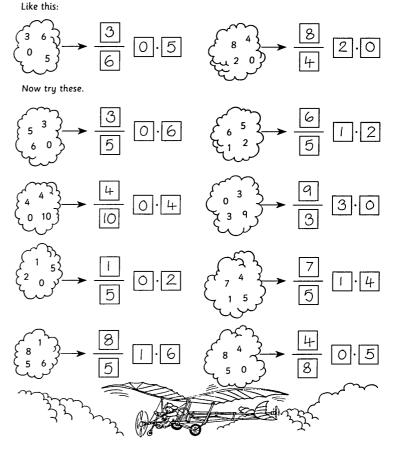
- Equating fractions to decimals
- Creating equivalent fractions and decimals with a given set of digits

#### APPARATUS

Numbered cards, 0-10

#### NOTES

Children could start by drawing a large outline of the boxes on a sheet of paper, then select the relevant numbered cards for each problem. Let them explore arrangements of the cards until they find a correct solution. A calculator can be used to check different arrangements. The numbers in the cloud can be used to make a fraction, and then a decimal, both **equivalent** (equal in size) to each other.

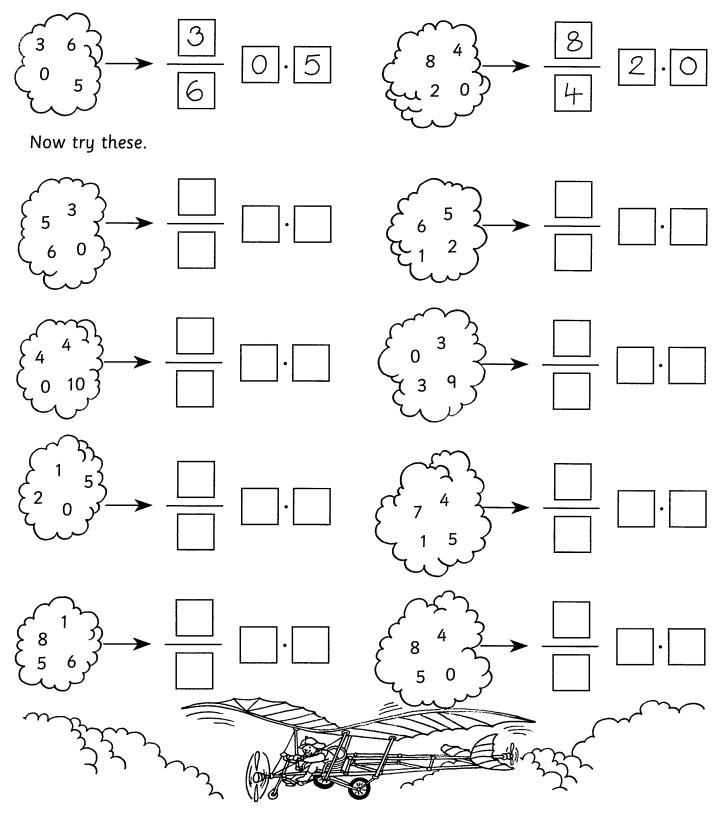


	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting					38 Colouring Fractions
More		28 Wheels		14 Equivalent Fractions	8 Fraction Shades 27 Nearest 100
Go Further With	<ul> <li>9 Inches and Centimetres</li> <li>18 Miles and Kilometres</li> </ul>	12 Decimate 14 Two Places 37 Four Rounds	20 Nearest Wholes		39 Decimal Pyramids

# **Fractions and Decimals**



The numbers in the cloud can be used to make a fraction, and then a decimal, both **equivalent** (equal in size) to each other. Like this:





# **One Hundred**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•	•			
4	•	•			
5	•				
6					

• Addition and subtraction.

### SKILLS

- Adding and subtracting, involving single-digit, two-digit and three-digit numbers
- Combining several operations, searching for an arrangement which gives a particular result

#### NOTE

One strategy to finding a solution is to start with the largest numbers in each line and work down towards the smallest, making adjustments to the use of + and – signs, as you progress. Each line uses the digits 1 to 9, in order to make 100. The missing signs are either + or – .

1. Write the missing signs. One has been done for you.

12 ..... 3 ..... 4 ..... 5 ..... 67 ..... 8 ..... 9 = 100 123 ..... 45 ..... 67 ..... 8 ..... 9 = 100 123 ..... 45 ..... 67 ..... 89 = 100 12 ..... 3 ..... 4 ..... 5 ..... 6 ..... 7 ..... 89 = 100 1 ..... 23 ..... 4 ..... 5 ..... 6 ..... 78 ..... 9 = 100 1 ..... 23 ..... 4 ..... 56 ..... 7 ..... 8 ..... 9 = 100

 Invent some of your own lines, using the digits 1 to 6, and + and - signs, to make different answers. Test them out on a friend, with the signs missing.

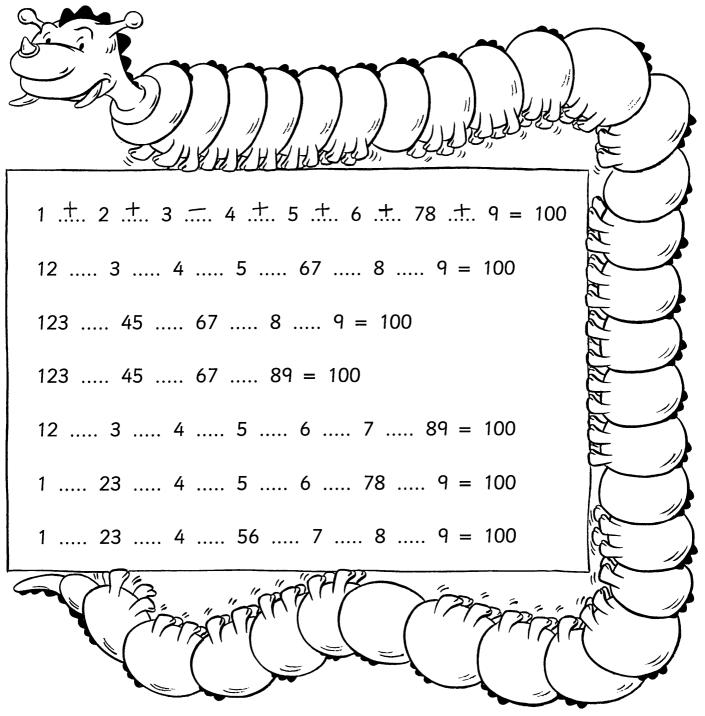
	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting		<ul><li>13 Big Match</li><li>18 Summary</li><li>27 Choosy</li></ul>	<ol> <li>10 Trios</li> <li>12 Keep Your Balance</li> <li>14 Card Tricks</li> </ol>	<ul><li>6 Shape Search</li><li>10 Stroking Cats</li><li>15 Hunt the Numbers</li></ul>	
More		3 Boxer 8 Dice Superstars	29 Asking Questions	10 Mystery People	<ol> <li>Dice Lines</li> <li>Equation Solving</li> <li>Arch Numbers</li> <li>Target Practice</li> </ol>
Go Further With		<ul><li>8 A Mouthful</li><li>33 Challenge</li><li>38 Switch</li></ul>	<ul><li>16 Number Nine</li><li>21 Equations</li><li>33 Signs</li></ul>	<ul><li>7 Number Tricks</li><li>10 Think of a Number</li><li>14 Whodunnit?</li></ul>	<ul><li>6 Countdown</li><li>13 Three Stones</li><li>15 A Special Date</li></ul>

