

# go further with NUMBER SKILLS 

# For National Curriculum levels 3-6 

## SPECTRUM MATHS

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## THE SPECTRUM MATHS SERIES

| Starting | More | Go Further With |
| :--- | :--- | :--- |
| Investigations | Investigations | Investigations |
| Games | Games | Games |
| Data Handling | Data Handling | Data Handling |
| Algebra/Shape and <br> Space | Space | Algebra/Shape and <br> Space |
| Number Skills | Number Skills | Number Skills |

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## INTRODUCTION


#### Abstract

Most schools use a mathematics scheme and teachers using these require a range of support material to supplement the scheme. Such material is provided by Spectrum Maths.


## SPECTRUM MATHS:

## NUMBER SKILLS

This is a series of three books of number activities primarily for Key Stages 1 and 2, though much of it is also appropriate for Key Stage 3.

The books are defined in terms of three levels. Broadly, these levels are :
Starting Number Skills (Years 1, 2 and 3)
More Number Skills (Years 3, 4 and 5)
Go Further With Number Skills (Years 5, 6 and 7).

Each book contains:
40 pupil activities in the form of photocopymasters. There are also detailed teacher's notes accompanying each activity and Special Papers in the form of photocopymasters to help children record their work.

## THE ACTIVITIES

A principal aim of mathematics teaching is to equip children to handle numbers with confidence. These activities provide an opportunity for children to practise number skills, with a strong emphasis on operational skills.

Each activity contains empty number boxes which children are required to complete, or sometimes colour. In most cases this is followed by an appropriate extension activity.

## USING THE ACTIVITIES

The activities do not, in general, attempt to teach children the number skills they need. They provide practice and reinforcement for children who, having been introduced to the skills, need experiences to develop them.

Activities can be selected by the teacher to suit particular needs and situations. They can be used in a variety of ways:

- to integrate into the school mathematics programme
- to consolidate other work in the school mathematics scheme
- to provide enrichment material at appropriate times
- to form support material for responding to wide ranges of ability
- to complement other activities within the Spectrum Maths series.

In particular, many activities in the Spectrum Games and Spectrum Investigations series can be used in conjunction with this series to provide rich and varied opportunities for children to develop their skills.

## THE TEACHER'S NOTES

The teacher's notes contain, for each activity:

- clear indications of the content area
- details of any necessary apparatus
- notes outlining suggestions for introducing the activities
- ideas for extending the activities
- answers to the activities
- clearly identifiable National Curriculum references on a grid
- reference to related activities within the book and other books in the Spectrum
Maths series.


## USING THE TEACHER'S NOTES

| LEVEL | UA | N | SSM | HD | A |
| :---: | :--- | :--- | :--- | :--- | :--- |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 |  |  |  |  |  |
| 4 |  |  |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |

KEY UA Using and Applying Mathematics N Number
SSM Shape, Space and Measures
HD Handling Data
A Algebra

## SKILLS

This section summarises the main content area of the activity.

## APPARATUS

Details of necessary apparatus or special paper photocopymasters which are included at the back of the book

## NOTE

This section contains suggestions for introducing the activity.

## EXTENSION

This contains ideas for extending the activity.

This section contains answers to the activity. These appear as a reduced copy of the pupil activity sheet.
The table on the left refers to the Programmes of Study and Levels $1-6$ of the National Curriculum. An algebra column has been included for teachers using this book at Key Stage 3.
An attempt has been made to locate, by means of dots in the table, the approximate content level for each activity, but it must be appreciated that many activities can be performed at a variety of levels.

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/ S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Starting |  |  |  |  |  |
| More | This section references related activities available throughout the Spectrum Series. The reference gives the number and title of the activity. |  |  |  |  |
| Go Further With |  |  |  |  |  |


| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  | $\bullet$ |  |  |  |
| 3 |  | $\bullet$ |  |  |  |
| 4 |  |  |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |

- Learning and using addition and subtraction facts.


## SKILLS

- Adding three single-digit numbers
- Searching for sets of numbers which have a given total


## APPARATUS

Numbered cards, 1-9

## NOTE

Suggest to the children that they draw a large wheel on paper, then use numbered cards placed on the wheel to help them find solutions.

The numbers in the big wheel make straight lines with the same totals.


This means: write the numbers 1 to 7 in the squares so that all cross-lines have a total of 14. Like this $\longrightarrow$


Try these. Use numbered cards to help you work out the answers. All the numbers must be different.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  | 23 Dice Sort |  |  |
| More |  |  |  |  |  |
|  |  | 26 Fifteens | $\mathbf{2}$ Lucky 13 |  | $\mathbf{2 5}$ Addition Grids <br> $\mathbf{3 4}$ Magic Windmills <br> $\mathbf{3 5}$ Magic Triangles <br> $\mathbf{3 8}$ Side Totals |

## The Big Wheel

The numbers in the big wheel make straight lines with the same totals.
 All the numbers must be different.


Magic Squares

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  | $\ddots$ |  |  |  |
| 3 |  |  |  |  |  |
| 4 |  |  |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |

- Learning and using addition and subtraction facts to 20.
- Adding three single-digit numbers.


## SKILLS

- Adding three single-digit numbers
- Searching for arrangements of numbers within a $3 \times 3$ grid for given row and column totals


## APPARATUS

Squared paper, scissors

## NOTE

The solutions can be deduced by systematically working round the square.

## EXTENSION

- Create $4 \times 4$ magic squares using, for example, the numbers 1-16.

This is a magic square.
All three rows, all three columns, and both diagonals have the same total

The magic number is: 24


1. Fill the gaps in these magic squares:

${ }^{n}$

2. Make magic square jigsaws. Cut these jigsaw pieces out of large squared paper. Then fit them together to make two magic squares - one of numbers, one of dots.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| More |  | 26 Fifteens |  |  | $\mathbf{1 8} 2 \times 2$ Addition <br> Squares <br> 25 Addition Grids <br> $\mathbf{2 6}$ Cloud Numbers |
| Go Further with |  |  |  |  | 22 Place Nine |

## Magic Squares

This is a magic square.
All three rows, all three columns, and both diagonals have the same total.

The magic number is: 24



1. Fill the gaps in these magic squares:


Magic
number:
is

|  | 4 |  |
| :--- | :--- | :--- |
|  | 8 |  |
| 7 | 12 |  |

Magic number:


is

Magic number:

is动


Magic number:


Magic 21 number:
2. Make magic square jigsaws. Cut these jigsaw pieces out of large squared paper. Then fit them together to make two magic squares - one of numbers, one of dots.


Grid Journeys

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  | $\ominus$ |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Addition of several single-digit numbers.
- Giving and understanding instructions for movement along a route.


## SKILLS

Finding a running total when adding several single-digit numbers
Following a path on a grid based on left, right, up, down movements

## EXTENSION

- Ask children to draw up a larger (say, $4 \times 4$ ) grid and work out routes for friends to follow.


Question 3: Some different journey scores starting at H are:

Two stages:
LU $-3+7+4=14$
UL $-3+5+4=12$
$R U-3+2+6=11$
UR $-3+5+6=14$
UU $-3+5+3=11$

Three stages:
UUR $-3+5+3+1=12$
UUL $-3+5+3+2=13$
URU $-3+5+6+1=15$
ULU $-3+5+4+2=14$
URD $-3+5+6+2=16$

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  |  |  | 32 Number Journey |
|  |  |  |  |  |  |

## Grid Journeys

The journey code is:
U - Up (north)
D - Down (south)
L - Left (west)
R - Right (east)

| A3 2 2 |  |  |
| :---: | :---: | :---: |
|  |  |  |
|  |  |  |

If you start at E and travel URDDL, your journey score is
$5+3+1+6+2+3=20$
Find these journey scores.

1. Start at E

LUR $\square$
$\square$
RDLL $\quad \square$
ULDRD $\square$
LDRRU $\square$
2. Start at $B$

RDDLL
LRRLD
LDRDR
DDRUU
DLDRU
3. Can you find ten different journey scores starting at $H$ ?
號


## 4

## Tenths

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ |  |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Using, with understanding, decimal notation, in the context of measurement.
- Approximating.


## SKILLS

- Locating position on a number line using tenths
- Rounding decimals to the nearest whole number


## APPARATUS

## Squared paper

## EXTENSION

- Children can be given further practice with the use of a 10-point number line on the wall. Vary the number cards at the ends of the line, for example:


Discussion will arise regarding the nearest whole number to 10.5 , for example.

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| More |  |  |  | 11 Temperature <br> Scales <br> Nearest 100 <br> Nearest 10 |  |
| Go Further With | 9 Inches and <br> Centimetres <br> 18 Miles and <br> Kilometres | 12 Decimate <br> $\mathbf{1 4}$ Two Places <br> $\mathbf{3 7}$ Four Rounds | $\mathbf{2 0}$ Nearest Wholes |  | $\mathbf{3 1 \text { Fractions and }}$Decimals <br> Decimal Pyramids |

## Tenths

These number lines are marked in tenths or fifths.

1. Complete the boxes to show where the arrow points on each number line. Show it in decimals. The first one has been done for you.

2. Draw your own number lines using squared paper.

Then draw boxes to show the position of some numbers.
Ask a friend to fill in the boxes.

## Powers

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | 0 | 0 |  |  |  |
| 4 | 0 | 0 |  |  |  |
| 5 | 0 |  |  |  |  |
| 6 |  |  |  |  |  |

- Learning multiplication facts up to $10 \times 10$ and using them in multiplication and division problems.
- Explaining number patterns and predicting subsequent numbers.
- Generalising, mainly in words, patterns which arise, eg 'square'.