# **One Hundred**



Each line uses the digits 1 to 9, in order to make **100**. The missing signs are either + or -.

1. Write the missing signs. One has been done for you.



 Invent some of your own lines, using the digits 1 to 6, and + and - signs, to make different answers. Test them out on a friend, with the signs missing.



### **Tridiscs**

LEVEL	UA	N	SSM	HD	A
1					
2					
3					
4					
5					
6		•			

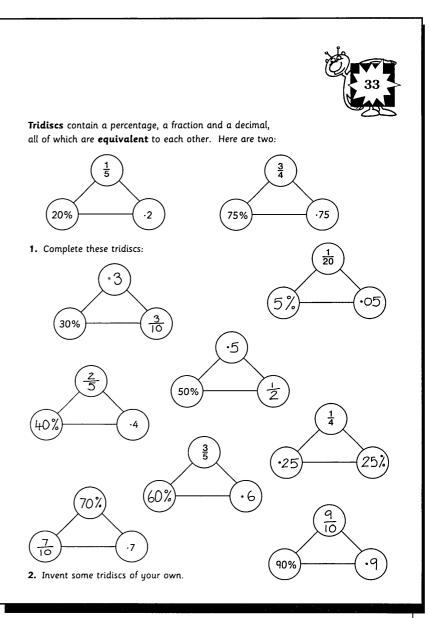
• Converting fractions to decimals and percentages.

#### SKILLS

 Expressing the equivalence of a fraction, a decimal and a percentage, when given one of them

#### NOTE

The activity can promote discussion about different possible solutions to the fraction parts e.g.  $\frac{2}{5}$  or  $\frac{4}{10}$ .

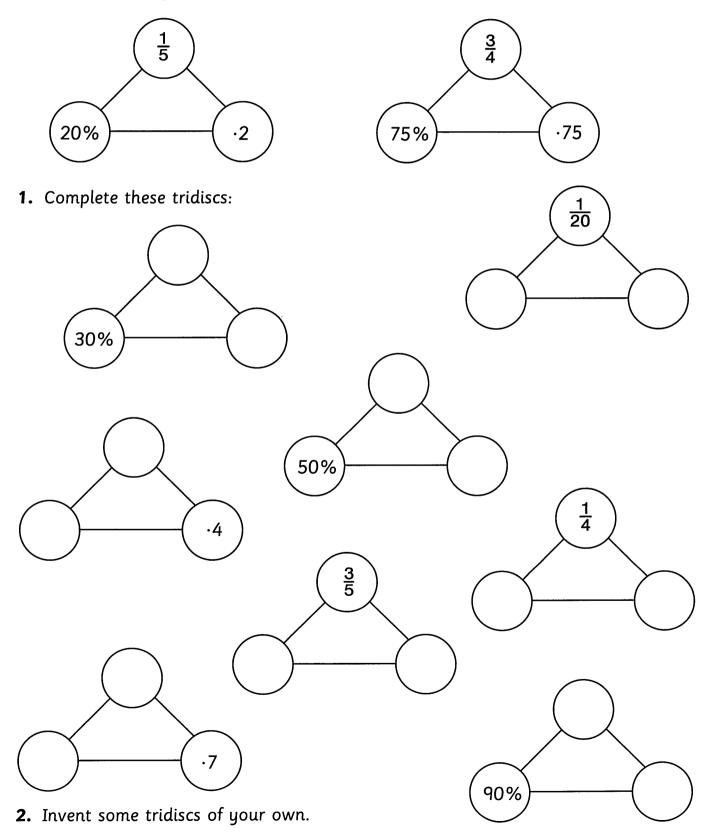


	Data Handling	Games Investigations		Algebra/S&S	Number Skills	
Starting					38 Colouring Fractions	
More		28 Wheels		14 Equivalent Fractions	8 Fraction Shades 27 Nearest 100	
Go Further With	<ul> <li>9 Inches and Centimetres</li> <li>18 Miles and Kilometres</li> </ul>	<ul><li>12 Decimate</li><li>14 Two Places</li><li>37 Four Rounds</li></ul>	20 Nearest Wholes		<ul> <li>28 Goal Percentages</li> <li>31 Fractions and Decimals</li> <li>36 Percentage Wheels</li> <li>39 Decimal Pyramids</li> </ul>	

## **Tridiscs**



**Tridiscs** contain a percentage, a fraction and a decimal, all of which are **equivalent** to each other. Here are two:





# **Multiplication Triangles**

LEVEL	UA	Ν	SSM	HD	A
I					
2					
3	٠				
4	•				
5	•				
6					

- Learning multiplication facts up to 10 × 10 and using them in multiplication and division problems.
- Factors and multiples.

#### SKILLS

- Multiplying single-digit numbers
- Recognising factors and multiples of numbers
- Using common factors

#### APPARATUS

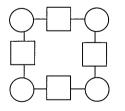
**Special Paper 5** 

#### NOTES

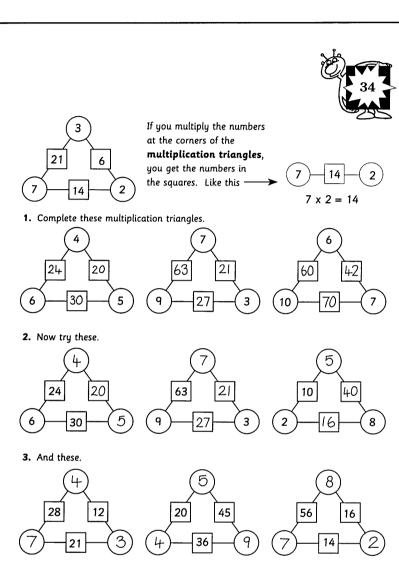
The first group of three are all straightforward and the next can be found by deduction. The last three are best solved by looking for common factors. Children can use Special Paper 5 when they make their own multiplication triangles.

#### EXTENSION

A further possibility is to make multiplication squares.



#### SPECTRUM LINKS

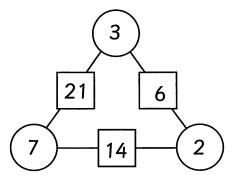


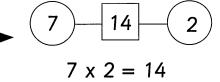
4. Invent some of your own multiplication triangles.

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More					24 Triangle Sums
Go Further With					14 Number Puzzles

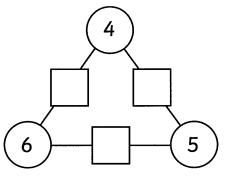
# **Multiplication Triangles**

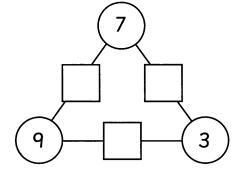


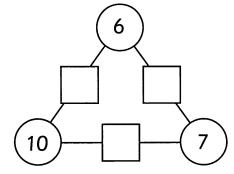




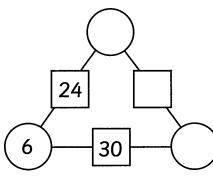
1. Complete these multiplication triangles.

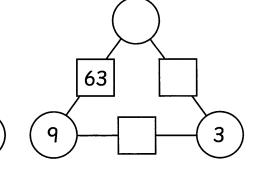


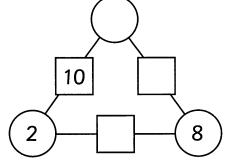




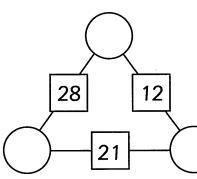
2. Now try these.

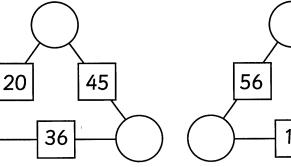


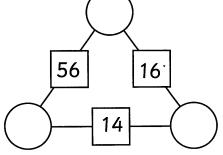




3. And these.







4. Invent some of your own multiplication triangles.



## **Mixed Totals**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3	•				
4	•	•			
5	•				
6					

Adding two three-digit numbers.
 Approximating to check the validity of addition calculations.

#### SKILLS

 Adding two three-digit numbers without a calculator

#### **APPARATUS**

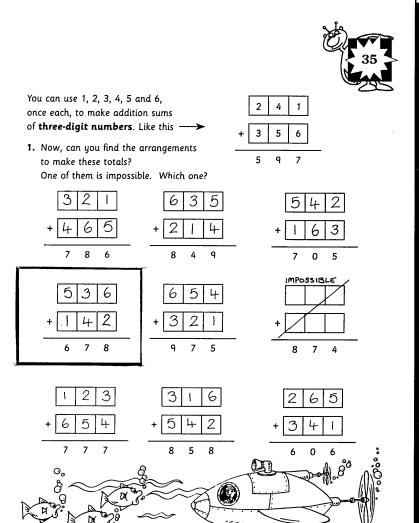
Numbered cards, 1-6

#### NOTES

Start by drawing a large outline of the three-digit addition. Then use different arrangements of the numbered cards to experiment for different totals.

#### EXTENSION

 Explore different possible answers for subtraction instead of addition.

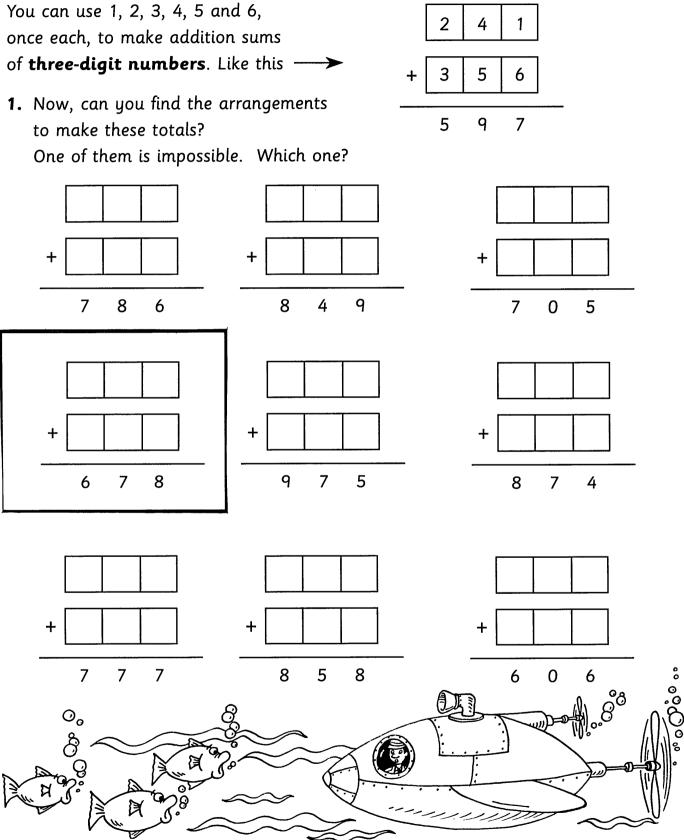


2. Can you make any other totals using the numbers 1 to 6 in this way?

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More					22 Nearly 60 36 Differences
Go Further With					17 Minus a Digit 27 Subtraction Guessing

### **Mixed Totals**





2. Can you make any other totals using the numbers 1 to 6 in this way?



## **Percentage Wheels**

LEVEL	UA	Ν	SSM	HD	A
1			Τ		
2					
3	•				
4	•				
5	•	•			
6					

Calculating percentages of a quantity.
Finding one number as a percentage of another.

#### SKILLS

- Finding the percentage of a quantity
- Expressing one quantity as a percentage of another

#### **APPARATUS**

Special Paper 6 for the initial activity and the extension

#### NOTE

Children can use Special Paper 6 when they invent their own wheels.