## SKILLS

- Expressing numbers using power notation


## APPARATUS

## Calculators

## NOTES

Children may need help with the idea of 'to the power of one'. They may also need the term 'units digit' explained.
$3^{4}$ is a short way of writing $3 \times 3 \times 3 \times 3=81$. This is called 'three to the power of four'.
$2^{6}$ is a short way of writing $2 \times 2 \times 2 \times 2 \times 2 \times 2=64$ This is called ' $t w o$ to the power of six'.

1. Complete these boxes. One has been done for you.


Powers of 3
$3^{1}=3$
$\mathbf{3}^{2}=9$
$\mathbf{3}^{3}=27$
$3^{4}=81$
$3^{5}=243$


Powers of 4
$4^{1}=4$
$4^{2}=16$
$4^{3}=64$
$4^{4}=256$
$4^{5}=1024$
2. Write down some powers of 5 and 10.

Write down some powers of other numbers. Now complete these boxes:


Question 3: 729; 9
Question 4: The patterns in the units digits of powers are:
Powers of 2: 2, 4, 8, 6, .....
Powers of 3: 3, 9, 7, 1, ......
Powers of 4: 4, 6, 4, 6, .....
Powers of 5: 5, 5,5,5, .....
Powers of 6: 6, 6, 6, 6, ......
Powers of 7: 7, 9, 3, 1, ......
Powers of 8: 8, 4, 2, 6, .....
Powers of 9: 9, 1, 9, 1, ......

## Powers

$3^{4}$ is a short way of writing $3 \times 3 \times 3 \times 3=81$.
This is called 'three to the power of four'.
$\mathbf{2}^{6}$ is a short way of writing $2 \times 2 \times 2 \times 2 \times 2 \times 2=64$ This is called 'two to the power of six'.

1. Complete these boxes. One has been done for you.

## Powers of 2



Powers of 3

$$
\begin{aligned}
& 3^{1}=\square \\
& 3^{2}=\square \\
& 3^{3}=\square \\
& 3^{4}=\square 81 \\
& 3^{5}=\square
\end{aligned}
$$

Powers of 4
$4^{1}=\square$
$4^{2}=\square$
$4^{3}=\square$
$4^{4}=\square$
$4^{5}=\square$
2. Write down some powers of 5 and 10.

Write down some powers of other numbers. Now complete these boxes:

$10=1000,000$

3. The powers of 3 are: $3,9,27,81,243 \ldots$ and then what? The units digits of these are: $3,9,7,1,3 \ldots$ and then what?
4. Do they form a pattern?

Investigate the units digits of powers of other numbers.


## M <br>  <br> Countdown

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Addition, subtraction, and multiplication.
- Approximating.


## SKILLS

- Writing expressions for numbers using combinations of a given set of digits and operations


## NOTE

If children cannot find a solution, then they must aim to be as close as possible.

## EXTENSION

Ask the children to work with the first set of useful numbers, and suggest they try to make as many target numbers as possible, within a particular range (100-200, for example).

2. Invent a set of your own target numbers and useful numbers.

See how many targets you can reach.

## SPECTRUM.LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Starting |  | 13 Big Match <br> 18 Summary <br> 27 Choosy | 10 Trios <br> 12 Keep Your Balance <br> 14 Card Tricks | 6 Shape Search <br> 10 Stroking Cats <br> 15 Hunt the Numbers |  |
| More |  | 3 Boxer <br> 8 Dice Superstars | 29 Asking Questions | 10 Mystery People | 15 Dice Lines <br> 20 Equation Solving <br> 28 Arch Numbers <br> 31 Target Practice |
| Go Further With |  | 8 A Mouthful <br> 33 Challenge <br> 38 Switch | 16 Number Nine <br> 21 Equations <br> 33 Signs | 7 Number Tricks <br> 10 Think of a Number <br> 14 Whodunnit? | 7 Mixed Equations <br> 13 Three Stones <br> 15 A Special Date |

## Countdown

These target numbers can be made from the useful numbers.

1. Try these. Use each useful number once only in a line. You can use multiplication, addition and subtraction. How many of these ten targets can you reach? Write your answers in the results column. (The first one has been done for you.)
Target numbers

| Target numbers | Useful numbers | Result |
| :---: | :---: | :---: |
| 336 | $100{ }^{8} 4{ }^{3} 17$ | $(3 \times 100)+(4 \times 7)+8$ |
| 132 | $100{ }^{3} 5^{4} 62$ |  |
| 256 | 1001788 |  |
| 410 | $100{ }^{3} 5^{8} 41$ |  |
| 314 | $100{ }^{5} 6^{3} 21$ |  |
| 680 | $10078{ }^{7} 8^{4} 2$ |  |
| 823 | 20047235 |  |
| 856 | $20083{ }^{8} 46$ |  |
| 525 | 10027145 |  |
| 186 | 10026754 |  |

2. Invent a set of your own target numbers and useful numbers.

See how many targets you can reach.

Mixed Equations

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ | $\bullet$ |  |  |  |
| 6 |  |  |  |  |  |

- Addition, subtraction, multiplication and division.
- Simple equations.


## SKILLS

- Finding solutions to a variety of different equations with three missing digits to be selected from four
- Adding, subtracting, multiplying, dividing, and combinations of these


## NOTE

Discuss the need for brackets and encourage children to use these when they are creating their own equations.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Starting |  | 13 Big Match <br> 18 Summary <br> 27 Choosy | 10 Trios <br> 12 Keep Your Balance <br> 14 Card Tricks | 6 Shape Search <br> 10 Stroking Cats <br> 15 Hunt the Numbers |  |
| More |  | $\begin{array}{ll} \hline 3 & \text { Boxer } \\ \mathbf{8} & \text { Dice Superstars } \end{array}$ | 29 Asking Questions | 10 Mystery People | 15 Dice Lines <br> 20 Equation Solving <br> 28 Arch Numbers <br> 31 Target Practice |
| Go Further With |  | 8 A Mouthful <br> 33 Challenge <br> 38 Switch | 16 Number Nine <br> 21 Equations <br> 33 Signs | ```Number Tricks 10 Think of a Number 14 Whodunnit?``` | 6 Countdown <br> 13 Three Stones 15 A Special Date |

## Mixed Equations

These are called mixed equations because they use a mixture of signs. In each equation, fill in the boxes by choosing three numbers from the four in the picture. They must all be different from each other.

1. Start with these:


$$
\square+\square-\square=4
$$

$\square$
 $=51$

$$
\square+\square=40
$$

$\square$

$$
\square-\square=31
$$

$$
\begin{array}{|l|l}
\square & \\
& \square \\
\hline
\end{array}
$$

2. Now try these:
$\square$

$$
\square \times(\square-\square)=6
$$

$$
\square \times(\square-\square)=6
$$

3. Invent your own set of mixed equations, using any three of these digits $\square$


## Nearly 20

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Adding and subtracting two two-digit numbers
- Estimating and approximating to check the validity of addition and subtraction calculations.


## SKILLS

- Subtracting two-digit numbers
- Creating subtractions by selecting from a choice of digits to give a particular answer


## APPARATUS

Numbered cards, 1-9

## NOTE

This activity can be started by drawing a large outline of the subtraction on a piece of paper, selecting the appropriate numbered cards, and then trying different arrangements to produce the best solution.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  | $\mathbf{1 7}$ Totals |  |  |
| More |  |  | 25 4-Card Fun |  | $\mathbf{7}$ What's Missing? <br> $\mathbf{2 2}$ Nearly 60 <br> $\mathbf{3 6}$ Differences |
| Go Further With |  |  |  |  | 9 <br> $\mathbf{9 7}$ 5-Card Sums <br> Minus a Digit <br> $\mathbf{2 7}$ Subtration <br> Guessing |
|  |  |  |  |  |  |

## Nearly 20

1. Choose four digits from the cloud.

Make them into two numbers, and subtract one from the other.
Aim to get as close to 20 as possible.
Record the result, and then the

difference between it and 20. Like this


Difference:


Difference:

## M <br> 5-Card Sums

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |

- Adding two two-digit numbers.
- Estimating and approximating to check the validity of addition and subtraction calculations.


## SKILLS

- Adding a single-digit number to a twodigit number
- Arranging five digits to create both the addition and the result


## APPARATUS

Numbered cards, 1-9

## NOTES

Start by asking children to draw a large outline of the addition on a piece of paper. Then select the appropriate numbered cards for each addition and arrange them in search of a solution.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  | 17 Totals |  |  |
| More |  |  |  |  |  |
| Go Further With |  |  | 25 4-Card Fun |  | $\mathbf{7}$ What's Missing? <br> $\mathbf{2 2}$ N Narly 60 <br> 36 <br> Differences |
|  |  |  |  | $\mathbf{8}$ Nearly 20 <br> $\mathbf{1 7}$ Minus a Digit <br> 27 <br> Subtraction <br> Guessing <br> 35 Mixed Totals |  |

## 5-Card Sums

Use numbered cards. Use the digits from the clouds to make a 5 -card sum (including the answer).
The sums can be additions or subtractions Each digit can only be used once.


Double See-Saws

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  | 0 |  |  |  |
| 3 | $\ominus$ | $\bullet$ |  |  |  |
| 4 | 0 |  |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |

- Learning and using addition and subtraction facts.