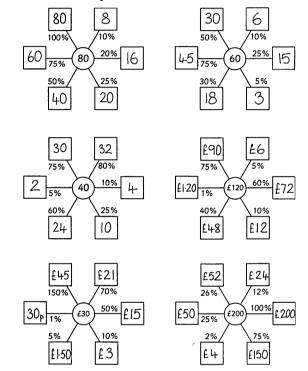
#### EXTENSION

Try reversing the process: make some wheels with all the boxes filled and ask the children to find the percentages to write on the spokes.



There is a number in the **hub** of each wheel and a **percentage** on each **spoke**. Use these to work out which number goes in the box.

1. Write the percentages of the centre number in the boxes. Two have been done for you.



 Invent your own percentage wheels and ask a friend to fill in the boxes. (Work out the answers for yourself, first.)

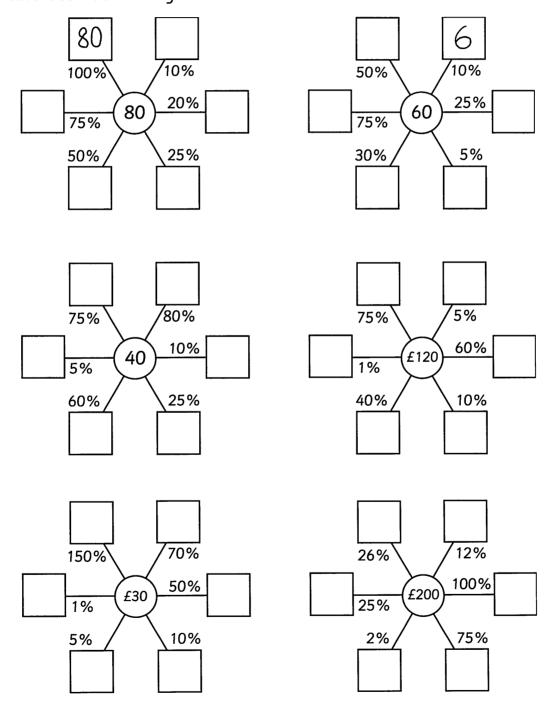
	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Go Further With					<ul><li>20 Multiple Percentages</li><li>28 Goal Percentages</li></ul>

### **Percentage Wheels**



There is a number in the **hub** of each wheel and a **percentage** on each **spoke**. Use these to work out which number goes in the box.

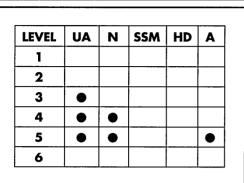
1. Write the percentages of the centre number in the boxes. Two have been done for you.



 Invent your own percentage wheels and ask a friend to fill in the boxes. (Work out the answers for yourself, first.)



### **Five Ways**



- Addition, subtraction, multiplication and division.
- Simple equations.

#### SKILLS

- Writing expressions for numbers using combinations of addition, subtraction, multiplication and division
- Using brackets

#### APPARATUS

Special Paper 7 for question 2 and the extension

#### NOTES

The activity can promote discussion about the need for brackets.

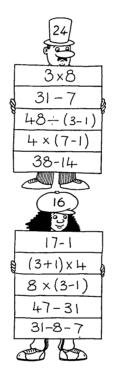
Special Paper 7 can be used for finding 'five ways' with some other numbers.

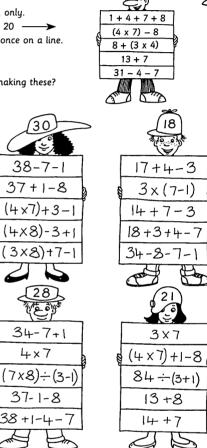
#### EXTENSION

Vary the original five numbers.

#### Use the digits 1, 3, 4, 7 and 8, only. Here are **five ways** of making 20 Each number can only appear once on a line.

1. Can you find five ways of making these?

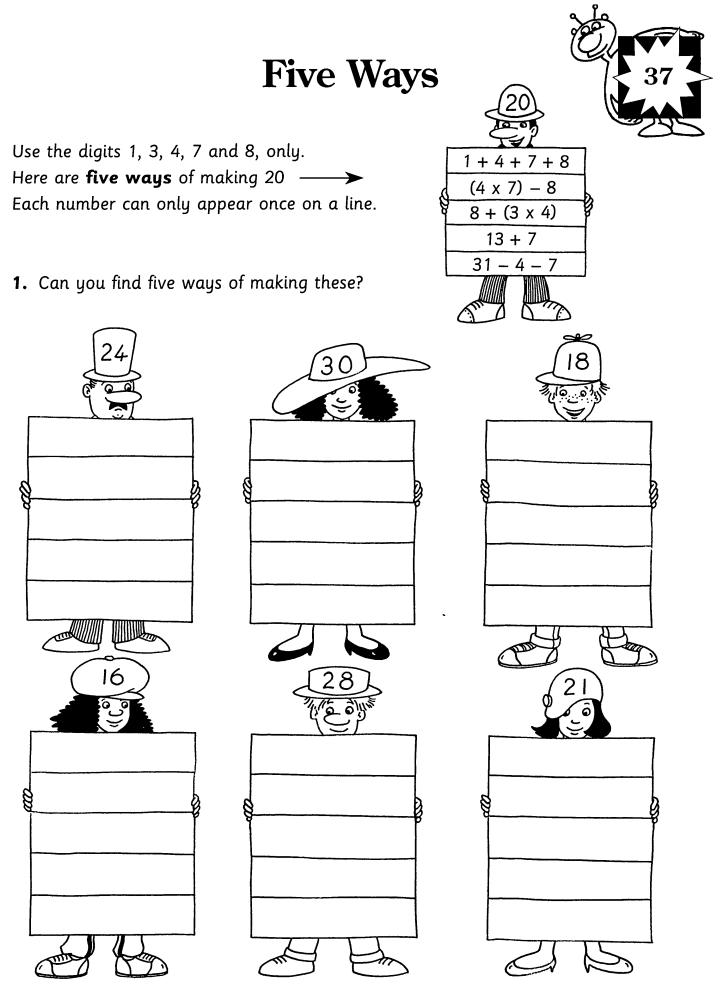




2. See if you can find five ways of making some other numbers.

SPEC	<b>TRUM</b>	LINKS

	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting		<ul><li>13 Big Match</li><li>18 Summary</li><li>27 Choosy</li></ul>	<ol> <li>10 Trios</li> <li>12 Keep Your Balance</li> <li>14 Card Tricks</li> </ol>	<ul><li>6 Shape Search</li><li>10 Stroking Cats</li><li>15 Hunt the Numbers</li></ul>	
More		3 Boxer 8 Dice Superstars	29 Asking Questions	10 Mystery People	<ol> <li>15 Dice Lines</li> <li>20 Equation Solving</li> <li>28 Arch Numbers</li> <li>31 Target Practice</li> </ol>
Go Further With		<ul><li>8 A Mouthful</li><li>33 Challenge</li><li>38 Switch</li></ul>	<ul><li>16 Number Nine</li><li>21 Equations</li><li>33 Signs</li></ul>	<ol> <li>Think of a Number</li> <li>Whodunnit?</li> <li>Number Tricks</li> </ol>	<ul><li>6 Countdown</li><li>7 Mixed Equations</li><li>13 Three Stones</li></ul>



2. See if you can find five ways of making some other numbers.



## **Take Your Pick**

LEVEL	UA	Ν	SSM	HD	A
1					
2					
3					
4					
5		٠			
6			1		

• Multiplying single-digit numbers of powers of 10.

#### SKILLS

 Estimating the result of multiplying together two numbers which are multiples of 10

#### APPARATUS

Calculator

#### NOTES

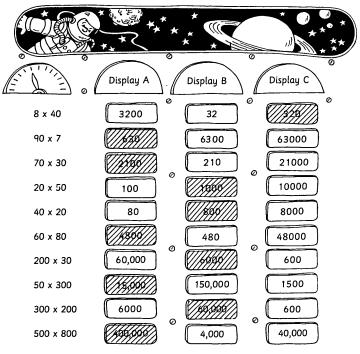
Accurate multiplication can first be attempted without a calculator, then checked with a calculator.

#### EXTENSIONS

- Ask children to produce two multiples of 10 which have a given product, such as 1800.
- Explore the different ways of reaching the same product, such as: 20 x 90, 30 x 60

The answer to each multiplication is on **display A**, **display B** or **display C**.

- 1. Guess the answer to each multiplication by ticking one of the displays.
- 2. Then use a calculator to find the correct display and colour it.



3. Write down ten more multiplications involving multiples of 10.

4. Guess the answers, then check with calculator.

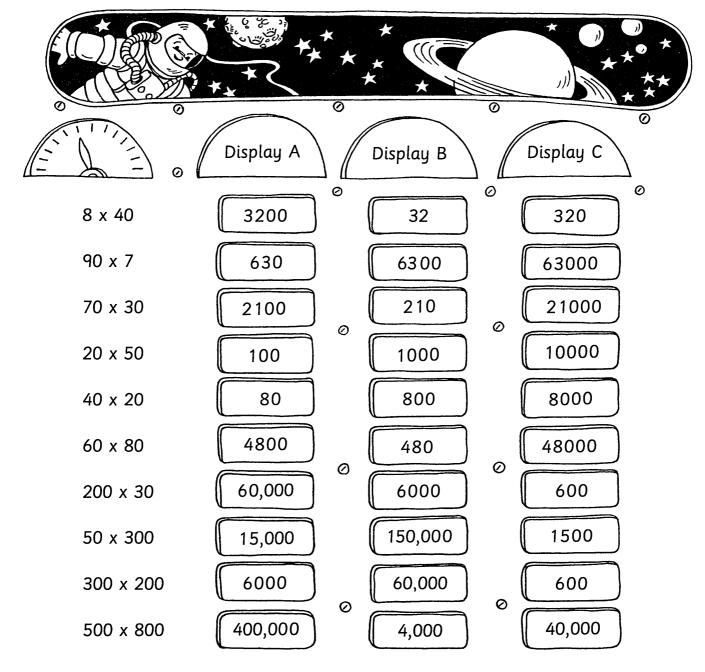
	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
More					40 Which Truck?

## **Take Your Pick**



The answer to each multiplication is on **display A**, **display B** or **display C**.

- 1. Guess the answer to each multiplication by ticking one of the displays.
- 2. Then use a calculator to find the correct display and colour it.



- **3.** Write down ten more multiplications involving multiples of 10.
- 4. Guess the answers, then check with calculator.



## **Decimal Pyramids**

LEVEL	UA	N	SSM	HD	A
1					
2					
3	•				
4	•	•			
5	•				
6			1		

• Solving addition problems using numbers with one decimal place.

#### SKILLS

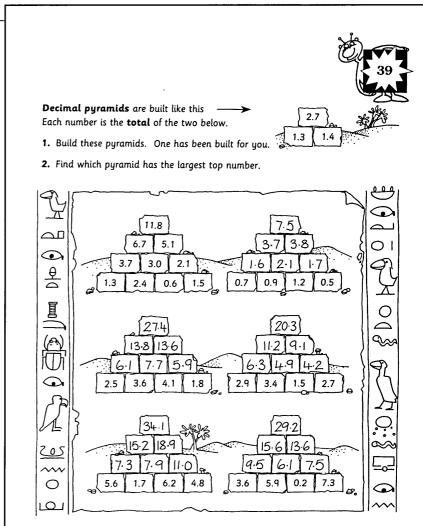
 Adding two decimal numbers each containing one decimal place

#### **APPARATUS**

Special Paper 8

#### NOTE

Use Special Paper 8 for recording the decimal pyramids required by question 2.



 See how many different top numbers you can find by trying different arrangements on the bottom layer of a pyramid for the decimal numbers: 1.5, 2.4, 3.8, 1.6.

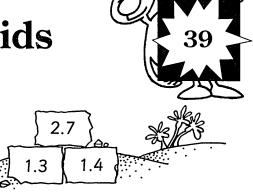
3.	Different arrangements of	1.5	2
	1.5, 2.4, 3.8, 1.6, produce	1.5	2
	six different top numbers:	1.5	3
		1.6	3
		3.8	2
		2.0	

ts of	1.5	2.4	3.8	1.6	(21.7)
ce	1.5	2.4	1.6	3.8	(17.3)
ers:	1.5	3.8	1.6	2.4	(20.1)
	1.6	3.8	1.5	2.4	(19.9)
	3.8	2.4	1.5	1.6	(17.1)
	3.8	1.5	1.6	2.4	(15.5)