## SKILLS

- Matching one number to the total of several others


## APPARATUS

Numbered cards, 1-20

## NOTES

Suggest to children that they draw a picture of a large double see-saw and use numbered cards on this to help them find answers. Note that the left-hand number must be even, for whole number solutions.


Question 2: possible solutions include 1 and 8,2 and 7, 3 and 6, 4 and 5 on the right-hand arm of the small see-saw.
Question 3: balance 10 with 5 and $2+3$ and with 5 and $1+4$. Balance 8 with 4 and $3+1$. Balance 6 with 3 and $1+2$.
Question 4: possible solutions include: balancing 20 with 10 and $4+6$; and balancing 16 with 8 and $6+2$.

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  | 12 Keep Your Balance |  | 30 <br> 3-Number <br> Se-Saws <br> 37 <br> 4-Number <br> See-Saws |
| More |  |  |  |  | 2 Pairs See-Saw |

## Double See-Saws

The total of the numbers on each side of each see-saw must balance. For example, the numbers on the small see-saw must balance: The total of the numbers on the small see-saw is 14 .

It must balance the other side of the big see-saw.
So, it ends up like this $\longrightarrow$


1. Complete the following double see-saws. They must all be different from each other.

2. Can you find four different solutions to the last see-saw in question one?
3. Can you find four different ways of balancing numbers, none of which are more than 10 ?
4. Can you find some ways of balancing numbers which are all even? Lowest Common Multiples

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | 0 |  |  |  |  |
| 4 |  | 0 |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |

- Multiplication facts up to $10 \times 10$.
- Patterns in multiples.

To find the lowest common multiples of 3 and 4: look in the $\times 3$ row, and in the $\times 4$ row.
List all the numbers you see in both ( $12,24,36$, etc.) and then choose the lowest one. It is $\mathbf{1 2 .}$

Now list the numbers which appear in both the $\times 6$ row and the $\times 10$ row. Find the lowest common multiple of 6 and 10. It is 30.
These lowest common multiples are written in the table below.


1. Now find some lowest common multiples for yourself.

First, choose one of the numbers on the left of the table below.
Then choose a number from along the bottom.
Using the table above, find the lowest common multiple of these two numbers.
When you have found it, write it on the table, in the right square.
2. Find the rest of the lowest common multiples to complete the table.


|  | 10 | 30 | 20 | 10 | 30 | 70 | 40 | 90 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{9}$ | 18 | 9 | 36 | 45 | 18 | 63 | 72 | 9 | 90 |
| $\mathbf{8}$ | 8 | 24 | 16 | 40 | 24 | 56 | 8 | 72 | 40 |
| $\mathbf{7}$ | 14 | 21 | 28 | 35 | 42 | 7 | 56 | 63 | 70 |
| $\mathbf{6}$ | 6 | 6 | 12 | 30 | 6 | 42 | 24 | 18 | 30 |
| $\mathbf{5}$ | 10 | 15 | 20 | 5 | 30 | 35 | 40 | 45 | 10 |
| $\mathbf{4}$ | $\mathbf{4}$ | 12 | $\mathbf{4}$ | 20 | 12 | 28 | 16 | 36 | 20 |
| $\mathbf{3}$ | 6 | 3 | 12 | 15 | 6 | 21 | 24 | 9 | 30 |
| $\mathbf{2}$ | $\mathbf{2}$ | 6 | $\mathbf{4}$ | 10 | 6 | 14 | 8 | 18 | 10 |
|  | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ |

## SPECTRUM LINKS

$\left.\begin{array}{|l|l|l|l|l|l|}\hline & \text { Data Handling } & \text { Games } & \text { Investigations } & \text { Algebra/S\&S } & \text { Number Skills } \\ \hline \text { More } & & & \begin{array}{l}\mathbf{6} \text { Table Patterns } \\ \mathbf{8} \text { Table Ends }\end{array} & \begin{array}{l}\mathbf{6} \text { Multiple Gaps } \\ \mathbf{1 2} \text { Sift the Multiples } \\ \mathbf{1 8} \text { Patterns With } 9\end{array} & \begin{array}{l}\text { 16 Factor Pairs } \\ \mathbf{2 6} \text { Cloud Numbers } \\ \mathbf{3 3}\end{array} \\ \hline \text { The Right Boxes }\end{array}\right\}$

## Lowest Common Multiples

To find the lowest common multiples of 3 and 4: look in the $\times 3$ row, and in the $\times 4$ row.
List all the numbers you see in both (12, 24, 36, etc.) and then choose the lowest one. It is 12.

Now list the numbers which appear in both the $\times 6$ row and the $\times 10$ row. Find the lowest common multiple of 6 and 10. It is 30 .
These lowest common multiples are written in the table below.

|  | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{x 3}$ | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 | 30 |
| $\mathbf{x 4}$ | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 |
| $\mathbf{x 5}$ | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 |
| $\mathbf{x 6}$ | 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 | 60 |
| $\mathbf{x 7}$ | 7 | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63 | 70 |
| $\mathbf{x 8}$ | 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 | 80 |
| $\mathbf{x 9}$ | 9 | 18 | 27 | 36 | 45 | 54 | 63 | 72 | 81 | 90 |
| $\mathbf{x 1 0}$ | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 |

1. Now find some lowest common multiples for yourself.

First, choose one of the numbers on the left of the table below.
Then choose a number from along the bottom.
Using the table above, find the lowest common multiple of these two numbers.
When you have found it, write it on the table, in the right square.
2. Find the rest of the lowest common multiples to complete the table.


| 10 |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 9 |  |  |  |  |  |  |  |  |  |
| 8 |  |  |  |  |  |  |  |  |  |
| 7 |  |  |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |  | 30 |
| 5 |  |  | 20 |  |  |  |  |  |  |
| 4 |  | 12 |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |
|  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |

Factor Show

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ | 0 |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Multiplication and division facts.
- Factors.


## SKILLS

- Searching for and recording factors of different numbers


## APPARATUS

Squared paper (for the extension)

## NOTES

Using a multiplication square can help in the search for factors, particularly with numbers beyond 24 . The resulting charts can provide a useful display to help with the exploration of factors and primes.

## EXTENSIONS

- Point out to children that most numbers have two or four factors. Ask, Which do not?
- Ask children to make an extended table on squared paper, to show factors of numbers greater than 24.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| More |  | 37 Snake Bite <br> 38 Divido | 6 Table Patterns <br> 7 Pick Your Cards <br> 8 Table Ends | 8 Completing Rectangles <br> 12 Sift the Multiples <br> 13 Table Patterns | 16 Factor Pairs <br> 26 Cloud Numbers |
| Go Further With |  | 13 Race Track <br> 20 Factor <br> 24 Multiple Choice | 9 Factors <br> 13 Tables | 4 Prime Numbers <br> 17 Factor Graph <br> 18 Multiplication Machines | 11 Lowest Common Multiples <br> 18 Factor Grids <br> 25 Highest Common Factors |

## Factor Show

This is a chart to show the factors of the numbers 1 to 24 .
The factors of 8 and 21 have been filled in for you. Can you work out how?


This shows that the factors
of 8 are: 1, 2, 4 and 8

This shows that $1,3,7$ and 21 are the factors of 21 .

1. Complete the table by writing in the factors of all the numbers from 1 to 24 .
2. Write about anything you notice.

Which numbers have the most factors? Which the least?

## Three Stones

| LEVEL | CA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ | $\bullet$ |  |  | $\bullet$ |
| 6 |  |  |  |  |  |

- Addition, subtraction, multiplication and division.
- Simple equations.


## SKILLS

- Creating expressions for numbers using combined operations of addition, subtraction, multiplication and division


## EXTENSION

- Ask the children to explore as many different solutions as can be found from a given number. For example:

18

$$
\begin{aligned}
& \text { (1) } 2=6+12 \\
& \text { (7) } 2=7+9+2 \\
& \text { (6) }=6+9+3
\end{aligned}
$$

## SPECTRUM LINKS



## Three Stones



You have a pile of stones to choose from. Use lines of three stones to make expressions for the target numbers in the table below.
For example:
Co
Qo



Target number

Expression
$6+12$

1. Write in as many expressions for the target numbers in the table as you can.

| Target <br> number | Expression | Target <br> number | Expression |
| :---: | :---: | :---: | :---: |
| 13 | 859 $(2 \times 4)+5$ | 18 | (6012 $6+12$ |
| 8 |  | 24 |  |
| 14 |  | 19 |  |
| 6 |  | 23 |  |
| 25 |  | 44 |  |
| 10 |  | 28 |  |
| 72 |  | 51 |  |

2. Make a new table. Write in some different target numbers and try again.

## Number Puzzles

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ | $\bullet$ |  |  |  |
| 6 |  |  |  |  |  |

- Learning and using addition and subtraction facts.
- Using 'trial and improvement' methods.


## SKILLS

- Adding and subtracting


## NOTES

The first three are straightforward. The next three can be solved by working round the puzzle from one corner.
The second group can be approached by trial and error. In some of these cases, more than one solution is possible. For example, the first one in this group:


If you add two numbers in circles, you get the number between them, in a square.

1. Complete the gaps in these.
$\begin{array}{ll}1 & 4 \\ 6 & 5 \\ 5 & 7\end{array}$

2. And these.

3. Look at any one of the second set of puzzles.

Can you find a different solution to the same puzzle?


SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| More |  |  |  |  | $\mathbf{2 4}$ Triangle Sums |
| Go Further With |  |  |  |  | $\mathbf{3 4}$ Multiplication <br> Triangles |

## Number Puzzles

If you add two numbers in circles, you get the number between them, in a square.

1. Complete the gaps in these.

2. And these.

3. Look at any one of the second set of puzzles. Can you find a different solution to the same puzzle?

## A Special Date

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ | $\bullet$ |  |  | $\bullet$ |
| 6 |  |  |  |  |  |

- Addition, subtraction, multiplication and division.
- Simple equations.


## SKILLS

- Creating expressions for different numbers using a set of digits and a choice of operation signs


## APPARATUS

Special Paper 1 for the extension

## EXTENSION

- Continue the activity using Special Paper 1.


1. Choose a date when something special happened, (not your birthdate). Suppose you choose: 23. 3. 93

Keeping the date digits in order and using signs, see how many different numbers you can make.

$$
\text { For example: } \begin{aligned}
& 2+3+3+9+3=20 \\
& 2+3+3+9-3=14 \\
& 23-3-9-3=8 \\
& 23+3-9+3=20
\end{aligned}
$$

2. Colour each number on this hundred square that you can make from your date. Write down how you made it. See how many of the numbers you can colour.


SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Starting |  | 13 Big Match <br> 18 Summary <br> 27 Choosy | 10 Trios <br> 12 Keep Your Balance <br> 14 Card Tricks | 6 Shape Search <br> 10 Stroking Cats <br> 15 Hunt the Numbers |  |
| More |  | 3 Boxer <br> 8 Dice Superstars | 29 Asking Questions | 10 Mystery People | 15 Dice Lines 20 Equation Solving <br> 28 Arch Numbers <br> 31 Target Practice |
| Go Further With |  | 8 A Mouthful <br> 33 Challenge <br> 38 Switch | 16 Number Nine <br> 21 Equations <br> 33 Signs | $\begin{aligned} & 7 \text { Number Tricks } \\ & 10 \text { Think of a Number } \\ & 14 \text { Whodunnit? } \end{aligned}$ | 6 Countdown <br> 7 Mixed Equations <br> 13 Three Stones |

## A Special Date

1. Choose a date when something special happened, (not your birthdate).

Suppose you choose: 23. 3. 93
Keeping the date digits in order and using signs, see how many different numbers you can make.
For example: $2+3+3+9+3=20$

$$
\begin{aligned}
& 2+3+3+9-3=14 \\
& 23-3-9-3=8 \\
& 23+3-9+3=20
\end{aligned}
$$

2. Colour each number on this hundred square that you can make from your date. Write down how you made it. See how many of the numbers you can colour.

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

3. Try again using your birthdate.


## Multiplying Grids

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\ominus$ |  |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Learning multiplication facts up to $10 \times 10$ and using them in multiplication and division problems.


## SKILLS

- Multiplying by single-digit numbers
- Dividing by single-digit numbers


## APPARATUS

Squared paper

## NOTES

Children creating their own multiplying grids, using multiplication in both directions, will find the numbers in the grids soon become large. It is easiest to start with very small numbers.
When using division, the top corner number has to be carefully selected so that it can be divided repeatedly by the same number.

This is a multiplying grid.

$\longrightarrow \times 2$ means multiply by 2 as you move along the row to the right.

1. This multiplying grid has been started. Fill in the gaps.

2. Now complete these:


$$
\sqrt{\qquad} \begin{array}{|c|c|c|c|c|}
\hline 16 & 48 & 144 & 432 & 1296 \\
\hline 8 & 24 & 72 & 216 & 648 \\
\hline 4 & 12 & 36 & 108 & 324 \\
\hline 2 & 6 & 18 & 54 & 162 \\
\hline 1 & 3 & 9 & 27 & 81 \\
\hline
\end{array}
$$

ふ
3. Invent your own multiplying grids on squared paper.

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/s\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  |  |  | 21 Grids |
| More |  |  |  |  | 13 Arrow Grids |

## Multiplying Grids

This is a multiplying grid．

|  |  |  |  |  | $\times 2$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2 | 4 | 8 |  |  |  |  |  |
| 3 | 6 | 12 | 24 |  |  |  |  |  |
|  | 9 | 18 | 36 |  |  |  |  |  |
| 3 | 72 |  |  |  |  |  |  |  |
| 27 | 54 | 108 | 216 |  |  |  |  |  |

1．This multiplying grid has been started．Fill in the gaps．
$\longrightarrow \quad \times 2$ means multiply by 2 as you
$\longrightarrow \quad \times 2$ means multiply by 2 as you
x 3 means multiply by $\mathbf{3}$ as you move down the column．


2．Now complete these：


约 s

## Minus A Digit

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  | $\bullet$ |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Subtracting two-digit numbers.
- Collecting data to produce a frequency table.


## SKILLS

- Subtracting two-digit numbers


## NOTE

Children can find out which digit is most often missing by making a frequency table like this:

| Digit | 123456789 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency |  |  |  |  |  |



Question 2: 1 is most often missing.

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  | $\mathbf{1 7}$ Totals |  |  |
| More |  |  |  |  |  |
| Go Further With |  |  | $\mathbf{2 5}$ 4-Card Fun |  | $\mathbf{7}$ What's Missing? <br> $\mathbf{2 2}$ Nearly 60 <br> $\mathbf{3 6}$ Differences |
|  |  |  |  | $\mathbf{8}$ Nearly 20 <br> 9 <br> 5-Card Sums <br> 27 <br> Subtraction <br> Guessing |  |

## Minus A Digit

1. Find the missing digits in these subtractions.


## Factor Grids

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | 0 |  |  |  |  |
| 4 | 0 | $\bullet$ |  |  |  |
| 5 | 0 |  |  |  |  |
| 6 |  |  |  |  |  |

- Learning multiplication facts up to $10 \times 10$ and using them in multiplication and division problems.
- Generalising, mainly in words, patterns, eg, 'factor'.


## SKILLS

- Finding factors
- Multiplying by single-digit numbers


## NOTES

Children will need to understand what is meant by a 'prime number'.

The activity can lead to exploration of numbers which have many factors. i.e. the numbers which appear in the bottom right-hand corner. So, for example, the factors of 36 are: 1, 2, 3, 4, $6,9,12,18,36$ ( 36 has nine factors altogether.)
The size of the grid determines the number of factors for the number in the bottom right-hand corner.


This is a factor grid.
You can use it to find, for example, the factors of 18: $1,2,3,6,9,18$.

or the factors of 12: $1,2,3,4,6,12$.


2. Now write the:

$$
\begin{array}{rl}
\text { factors of } 20 & \frac{1,2,4,5,10,20}{} \\
\text { factors of } 50 & \frac{1,2,5,10,25,50}{} \\
\text { factors of } 40 & 1,2,4,8,5,10,20,40 \\
\text { factors of } 100 & \frac{1,2,4,5,10,20,25,50,100}{}
\end{array}
$$

3. Complete these and write some lists of factors.

4. Make some more factor grids. You can make them by multiplying numbers in the grid by any pair of prime numbers ( $2,3,5,7,11,13$ and so on).

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| More |  | 37 Snake Bite 38 Divido | 6 Table Patterns <br> 7 Pick Your Cards <br> 8 Table Ends | 8 Completing Rectangles <br> 12 Sift the Multiples <br> 13 Table Pattern | 16 Factor Pairs <br> 26 Cloud Numbers |
| Go Further With |  | 13 Race Track <br> 20 Factor <br> 24 Multiple Choice | 9 Factors <br> 13 Tables | 4 Prime Numbers <br> 17 Factor Graph <br> 18 Multiplication Machines | 11 Lowest Common Multiples <br> 12 Factor Show <br> 25 Highest Common Factors |

## Factor Grids

This is a factor grid.
You can use it to find, for example, the factors of 18: $1,2,3,6,9,18$.

or the factors of 12: $1,2,3,4,6,12$.



1. Complete this factor grid:

2. Now write the:
factors of $\mathbf{2 0}$ $\qquad$
factors of $\mathbf{5 0}$ $\qquad$
factors of 40 $\qquad$
factors of $\mathbf{1 0 0}$ $\qquad$
3. Complete these and write some lists of factors.

4. Make some more factor grids. You can make them by multiplying numbers in the grid by any pair of prime numbers ( $2,3,5,7,11,13$ and so on).

## Remainder Charts

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Understanding remainders.
- Dividing two-digit numbers by single-digit numbers.


## SKILLS

- Dividing by single-digit numbers
- Finding remainders
- Multiplying by single-digit numbers


## NOTE

Discuss what it means when ' 0 ' appears in a chart.

## EXTENSION

- If the 16 remainder chart is extended, for example, from 2 to 16 , then all possible remainders can be analysed. This can lead to discussion about which numbers could not appear in this chart and why.


1. Divide 28 by other numbers, and complete the remainder chart. Write about anything you notice. (Hint: think about factors.)
2. Now complete these remainder charts:


| 35 |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Divide by |  |  |  |  |  |  |  |  |  |
| Remainder | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|  | 1 | 2 | 3 | 0 | 5 | 0 | 3 | 8 | 5 |

3. Make the charts longer to show remainders if you are dividing by numbers greater than 10.
4. Invent some remainder charts of your own.

Question 1: Children should notice that, when a number is divided by one of its factors, the remainder is 0 .

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Go Further With |  | 2 Remainders <br> 10 Sixes <br> 27 Sevens <br> 28 Divide It <br> 34 Left Overs | 9 Factors <br> 25 Divisions <br> 40 Remainders | 19 Remainder Tables |  |

## Remainder Charts

Here is the remainder chart for 28.