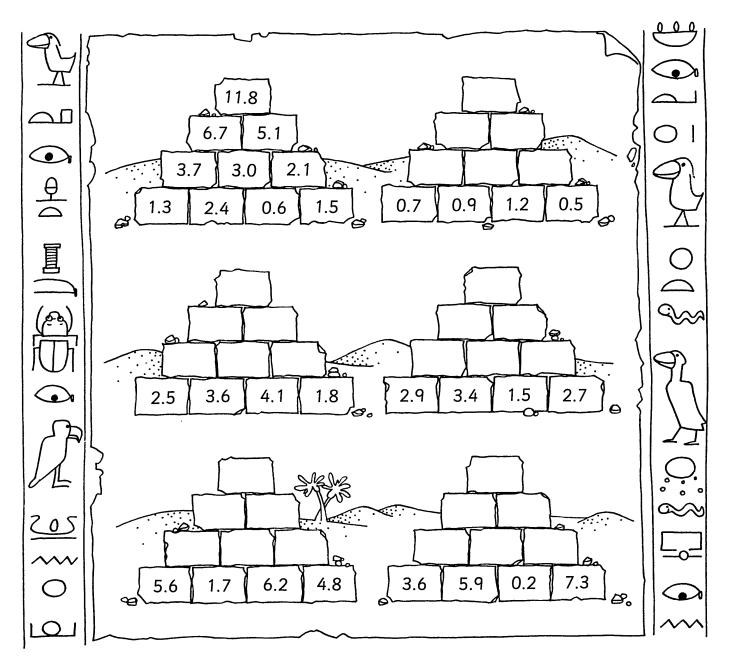
	Data Handling	Games	Investigations	Algebra/S&S	Number Skills
Starting					40 Difference Pyramids
More					11 Temperature Scales 27 Nearest 100
Go Further With	<ul> <li>9 Inches and Centimetres</li> <li>18 Miles and Kilometres</li> </ul>	12 Decimate 14 Two Places 37 Four Rounds	4 Top Brick 7 Up the Wall 20 Nearest Wholes		4 Tenths 31 Fractions and Decimals

# **Decimal Pyramids**

**Decimal pyramids** are built like this —— Each number is the **total** of the two below.



- 1. Build these pyramids. One has been built for you.
- 2. Find which pyramid has the largest top number.



3. See how many different top numbers you can find by trying different arrangements on the bottom layer of a pyramid for the decimal numbers:
1.5, 2.4, 3.8, 1.6.



### **Tower Blocks**

LEVEL	UA	N	SSM	HD	A
1					
2					
3		٠			
4		•			
5	•				
6					

• Addition, subtraction, multiplication and division.

#### SKILLS

 Finding expressions for different numbers using a restricted set of digits

#### **EXTENSION**

Allow a choice of five digits, but insist that each expression contains at least one multiplication or division sign. In each **tower block**, you may use any mathematical signs, but only the four digits at the top. Each digit can only appear once in a line.

 Try to complete each tower block by filling in every floor. Some have been done for you.

<u> </u>		نىپ		م الملي مع	کہ ۔۔۔۔۔ موجد د	~~^(	, My
M	<sup>2</sup> 4 <sup>3</sup>	ano	In	2 1 4 7	3 Cu	$\overline{\mathbb{Q}}$	2 4 3 5
10	(2×4)+3-1		20	(4+7-1) × Z		30	3×5×2
9	12-3	1522	19	17+2		29	25+4
8	2×4	hand marter	18	(2×7)+4		28	32-4
7	(2×4)-1	2	17	21-4	<u>بر ب</u>	27	23+4
6	3 x 2		16	14+2		26	25+4-3
5	3+2		15	(7 X 2) +I	, La	25	(3+2)×5
4	1+3		14	2×7		24	23+5-4
3	4-1	000 000 000 000	13	7+++2		23	32-5-4
2	4-2	0 0 0 0 0 0 0 0 0	12	14-2	0 0 0 0 0 0	22	25-3
1	3-2		11	4+7		21	24-3

 Repeat the activity with different sets of digits for each block. Shuffle a pack of playing cards containing the numbers 1 - 9 only. Then deal out three sets of four cards to represent the digits to be used for each block.

	Data Handling Game		Investigations	Algebra/S&S	Number Skills	
Starting		<ul><li>13 Big Match</li><li>18 Summary</li><li>27 Choosy</li></ul>	10 Trios 12 Keep Your Balance 14 Card Tricks	<ul><li>6 Shape Search</li><li>10 Stroking Cats</li><li>15 Hunt the Numbers</li></ul>		
More		3 Boxer 8 Dice Superstars	29 Asking Questions	10 Mystery People	<ul><li>15 Dice Lines</li><li>20 Equation Solving</li><li>28 Arch Numbers</li><li>31 Target Practice</li></ul>	
Go Further With		<ul><li>8 A Mouthful</li><li>33 Challenge</li><li>38 Switch</li></ul>	<ul><li>16 Number Nine</li><li>21 Equations</li><li>33 Signs</li></ul>	<ul><li>7 Number Tricks</li><li>10 Think of a Number</li><li>14 Whodunnit?</li></ul>	<ul><li>6 Countdown</li><li>7 Mixed Equations</li><li>13 Three Stones</li></ul>	

### **Tower Blocks**



In each **tower block**, you may use any mathematical signs, யீம but only the four digits at the top. Each digit can only appear once in a line. 1. Try to complete each tower block by filling in every floor. a o a a Some have been done for you. α a O 12 - 3q 23+4 3x2 0 0 0 0 ۵ ۵  $(7 \times 2) + 1$ 0 0 \_ 0 0 7+4+2 a o П D 0 0 п 0 0 0 0 0 0 0 0 a 🗆 🗆 

 Repeat the activity with different sets of digits for each block. Shuffle a pack of playing cards containing the numbers 1 - 9 only. Then deal out three sets of four cards to represent the digits to be used for each block.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	52	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57.	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

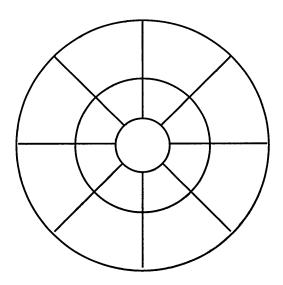
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

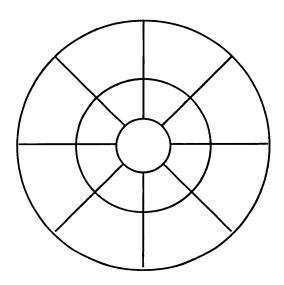
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

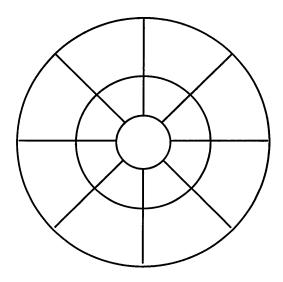
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