Divide by
Remainder

| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  | 3 | 4 |  |  |  |  |

1. Divide 28 by other numbers, and complete the remainder chart. Write about anything you notice. (Hint: think about factors.)
2. Now complete these remainder charts:

3. Make the charts longer to show remainders if you are dividing by numbers greater than 10.
4. Invent some remainder charts of your own.

Multiple Percentages

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Recognising and understanding
simple percentages.
- Multiplication facts.
- Multiples.


## SKILLS

- Expressing proportion as a percentage
- Recognising multiples of single-digit numbers


## APPARATUS

Special Paper 2 for the extensions

## NOTE

Ask children to make predictions about the percentages of, for example, the multiples of 5 , multiples of 6 , multiples of 7, and so on.

## EXTENSIONS

- Using Special Paper 2, children can make their own 100 charts and find percentages of other multiples.
- Extend to square numbers, prime numbers, etc. Use Special Paper 2 for this, too.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| More |  |  | 6 Table Patterns <br> 8 Table Ends | 6 Multiple Gaps <br> 12 Sift the Multiples <br> 18 Patterns With 9 | 16 Factor Pairs <br> 26 Cloud Numbers <br> 33 The Right Boxes |
| Go Further With | 26 Sevens <br> 36 Multiplication Tables | 17 Fives and Threes <br> 24 Multiple Choice | 13 Tables <br> 37 Multiples | 17 Factor Graph | 20 Goal Percentages <br> 33 Tridiscs <br> 36 Percentage Wheels |

## Multiple Percentages

In this activity you must find two things: multiples and percentages.
In this 100 chart, the multiples of 2 have been shaded.
There are 50 of them. So, the percentage of numbers which are multiples of 2 is:


1. Here the multiples of 2 and 3 have been shaded.
The percentage which are multiples of 2 or 3 is:
2. Colour these squares and find the percentages.

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

Percentage
which are
multiples
of 4 is:


Percentage which are multiples of 7 or 9 is:
$\square$


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

## Percentage

 which are multiples of 3 or 4 is:

## Percentage

or 5 is:

## which are <br> multiples of 3


$\square$

##  <br> Division Grids

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Dividing two-digit numbers by single-digit numbers.
- Recognising that multiplication and division are inverse operations.


## SKILLS

- Dividing two-digit numbers by singledigit numbers
- Multiplying as the inverse of dividing
- Adding two-digit numbers


## NOTE

In order to complete question 2, children may need some help in understanding that multiplication and division are inverse operations.

You can find the numbers in the right-hand grid by looking at the numbers in the same position in the left-hand grid and dividing them by the number in the star. For example:
\(\left.\begin{array}{|c|c|c|}\hline 6 \& 21 \& 15 <br>
\hline 18 \& 3 \& 24 <br>
\hline 12 \& 27 \& 9 <br>

\hline\end{array}\right\rangle \div 3<\)| 2 | 7 | 5 |
| :---: | :---: | :---: |
| 6 | 1 | 8 |
| 4 | 9 | 3 |

1. Complete the grid.

2. Now try these.

3. Find the totals of all the rows in each grid. What do you notice?
4. The row totals of the left-hand grids, when divided, give the row totals of the right-hand grids.

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  |  | 11 Addition Wheels |  |
| More |  | 38 Divido |  | 21 Multiplication |  |
| Wheels |  |  |  |  |  |

## Division Grids

You can find the numbers in the right-hand grid by looking at the numbers in the same position in the left-hand grid and dividing them by the number in the star.
For example:

| 6 | 21 | 15 |
| :---: | :---: | :---: |
| 18 | 3 | 24 |
| 12 | 27 | 9 |$\quad \div 3$| 2 | 7 | 5 |
| :---: | :---: | :---: |
| 6 |  |  |
|  |  |  |

1. Complete the grid.
2. Now try these.

| 8 | 36 | 12 |
| :---: | :---: | :---: |
| 20 | 4 | 32 |
| 16 | 28 | 24 |$\quad \div 4=$


| 14 | 42 | 7 |
| :--- | :--- | :--- |
| 49 | 28 |  |
|  | 56 |  |



|  | 42 |  |
| :--- | :--- | :--- |
| 12 |  | 30 |
|  | 48 |  |



| 4 | 1 |  |
| :--- | :--- | :--- |
|  |  | 3 |
|  | 8 | 7 |


|  |  | 25 |
| :--- | :--- | :--- |
| 45 | 30 |  |
| 10 |  |  |$\quad \div 5 \quad=$


|  |  |  |
| :--- | :--- | :--- |
|  |  | 5 |
| 3 |  | 9 |



## $[$ <br> Place Nine

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Learning and using adding and subtraction facts.
- Adding several single-digit numbers.


## SKILLS

- Adding and subtracting
- Seeking arrangements of numbers in a two-way table to match given totals


## APPARATUS

Numbered cards, 1-9

## NOTES

Ask children to draw a large $3 \times 3$ grid on paper, and use a set of numbered cards to place in the grid.
They can also make labels to represent the row and column totals, and place these in position for each puzzle. The task can be made easier by giving children an extra clue (number in a square).

$\begin{array}{lll}14 & 11 & 20\end{array}$


Each grid contains one each of the numbers from 1 to 9 . Both the row and column totals are given.
The puzzle is to put the numbers from
1 to 9 in the right positions.
Here is the solution


1. How many of these can you solve?

$\begin{array}{lll}15 & 14 & 16\end{array}$

2. What about these?

| 4 | 1 | 5 | 10 |
| :--- | :--- | :--- | :--- |
| 3 | 7 | 8 | 18 |
| 6 | 2 | 9 | 17 |
| 13 | 10 | 22 |  |


| 6 5 | 1 | 12 |
| :--- | :--- | :--- |
| 2 | 7 | 1 |
| 9 | 3 | 8 |
| 9 | 20 |  |
| 17 | 15 | 13 |



## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| More |  | 26 Fifteens |  |  | 18 2×2 Addition <br> Squares <br> 25 Addition Grids <br> 26 Cloud Numbers |
| Go Further With |  |  |  |  | 2 Magic Squares |

## Place Nine

|  |  |  |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |

Each grid contains one each of the numbers from 1 to 9 . Both the row and column totals are given. The puzzle is to put the numbers from 1 to 9 in the right positions. Here is the solution
$\begin{array}{lll}14 & 11 & 20\end{array}$

## 15

 Here is the solution $\longrightarrow$


1. How many of these can you solve?


|   1 14 <br>  2  12 <br> 12    |
| :--- |


$\begin{array}{lll}15 & 14 & 16\end{array}$

|  |  |  |
| :--- | :--- | :--- |
|  | 4 |  |
|  |  |  |

16
12
17
$18 \quad 12 \quad 15$
$\begin{array}{lll}15 & 15 & 15\end{array}$
2. What about these?

$13 \quad 10 \quad 22$

$\begin{array}{lll}17 & 15 & 13\end{array}$

$\begin{array}{lll}15 & 13 & 17\end{array}$

## Multiples of 10

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ |  |  |  |  |  |
| 2 |  | $\bullet$ |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |

Addition patterns.
Number patterns.
Addition of two-digit numbers.

## SKILLS

Adding sets of numbers to find totals which are multiples of 10

## NOTES

Ask the children to look for the sums of units digits which produce multiples of 10. For example, 1 and 9,2 and 8,3 and 7 , 5 and 5.

This grid contains many strips or groups of numbers whose total is a multiple of $\mathbf{1 0}$.

For example,
this strip has a total of 30 , which is a multiple of 10 .

| 12 |
| :--- |
| 18 |
| 30 |


| 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | 8 | 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 | 17 | 18 |
| 19 | 20 | 21 | 22 | 23 | 24 |
| 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 |

## III1111..



1. These are the outlines of strips or groups which have numbers whose total is a multiple of 10 . See how many you can find. They are all different.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  | 35 In the Window |  | 4Giraffe <br> 12 <br> Difference Dog <br> Elephant Tricks <br> More |
|  |  |  | 19Unit Digit <br> Patterns <br> Go Further With |  |  |

## Multiples of 10

This grid contains many strips or groups of numbers whose total is a multiple of $\mathbf{1 0}$.

For example, this strip has a total of 30 , which is a multiple of 10 .
 30

| 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | 8 | 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 | 17 | 18 |
| 19 | 20 | 21 | 22 | 23 | 24 |
| 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 |



1. These are the outlines of strips or groups which have numbers whose total is a multiple of 10 . See how many you can find. They are all different.
2. See how many strips or groups you can find in this grid with totals which are multiples of 10 .

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |



## Division Wheels

| LEVEL | UA | $\mathbf{N}$ | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ |  |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Dividing two-digit numbers by a single-digit number.
- Recognising that multiplication and division are inverse operations and using this to check calculations.


## SKILLS

- Dividing two-digit numbers by singledigit numbers
- Using multiplication as the inverse of division


## APPARATUS

Special Paper 3 for the extension activity

## NOTE

The table is given as a check. In the first instance, children should be encouraged to try completing the wheels without reference to it.