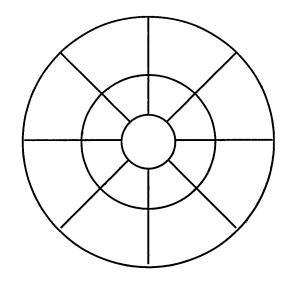
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

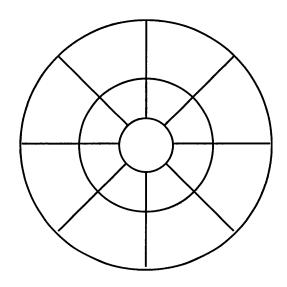
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

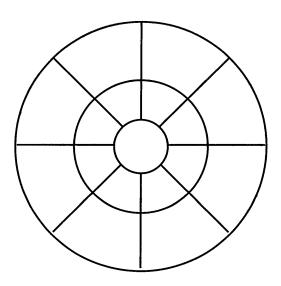


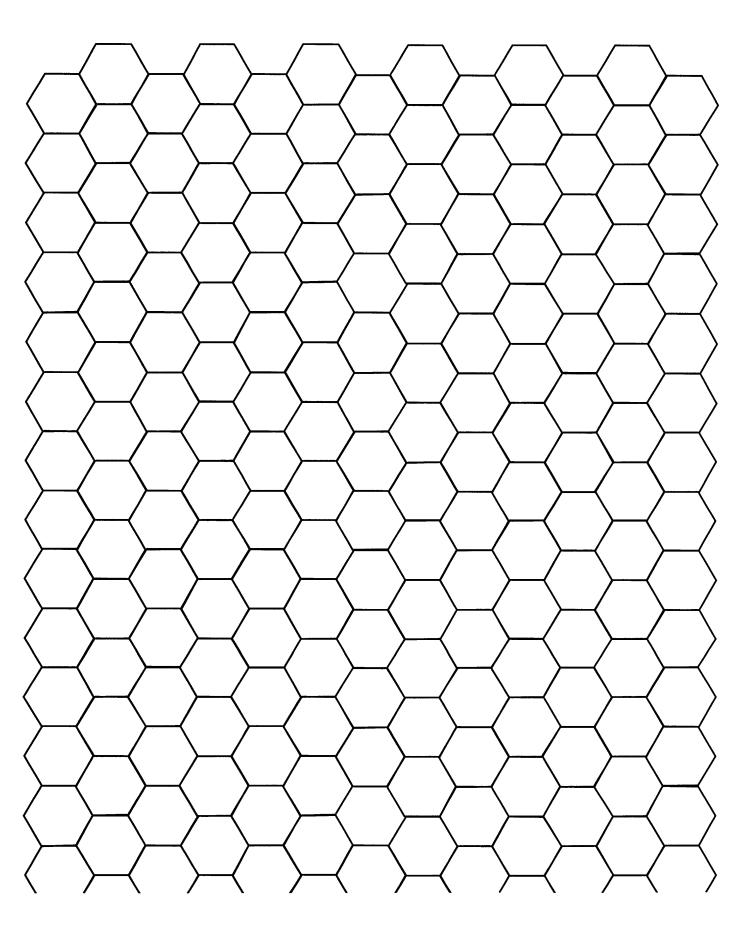


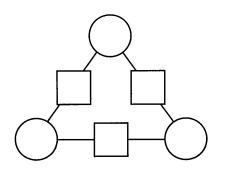


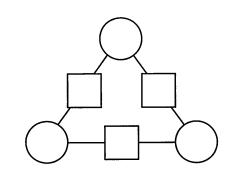


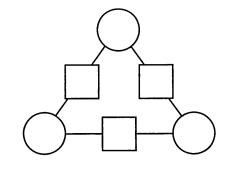


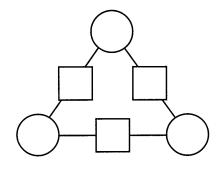


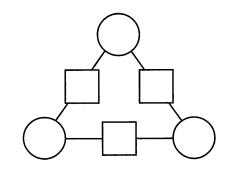


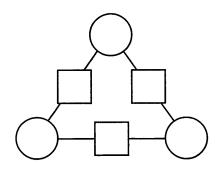


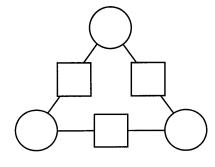


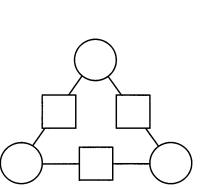


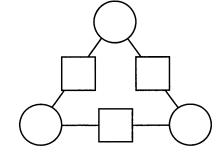


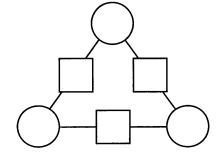


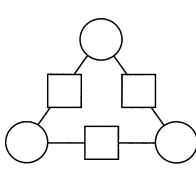


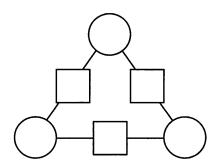


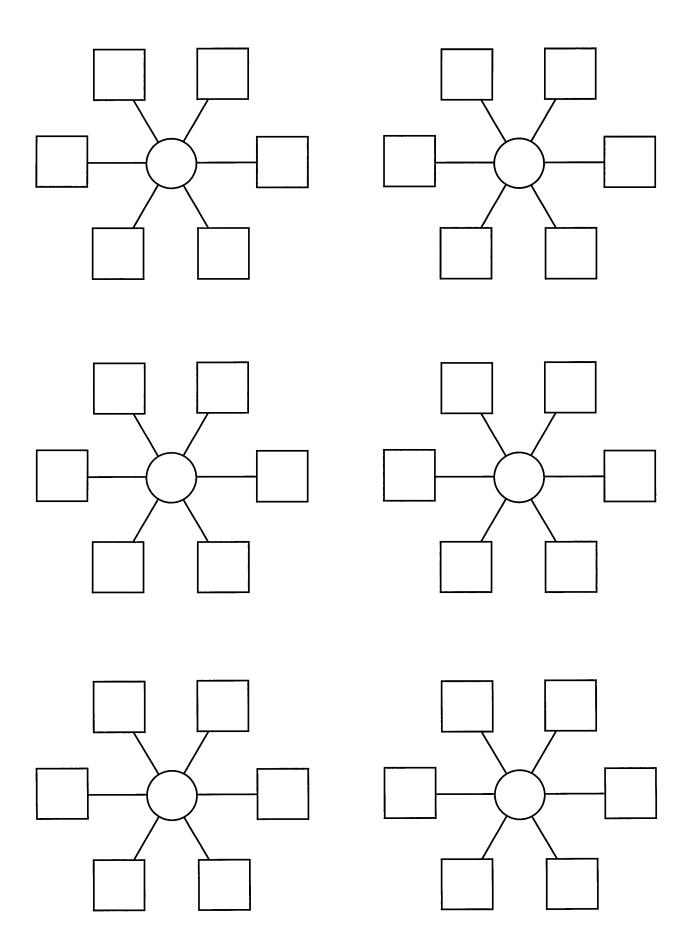


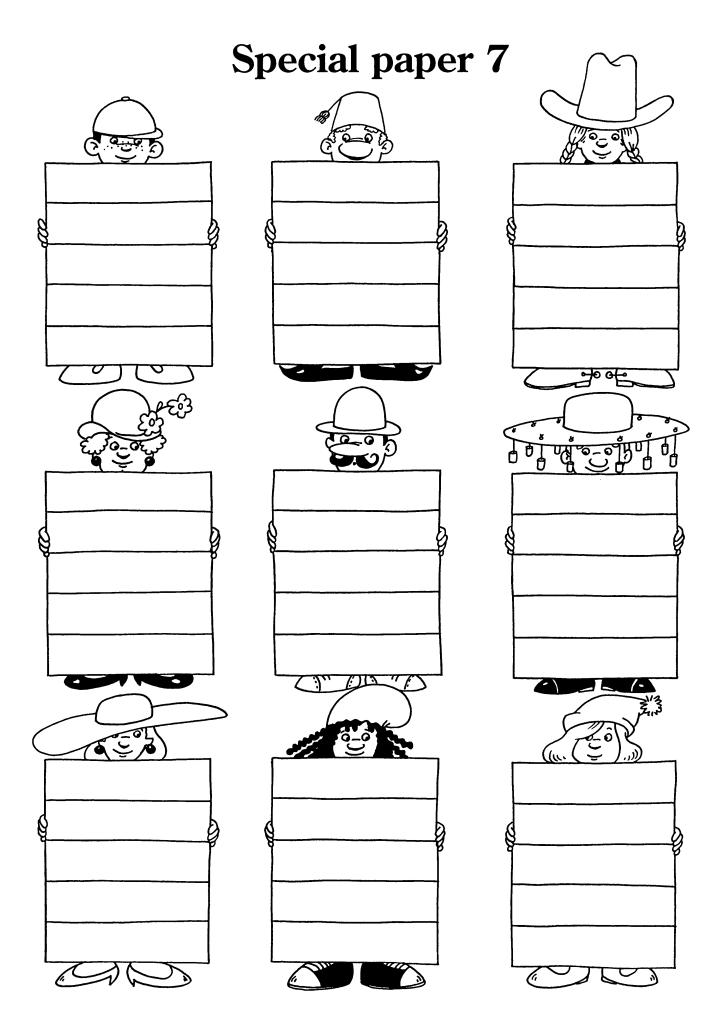


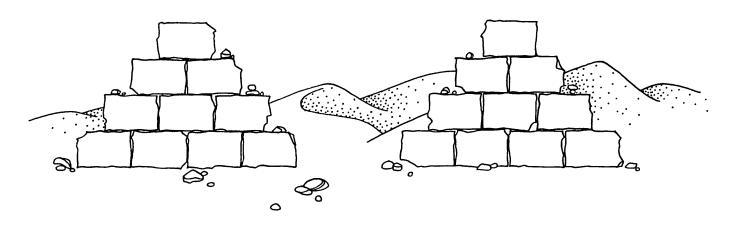


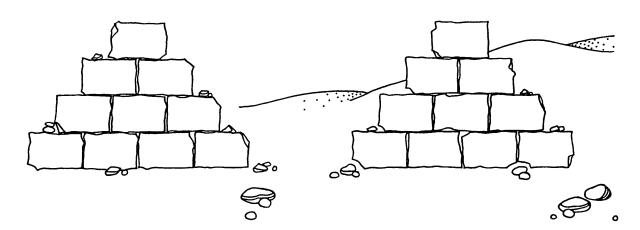


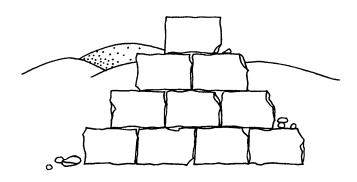


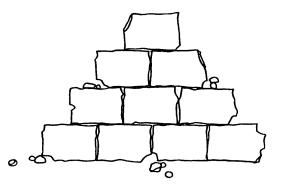




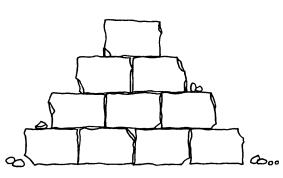


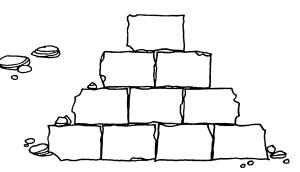












The number skills activities in **Spectrum Maths** come in three books which will complement and enrich any mathematics scheme.