## EXTENSIONS

- Children can build their own division wheels, using Special Paper 3.
- They could take the activity further to include division by numbers greater than 10.
SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  |  |  | 11 Addition Wheels |
| More |  | 38 Divido |  |  | 21 Multiplication <br> Wheels |
| Go Further With |  | 10 Sixes <br> 27 <br> $\mathbf{2 8}$ Sevens <br> Divide It | $\mathbf{9 5}$ Factors <br> (ivisions <br> Remainders | 19 Remainder Tables | 21 Division Grids |

## Division Wheels

This part of the table shows these division facts:
$24 \div 6=4$
$24 \div 4=6$

1. Write down some more division facts for dividing by 8 , and then for dividing by 6 .
2. Complete these division wheels. The first one has been started for you, to show you how it works. Use the table to check your answers.

| $x$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 2 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 |
| 3 | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 | 30 |
| 4 | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 |
| 5 | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 |
| 6 | 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 | 60 |
| 7 | 7 | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63 | 70 |
| 8 | 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 | 80 |
| 9 | 9 | 18 | 27 | 36 | 45 | 54 | 63 | 72 | 81 | 90 |
| 10 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 |


3. Build your own division wheels using these divisions: $\div 2, \div 4, \div 6, \div 10$

Highest Common Factors

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Division facts.
- Factors.


## SKILLS

- Listing the factors of a number
- Finding the highest common factor of two numbers


## NOTE

The sheet is best preceded by an activity which involves searching for factors. For example: 18: 'Factor Grids' or 12: 'Factor Show'

On this grid you can show the highest common factors of pairs of numbers.
For example:
factors of 12 are: $1,2,3,4,6,12$
factors of 20 are: $1,2,4,5,10,20$
Common factors of 12 and 20 are: 1, 2, 4 (that means they are factors of both numbers).

The highest common factor of 12 and 20 is:

1. Complete the grid by finding the highest common factors of the other pairs of numbers.
2. Now complete these grids.

|  | 24 | 16 | 10 |
| :---: | :---: | :---: | :---: |
| 12 | 12 | 4 | 2 |
| 15 | 3 | 1 | 5 |
| 8 | 8 | 8 | 2 |


|  | 30 | 9 | 32 |
| :---: | :---: | :---: | :---: |
| 40 | 10 | 1 | 8 |
| 6 | 6 | 3 | 2 |
| 18 | 6 | 9 | 2 |



|  | 30 | 20 | 16 | 36 |
| :---: | :---: | :---: | :---: | :---: |
| 48 | 6 | 4 | 16 | 12 |
| 10 | 10 | 10 | 2 | 2 |
| 50 | 10 | 10 | 2 | 2 |


|  | 32 | 8 | 28 | 14 |
| :---: | :---: | :---: | :---: | :---: |
| 12 | 4 | 4 | 4 | 2 |
| 18 | 2 | 2 | 2 | 2 |
| 42 | 2 | 2 | 14 | 7 |

3. Draw your own grids, and invent your own numbers for finding the highest common factors.

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| More |  | 37 Snake Bite <br> 38 Divido | 6 Table Patterns <br> 7 Pick Your Cards <br> 8 Table Ends | 8 Completing Rectangles <br> 12 Sift the Multiples <br> 13 Table Patterns | 16 Factor Pairs <br> 26 Cloud Numbers |
| Go Further With |  | 13 Race Track <br> 20 Factor <br> 24 Multiple Choice | 9 Factors <br> 13 Tables | 4 Prime Numbers <br> 17 Factor Graph <br> 18 Multiplication Machines | 11 Lowest Common Multiples <br> 12 Factor Show <br> 18 Factor Grids |

## Highest Common Factors

On this grid you can show the
highest common factors of
pairs of numbers.
For example:
factors of 12 are: $1,2,3,4,6,12$
factors of 20 are: $1,2,4,5,10,20$
Common factors of 12 and 20 are: 1, 2, 4 (that means they are factors of both numbers).

|  | 12 | 15 | 8 |
| :--- | :--- | :--- | :--- |
| 6 |  |  |  |
| 20 | 4 |  |  |
| 16 |  |  |  |

The highest common factor of 12 and 20 is: 4

1. Complete the grid by finding the highest common factors of the other pairs of numbers.
2. Now complete these grids.


|  | 30 | 20 | 16 | 36 |
| :--- | :--- | :--- | :--- | :--- |
| 48 |  |  |  |  |
| 10 |  |  |  |  |
| 50 |  |  |  |  |


|  | 32 | 8 | 28 | 14 |
| :--- | :--- | :--- | :--- | :--- |
| 12 |  |  |  |  |
| 18 |  |  |  |  |
| 42 |  |  |  |  |

3. Draw your own grids, and invent your own numbers for finding the highest common factors. Hexanimals

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | 0 | 0 |  |  |  |
| 4 |  | 0 |  |  |  |
| 5 | 0 |  |  |  |  |
| 6 |  |  |  |  |  |

- Learning and using addition and subtraction facts to 20 .
- Adding mentally several single-digit numbers.


## SKILLS

- Finding sets of several numbers which have a given total


## APPARATUS

Special Paper 4, for the initial work and the extension

## NOTE

Children can use Special Paper 4 to create their own jungle and to record Hexanimals.

## EXTENSION

- Explore different Hexanimals on this grid. For example, start with a total of 10 , then 11 , then 12 , and so on, each time inviting children to find a Hexanimal.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  | 35 In the Window |  | $\mathbf{4}$Giraffe <br> 12 <br> Difference Dog <br> $\mathbf{3 1}$ Elephant Tricks <br> More |
|  |  |  |  | $\mathbf{1 9}$Unit Digit <br> Patterns <br> Go Further With |  |

## Hexanimals

Hexanimals are hidden in the Hexjungle.


1. Look at the numbers in each hexanimal's head.


## Subtraction Guessing

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 |  |  |  |  |  |
| 4 | 0 | 0 |  |  |  |
| 5 | 0 |  |  |  |  |
| 6 |  |  |  |  |  |

- Approximating to the nearest 10 .
- Subtracting two two-digit numbers.
- Estimating and approximating to check the validity of subtraction calculations.


## SKILLS

- Approximating results of subtracting
- Rounding numbers to the nearest 10
- Using a calculator as a check


## APPARATUS

Calculator

## EXTENSION

- This activity can be extended to much larger numbers which, for example, are rounded off to the nearest 100 ,
e.g.

4862
3104
1758 $\longrightarrow \begin{aligned} & 5000 \\ & 3000\end{aligned}$

3. Now guess the answers to these subtractions, then check with a calculator.

| 87 |
| ---: |
| 87 |
| -71 |

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| More |  |  |  |  | 22 Nearly 60 <br> 36 Differences <br> 40 Which Truck? |
| Go Further With |  |  |  |  | 17 Minus a digit |

## Subtraction Guessing


2. Now try these. Each time, find the differences between the guesses and the exact answers.

3. Now guess the answers to these subtractions, then check with a calculator.
87

-71 $\quad$| 128 |
| ---: |
| $-\quad 62$ |

## Goal Percentages

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | 0 |  |  |  |  |
| 4 | 0 | 0 |  |  |  |
| 5 | 0 | $\bullet$ |  |  |  |
| 6 |  |  |  |  |  |

- Recognising and understanding simple percentages.
- Calculating percentages.
- Extracting information from tables and lists.


## SKILLS

- Expressing proportions of 100, 50 and 25 as a percentage
- Finding percentages of a quantity
- Processing discrete data


## EXTENSIONS

- Find percentages when the sets of scores do not total 100,50 or 25.
- Sunday newspapers provide a range of data, and the percentages can be found using a calculator.


Here is a list of scores for 50 football matches.

| H A |  | H A |  | H A | H A | H A | H A | H A | H A |  | H A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-1 | 0-1 | 1-0 | 1-1 | 4-3 | 5-1 | 2-0 | 1-2 | 0.2 | 0-2 | 1-0 | 0-3 |
| 1-2 | 0-0 | 3-1 | 6-1 | 0-1 | 0-1 | 4-3 | 1-0 | 1-0 | 3-4 | 1-1 | 2.0 |
| 2-0 | 1-2 | 0-0 | 1-0 | 0-3 | 1-0 | 3-0 | 0-3 | 2-0 | 1-0 | 0-1 | 0-1 |
| 1-2 | 2-2 | 1-2 | 1-2 | 1-0 | 1-1 | 5-0 | 1-1 | 1-1 | 0-2 | 1-0 | 1-0 |
| 1-3 | 1-0 |  |  |  |  |  |  |  |  |  |  |

Out of 100 teams, three scored 4 goals.
So the percentage of teams scoring 4 goals is: $3 \%$

1. Find these percentages:

Teams scoring 0 goals $33 \%$
Teams scoring 1 goal $37 \%$
Teams scoring 2 goals $15 \%$
Teams scoring 3 goals $9 \%$

| Teams scoring 2 or more goals | $30 \%$ |
| :--- | ---: |
| Matches ending in a draw | $16 \%$ |
| Matches ending in a home win | $44 \%$ |
| Matches ending in an away win | $40 \%$ |

Here is a list of the scores in 25 hockey matches:

| $H$ | $A$ | $H$ | $A$ | $H$ | $A$ | $H$ | $A$ | $H$ | $A$ | $H$ | $A$ | $H$ | $A$ | $H$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | $\mathbf{A}$

## 2. Find these percentages:

| Teams scoring 0 goals | $16 \%$ |  | Teams scoring 2 or more goals |
| :--- | :--- | :--- | :--- |
|  |  | $44 \%$ |  |
| Teams scoring 1 goal | $40 \%$ |  | Matches ending in a draw |

## SPECTRUM LINKS

$\left.\begin{array}{|l|l|l|l|l|l|}\hline & \text { Data Handling } & \text { Games } & \text { Investigations } & \text { Algebra/S\&S } & \text { Number Skills } \\ \hline \text { More } & 18 \text { Arsenal v Liverpool } & & & & \\ \hline \text { Go Further With } & & & & & \begin{array}{l}\text { 20 Multiple } \\ \text { Percentages } \\ \text { S3 }\end{array} \\ \text { Tidiscs } \\ 36 \text { Percentage } \\ \text { Wheels }\end{array}\right]$

## Goal Percentages

Here is a list of scores for 50 football matches.

| H A | H A | H A | H A | H A | H A | H A | H A | H A | H A | H A | H A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-1 | 0-1 | 1-0 | 1-1 | 4-3 | 5-1 | 2-0 | 1-2 | 0-2 | 0-2 | 1-0 | 0-3 |
| 1-2 | 0-0 | 3-1 | 6-1 | 0-1 | 0-1 | 4-3 | 1-0 | 1-0 | 3-4 | 1-1 | 2-0 |
| 2-0 | 1-2 | 0-0 | 1-0 | 0-3 | 1-0 | 3-0 | 0-3 | 2-0 | 1-0 | 0-1 | 0-1 |
| 1-2 | 2-2 | 1-2 | 1-2 | 1-0 | 1-1 | 5-0 | 1-1 | 1-1 | 0-2 | 1-0 | 1-0 |
| 1-3 | 1-0 |  |  |  |  |  |  |  |  |  |  |

Out of 100 teams, three scored 4 goals.
So the percentage of teams scoring 4 goals is: $3 \%$

1. Find these percentages:

Teams scoring 0 goals $\square$ Teams scoring 2 or more goals $\square$
Teams scoring 1 goal $\square$ Matches ending in a draw $\square$
Teams scoring 2 goals $\square$ Matches ending in a home win $\square$
Teams scoring 3 goals $\square$ Matches ending in an away win $\square$
Here is a list of the scores in 25 hockey matches:

| $H$ A | $H$ | $A$ | $H$ | $A$ | $H$ | $A$ | $H$ | $A$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $H$ | $H$ | $H$ | $H$ | $A$ |  |  |  |  |
| $1-0$ | $3-1$ | $2-0$ | $1-1$ | $0-0$ | $1-4$ | $5-0$ | $2-1$ |  |
| $2-0$ | $3-3$ | $1-1$ | $4-1$ | $2-3$ | $1-1$ | $2-1$ | $1-2$ |  |
| $0-1$ | $3-1$ | $1-0$ | $1-1$ | $2-1$ | $1-6$ | $4-4$ |  |  |
| $4-2$ | $2-4$ |  |  |  |  |  |  |  |

2. Find these percentages:

Teams scoring 0 goals $\square$ Teams scoring 2 or more goals $\square$
Teams scoring 1 goal $\square$ Matches ending in a draw $\square$
Teams scoring 2 goals $\square$ Matches ending in a home win $\square$
Teams scoring 3 goals $\square$
Matches ending in an away win $\square$

## Consecutive Flowers

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Addition of several numbers.
- Number patterns.
- Generalising patterns in numbers.


## SKILLS

- Finding a set of consecutive whole numbers which have a given total
- Approximating by division


## NOTE

A useful starting technique is to locate approximate size of the numbers by dividing the centre number by the number of petals.

Consecutive flowers have consecutive numbers on the petals, with the total in the centre.


Question 3: flowers with 3 petals have centre numbers which are multiples of 3.
Question 4: flowers with 5 petals have centre numbers which are multiples of 5 .

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  |  |  | 2 Lucky Number <br> Sweets |
| More |  |  | 21 Three in a Row |  | 6 Consecutive Trains |
|  |  |  |  |  |  |

## Consecutive Flowers



Consecutive flowers have consecutive numbers on the petals, with the total in the centre.

1. Complete these flowers, by writing the numbers on the petals.


Fraction Wheels

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ | $\bullet$ |  |  |  |
| 6 |  |  |  |  |  |

- Recognising and understanding simple fractions.
- Calculating fractions of quantities.


## SKILLS

- Writing fractions of a quantity


## EXTENSION

- A reverse form of this activity is to provide children with all the numbers in the boxes, and invite them to write the appropriate fraction on each arm.



## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Starting |  |  |  |  | $\mathbf{3 8}$Colouring <br> Fractions <br> More |
|  |  | $\mathbf{2 8}$ Wheels |  | 14Equivalent <br> Fractions <br> Go Further With |  |

## Fraction Wheels

The number or amount in the centre of each fraction wheel can be divided into fractions. The fractions are written on the spokes of the wheel.

1. Write the fractions of the centre numbers in the boxes.

Two have been done for you.

2. Invent your own fraction wheels.

Fractions and Decimals

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ |  |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  | $\bullet$ |  |  |  |

Converting fractions to decimals.

## SKILLS

- Equating fractions to decimals
- Creating equivalent fractions and decimals with a given set of digits


## APPARATUS

Numbered cards, 0-10

## NOTES

Children could start by drawing a large outline of the boxes on a sheet of paper, then select the relevant numbered cards for each problem. Let them explore arrangements of the cards until they find a correct solution. A calculator can be used to check different arrangements.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Starting |  |  |  |  | 38 Colouring Fractions |
| More |  | 28 Wheels |  | 14 Equivalent Fractions | $\begin{aligned} & 8 \text { Fraction Shades } \\ & 27 \text { Nearest } 100 \end{aligned}$ |
| Go Further With | 9 Inches and Centimetres <br> 18 Miles and <br> Kilometres | 12 Decimate <br> 14 Two Places <br> 37 Four Rounds | 20 Nearest Wholes |  | 39 Decimal Pyramids |

## Fractions and Decimals

The numbers in the cloud can be used to make a fraction, and then a decimal, both equivalent (equal in size) to each other.
Like this:


Now try these.




## One Hundred

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | $\bullet$ |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Addition and subtraction.


## SKILLS

- Adding and subtracting, involving single-digit, two-digit and three-digit numbers
- Combining several operations, searching for an arrangement which gives a particular result


## NOTE

One strategy to finding a solution is to start with the largest numbers in each line and work down towards the smallest, making adjustments to the use of + and signs, as you progress.

Each line uses the digits 1 to 9 , in order to make 100.
The missing signs are either + or - .

1. Write the missing signs. One has been done for you.

2. Invent some of your own lines, using the digits 1 to 6 , and + and - signs, to make different answers. Test them out on a friend, with the signs missing.

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Starting |  | 13 Big Match <br> 18 Summary <br> 27 Choosy | 10 Trios <br> 12 Keep Your Balance <br> 14 Card Tricks | 6 Shape Search <br> 10 Stroking Cats <br> 15 Hunt the Numbers |  |
| More |  | 3 Boxer <br> 8 Dice Superstars | 29 Asking Questions | 10 Mystery People | 15 Dice Lines <br> 20 Equation Solving <br> 28 Arch Numbers <br> 31 Target Practice |
| Go Further With |  | 8 A Mouthful <br> 33 Challenge <br> 38 Switch | 16 Number Nine <br> 21 Equations <br> 33 Signs | $\begin{array}{\|rl\|} \hline 7 & \text { Number Tricks } \\ 10 & \text { Think of a Number } \\ 14 & \text { Whodunnit? } \end{array}$ | 6 Countdown <br> 13 Three Stones <br> 15 A Special Date |

## One Hundred



Each line uses the digits 1 to 9 , in order to make 100 . The missing signs are either + or - .

1. Write the missing signs. One has been done for you.

2. Invent some of your own lines, using the digits 1 to 6 , and + and - signs, to make different answers. Test them out on a friend, with the signs missing.

## Tridiscs

| LEVEL | HA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 |  |  |  |  |  |
| 4 |  |  |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  | $\bullet$ |  |  |  |

- Converting fractions to decimals and percentages.


## SKILLS

- Expressing the equivalence of a fraction, a decimal and a percentage, when given one of them


## NOTE

The activity can promote discussion about different possible solutions to the fraction parts egg. $\frac{2}{5}$ or $\frac{4}{10}$.

Tridiscs contain a percentage, a fraction and a decimal, all of which are equivalent to each other. Here are two:


1. Complete these tridiscs:


## SPECTRUM LINKS



Tridiscs


Tridiscs contain a percentage, a fraction and a decimal, all of which are equivalent to each other. Here are two:


1. Complete these tridiscs:

2. Invent some tridiscs of your own.


Multiplication Triangles

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | 0 |  |  |  |  |
| 4 | 0 | 0 |  |  |  |
| 5 | 0 |  |  |  |  |
| 6 |  |  |  |  |  |

If you multiply the numbers at the corners of the multiplication triangles, you get the numbers in the squares. Like this $\longrightarrow$


1. Complete these multiplication triangles.

Learning multiplication facts up to $10 \times 10$ and using them in multiplication and division problems.

- Factors and multiples.


## SKILLS

- Multiplying single-digit numbers
- Recognising factors and multiples of numbers
- Using common factors


## APPARATUS

Special Paper 5

## NOTES

The first group of three are all straightforward and the next can be found by deduction. The last three are best solved by looking for common factors. Children can use Special Paper 5 when they make their own multiplication triangles.

## EXTENSION

A further possibility is to make multiplication squares.



2. Now try these.

3. And these.

4. Invent some of your own multiplication triangles.

SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| More |  |  |  |  | 24 Triangle Sums |
| Go Further With |  |  |  |  | 14 Number Puzzles |

# Multiplication Triangles 



If you multiply the numbers
at the corners of the
multiplication triangles,
you get the numbers in the squares. Like this


$$
7 \times 2=14
$$

1. Complete these multiplication triangles.

2. Now try these.

3. And these.

4. Invent some of your own multiplication triangles.

Mixed Totals

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 |  | 0 |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |

- Adding two three-digit numbers.
- Approximating to check the validity of addition calculations.