**Starting Number Skills** for National Curriculum Levels 1–3 ISBN 000 312687 0

**More Number Skills** for National Curriculum Levels 2–5 ISBN 000 312688 9

**Go Further with Number Skills** for National Curriculum Levels 3–6 ISBN 000 312689 7

Clear easy-to-use instructions for the teacher:

- National Curriculum Attainment Levels at a glance
- Notes outlining possible results of the activities
- Ideas for consolidation, development and extension

Photocopiable pages for the children:

- Well-thought-out activities for children of 5–14 working at Levels 1 to 6
- Special sheets to help with recording
- Simple language

Go Further with Games

• Attractive presentation

Also available in the Spectrum Maths series:

For National Curriculum Levels 1–3 Starting Algebra/Shape and Space Starting Data Handling Starting Investigations Starting Games For National Curriculum Levels 2–5 More Algebra/Shape and Space More Data Handling More Investigations More Games For National Curriculum Levels 3–6 Go Further with Algebra/Shape and Space Go Further with Data Handling Go Further with Investigations

ISBN 000 312684 6 ISBN 000 312696 X ISBN 000 312693 5 ISBN 000 312690 0

ISBN 000 312685 4 ISBN 000 312697 8 ISBN 000 312694 3 ISBN 000 312691 9

ISBN 000 312686 2 ISBN 000 312698 6 ISBN 000 312695 1 ISBN 000 312692 7