## SKILLS

- Adding two three-digit numbers without a calculator


## APPARATUS

Numbered cards, 1-6

## NOTES

Start by drawing a large outline of the three-digit addition. Then use different arrangements of the numbered cards to experiment for different totals.

## EXTENSION

- Explore different possible answers for subtraction instead of addition.



## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| More |  |  |  |  | 22 Nearly 60 <br> 36 Differences |
| Go Further With |  |  |  | 17 Minus a Digit <br> 27 Subtraction <br> Guessing |  |

## Mixed Totals

You can use 1, 2, 3, 4, 5 and 6, once each, to make addition sums of three-digit numbers. Like this $\longrightarrow$

1. Now, can you find the arrangements to make these totals?


One of them is impossible. Which one?

$\begin{array}{lll}7 & 7 & 7\end{array}$


2. Can you make any other totals using the numbers 1 to 6 in this way?

Percentage Wheels

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ |  |  |  |  |
| 5 | $\bullet$ | $\bullet$ |  |  |  |
| 6 |  | $\bullet$ |  |  |  |

- Calculating percentages of a quantity.
- Finding one number as a percentage of another.

There is a number in the hub of each wheel and a percentage on each spoke. Use these to work out which number goes in the box.

1. Write the percentages of the centre number in the boxes.

Two have been done for you.


## EXTENSION

- Try reversing the process: make some wheels with all the boxes filled and ask the children to find the percentages to write on the spokes.

2. Invent your own percentage wheels and ask a friend to fill in the boxes. (Work out the answers for yourself, first.)

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Go Further With |  |  |  |  | 20 Multiple <br> Percentages <br> Goal Percentages |
|  |  |  |  |  |  |

## Percentage Wheels



There is a number in the hub of each wheel and a percentage on each spoke. Use these to work out which number goes in the box.

1. Write the percentages of the centre number in the boxes.

Two have been done for you.

2. Invent your own percentage wheels and ask a friend to fill in the boxes. (Work out the answers for yourself, first.)

Five Ways

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ | $\bullet$ |  |  | $\bullet$ |
| 6 |  |  |  |  |  |

- Addition, subtraction, multiplication and division.
- Simple equations.


## SKILLS

- Writing expressions for numbers using combinations of addition, subtraction, multiplication and division
- Using brackets


## APPARATUS

Special Paper 7 for question 2 and the extension

## NOTES

The activity can promote discussion about the need for brackets.

Special Paper 7 can be used for finding 'five ways' with some other numbers.

Use the digits $1,3,4,7$ and 8 , only. Here are five ways of making $20 \longrightarrow$ Each number can only appear once on a line.

1. Can you find five ways of making these?

2. See if you can find five ways of making some other numbers.

## EXTENSION

- Vary the original five numbers.


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Starting |  | 13 Big Match <br> 18 Summary <br> 27 Choosy | 10 Trios <br> 12 Keep Your Balance <br> 14 Card Tricks | 6 Shape Search <br> 10 Stroking Cats <br> 15 Hunt the Numbers |  |
| More |  | 3 Boxer <br> 8 Dice Superstars | 29 Asking Questions | 10 Mystery People | 15 Dice Lines <br> 20 Equation Solving <br> 28 Arch Numbers <br> 31 Target Practice |
| Go Further With |  | 8 A Mouthful <br> 33 Challenge <br> 38 Switch | 16 Number Nine <br> 21 Equations <br> 33 Signs | 10 Think of a Number <br> 14 Whodunnit? <br> 7 Number Tricks | $\begin{aligned} 6 & \text { Countdown } \\ 7 & \text { Mixed Equations } \\ 13 & \text { Three Stones }\end{aligned}$ |

## Five Ways

Use the digits 1, 3, 4, 7 and 8, only. Here are five ways of making 20
 Each number can only appear once on a line.

1. Can you find five ways of making these?

2. See if you can find five ways of making some other numbers.

## Take Your Pick

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 |  |  |  |  |  |
| 4 |  |  |  |  |  |
| 5 |  | 0 |  |  |  |
| 6 |  |  |  |  |  |

- Multiplying single-digit numbers of powers of 10 .


## SKILLS

- Estimating the result of multiplying together two numbers which are multiples of 10


## APPARATUS

Calculator

## NOTES

Accurate multiplication can first be attempted without a calculator, then. checked with a calculator.

## EXTENSIONS

- Ask children to produce two multiples of 10 which have a given product, such as 1800.
- Explore the different ways of reaching the same product, such as:
$20 \times 90,30 \times 60$


## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :--- | :--- | :--- | :--- | :--- | :---: |
| More |  |  |  |  | 40 Which Truck? |
|  |  |  |  |  |  |

## Take Your Pick

The answer to each multiplication is on display A, display B or display C.

1. Guess the answer to each multiplication by ticking one of the displays.
2. Then use a calculator to find the correct display and colour it.

3. Write down ten more multiplications involving multiples of 10 .
4. Guess the answers, then check with calculator.

Decimal Pyramids

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ |  |  |  |  |
| 4 | $\bullet$ | $\bullet$ |  |  |  |
| 5 | $\bullet$ |  |  |  |  |
| 6 |  |  |  |  |  |

- Solving addition problems using numbers with one decimal place.


## SKILLS

- Adding two decimal numbers each containing one decimal place


## APPARATUS

Special Paper 8

## NOTE

Use Special Paper 8 for recording the decimal pyramids required by question 2 .

Decimal pyramids are built like this $\longrightarrow$ Each number is the total of the two below.

1. Build these pyramids. One has been built for you.

2. Find which pyramid has the largest top number.

3. See how many different top numbers you can find by trying different arrangements on the bottom layer of a pyramid for the decimal numbers: 1.5, 2.4, 3.8, 1.6.
4. Different arrangements of

| 1.5 | 2.4 | 3.8 | 1.6 | $(21.7)$ |
| :--- | :--- | :--- | :--- | :--- |
| 1.5 | 2.4 | 1.6 | 3.8 | $(17.3)$ |
| 1.5 | 3.8 | 1.6 | 2.4 | $(20.1)$ |
| 1.6 | 3.8 | 1.5 | 2.4 | $(19.9)$ |
| 3.8 | 2.4 | 1.5 | 1.6 | $(17.1)$ |
| 3.8 | 1.5 | 1.6 | 2.4 | $(15.5)$ |

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Starting |  |  |  |  | 40 Difference Pyramids |
| More |  |  |  |  | 11 Temperature Scales <br> 27 Nearest 100 |
| Go Further With | 9 Inches and Centimetres <br> 18 Miles and Kilometres | 12 Decimate <br> 14 Two Places <br> 37 Four Rounds | 4 Top Brick <br> 7 Up the Wall 20 Nearest Wholes |  | 4 Tenths <br> 31 Fractions and Decimals |

## Decimal Pyramids

Decimal pyramids are built like this
Each number is the total of the two below.

1. Build these pyramids. One has been built for you.

2. Find which pyramid has the largest top number.

3. See how many different top numbers you can find by trying different arrangements on the bottom layer of a pyramid for the decimal numbers: 1.5, 2.4, 3.8, 1.6 .

## Tower Blocks

| LEVEL | UA | N | SSM | HD | A |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 | $\bullet$ | 0 |  |  |  |
| 4 | $\bullet$ | 0 |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |

- Addition, subtraction, multiplication and division.


## SKILLS

- Finding expressions for different numbers using a restricted set of digits


## EXTENSION

- Allow a choice of five digits, but insist that each expression contains at least one multiplication or division sign.

In each tower block, you may use any mathematical signs, but only the four digits at the top.
Each digit can only appear once in a line.

1. Try to complete each tower block by filling in every floor. Some have been done for you.

2. Repeat the activity with different sets of digits for each block.

Shuffle a pack of playing cards containing the numbers 1-9 only. Then deal out three sets of four cards to represent the digits to be used for each block.

## SPECTRUM LINKS

|  | Data Handling | Games | Investigations | Algebra/S\&S | Number Skills |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Starting |  | 13 Big Match <br> 18 Summary <br> 27 Choosy | 10 Trios <br> 12 Keep Your Balance <br> 14 Card Tricks | 6 Shape Search <br> 10 Stroking Cats <br> 15 Hunt the Numbers |  |
| More |  | 3 Boxer <br> 8 Dice Superstars | 29 Asking Questions | 10 Mystery People | 15 Dice Lines <br> 20 Equation Solving <br> 28 Arch Numbers <br> 31 Target Practice |
| Go Further With |  | 8 A Mouthful <br> 33 Challenge <br> 38 Switch | 16 Number Nine <br> 21 Equations <br> 33 Signs | 7 Number Tricks <br> 10 Think of a Number <br> 14 Whodunnit? | 6 Countdown <br> 7 Mixed Equations <br> 13 Three Stones |

## Tower Blocks

In each tower block, you may use any mathematical signs, but only the four digits at the top. Each digit can only appear once in a line.

1. Try to complete each tower block by filling in every floor.
 Some have been done for you.

2. Repeat the activity with different sets of digits for each block.

Shuffle a pack of playing cards containing the numbers 1-9 only.
Then deal out three sets of four cards to represent the digits to be used for each block.

## Special paper 1

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 52 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

## Special paper 2

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
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| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
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| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
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| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
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| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

Special paper 3


## Special paper 4



Special paper 5
18 8 $8^{8}$ Ri ${ }^{8}$
$\qquad$

## Special paper 6




## Special paper 8




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